


| Bayes' Net Semantics |
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| - A set of nodes, one per variable $X$ $P\left(A_{l}\right) \quad \ldots \quad P\left(A_{n}\right)$ <br> - A directed, acyclic graph <br> - A conditional distribution for each node <br> - A collection of distributions over X, one for each combination of parents' values $P\left(X \mid a_{1} \ldots a_{n}\right)$ <br> - CPT: conditional probability table $P\left(X \mid A_{1} \ldots A_{n}\right)$ <br> - Description of a noisy "causal" process <br> A Bayes net $=$ Topology (graph) + Local Conditional Probabilities |


| Probabilities in BNS |
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| - Bayes' nets implicitly encode joint distributions |
| - As a product of local conditional distributions |
| - To see what probability a BN gives to a full assignment, multiply all the |
| relevant conditionals together: |
| $P\left(x_{1}, x_{2}, \ldots x_{n}\right)=\prod_{i=1}^{n} P\left(x_{i} \mid\right.$ parents $\left.\left(X_{i}\right)\right)$ |
| - Example: |


| Probabilities in BNs ETP |
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| - Why are we guaranteed that setting $P\left(x_{1}, x_{2}, \ldots x_{n}\right)=\prod_{i=1}^{n} P\left(x_{i} \mid \text { parents }\left(X_{i}\right)\right)$ <br> results in a proper joint distribution? <br> - Chain rule (valid for all distributions): $\quad P\left(x_{1}, x_{2}, \ldots x_{n}\right)=\prod_{i=1}^{n} P\left(x_{i} \mid x_{1} \ldots x_{i-1}\right)$ <br> - Assume conditional independences: $\quad P\left(x_{i} \mid x_{1}, \ldots x_{i-1}\right)=P\left(x_{i} \mid \operatorname{parents}\left(X_{i}\right)\right)$ <br> $\rightarrow$ Consequence: $\quad P\left(x_{1}, x_{2}, \ldots x_{n}\right)=\prod_{i=1}^{n} P\left(x_{i} \mid\right.$ parents $\left.\left(X_{i}\right)\right)$ <br> - Not every BN can represent every joint distribution <br> - The topology enforces certain conditional independencies |





