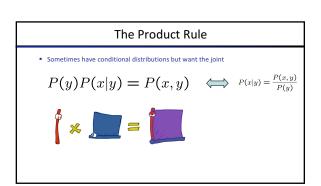
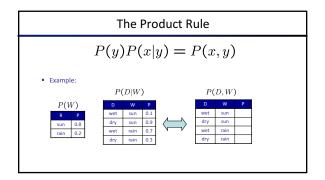
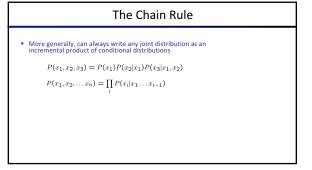
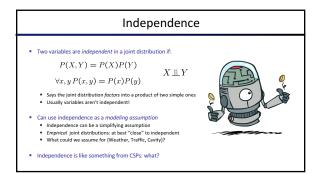


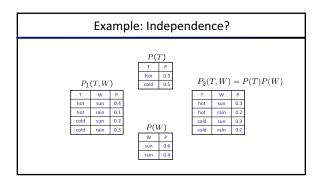
Inference by Enumeration Computational problems? Worst-case time complexity O(dⁿ) Space complexity O(dⁿ) to store the joint distribution

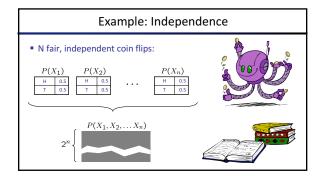


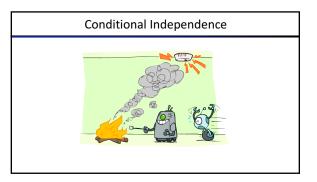


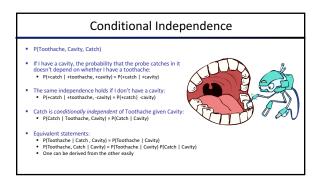


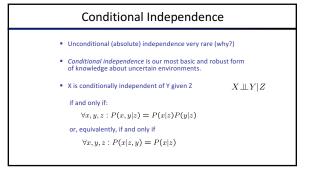




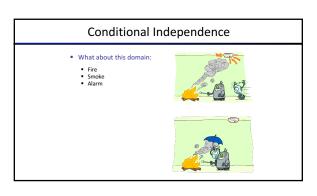


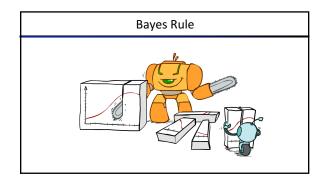


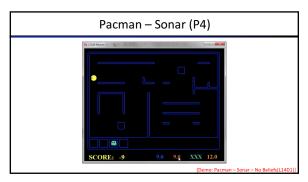


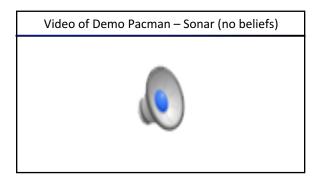


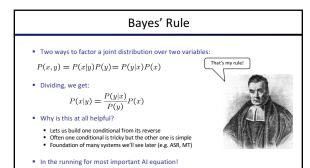




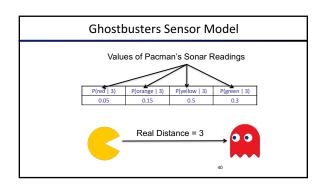


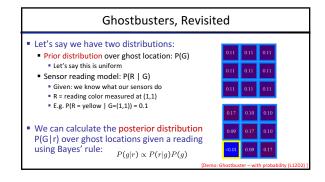


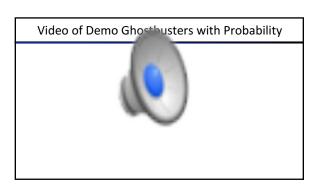




Inference with Bayes' Rule $P(\text{cause}|\text{effect}) = \frac{P(\text{effect}|\text{cause})P(\text{cause})}{P(\text{effect})}$ * Example: * M: meningitis, S: stiff neck $P(+m) = 0.0001 \\ P(+s|+m) = 0.8 \\ P(+s|-m) = 0.01 \end{bmatrix} \text{Example givens}$ $P(+m|+s) = \frac{P(+s|+m)P(+m)}{P(+s)} = \frac{P(+s|+m)P(+m)}{P(+s|+m)P(+m)+P(+s|-m)P(-m)} = \frac{0.8 \times 0.0001}{0.8 \times 0.0001 + 0.01 \times 0.999}$ • Note: posterior probability of meningitis still very small = 0.0079







Probability Recap

- Conditional probability
- $P(x|y) = \frac{P(x,y)}{P(y)}$
- Product rule
- P(x,y) = P(x|y)P(y)
- Chain rule
- $P(X_1, X_2, \dots X_n) = P(X_1)P(X_2|X_1)P(X_3|X_1, X_2) \dots$ $= \prod_{i=1}^{n} P(X_i|X_1, \dots, X_{i-1})$ $P(x|y) = \frac{P(y|x)}{P(y)}P(x)$
- Bayes rule
- $\begin{tabular}{ll} \blacksquare & {\rm X,Y independent\ if\ and\ only\ if:} & \forall x,y:P(x,y)=P(x)P(y) \\ \end{tabular}$
- \blacksquare X and Y are conditionally independent given Z: $X \perp\!\!\!\perp Y | Z$ if and only if: $\forall x,y,z: P(x,y|z) = P(x|z)$
 - $\forall x, y, z : P(x, y|z) = P(x|z)P(y|z)$