# CSE 473: Artificial Intelligence Constraint Satisfaction Dieter Fox Based on slides adapted Luke Zettlemoyer, Dan Klein, Stuart Russell or Andrew Moore

# What is Search For?

- Models of the world: single agent, deterministic actions, fully observed state, discrete state space
- Planning: sequences of actions
  - The path to the goal is the important thing
  - Paths have various costs, depths
  - Heuristics to guide, fringe to keep backups
- Identification: assignments to variables
  - The goal itself is important, not the path
  - All paths at the same depth (for some formulations)
  - CSPs are specialized for identification problems















## Varieties of Constraints

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  - Unary constraints involve a single variable (equiv. to shrinking domains):
    - $SA \neq green$
  - Binary constraints involve pairs of variables:

 $SA \neq WA$ 

- Higher-order constraints involve 3 or more variables: e.g., cryptarithmetic column constraints
- Preferences (soft constraints):
  - E.g., red is better than green
  - Often representable by a cost for each variable assignment
    Gives constrained optimization problems
  - (We'll ignore these until we get to Bayes' nets)

## Real-World CSPs

- Assignment problems: e.g., who teaches what class
- Timetabling problems: e.g., which class is offered when
- and where? Hardware configuration
- Transportation scheduling
- Factory scheduling
- Floorplanning
- Fault diagnosis
- Interpretended in the second secon
- Many real-world problems involve real-valued variables...

## Standard Search Formulation

- Standard search formulation of CSPs (incremental)
- Let's start with a straightforward, dumb approach, then fix it
- States are defined by the values assigned so far
  Initial state: the empty assignment, {}
  - Successor function: assign a value to an unassigned variable
  - Goal test: the current assignment is complete and satisfies all constraints







Can solve n-queens for n ≈ 25

### 







# Improving Backtracking

- General-purpose ideas give huge gains in speed
- Ordering:
  - Which variable should be assigned next?
  - In what order should its values be tried?
- Filtering: Can we detect inevitable failure early?
- Structure: Can we exploit the problem structure?





















































#### Summary

- CSPs are a special kind of search problem: States defined by values of a fixed set of variables · Goal test defined by constraints on variable values
- Backtracking = depth-first search with one legal variable assigned per node
- Variable ordering and value selection heuristics help significantly
- Forward checking prevents assignments that guarantee later failure .
- Constraint propagation (e.g., arc consistency) does additional work to constrain values and detect inconsistencies
- The constraint graph representation allows analysis of problem structure
- Tree-structured CSPs can be solved in linear time .
- Iterative min-conflicts is usually effective in practice



















## GA's for Locomotion

Ever wonder what it would be like to see evolution happening right before your eyes?