CSE 473: Artificial Intelligence Autumn 2016

Search: Cost & Heuristics

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With slides from Dan Klein, Stuart Russell, Andrew Moore, Luke Zettlemoyer

Announcements

Project 0: "Warm-up" – due today

Project 1: "Search" - due Friday 10/14 Start early!

Wed: Guest lecture on heuristics by Travis Mandel

Search thru a Problem Space / State Space

• Input:

- Set of states
- Operators [and costs]
- Start state
- Goal state [test]

• Output:

- Path: start \Rightarrow a state satisfying goal test
- [May require shortest path]
- [Sometimes just need state passing test]



DFS vs BFS						
Algorithm Complete Optimal Time Space						
DFS		N unless finite	N	$O(b^m)$	O(bm)	
BFS		Y	Y	$O(b^d)$	$O(b^d)$	
broken for the second						
Cycle checking in DFS costs exponential memory!						











Cost of Iterative Deepening					
Г	b	ratio ID to DFS			
-	2	3			
-	3	2			
	5	1.5			
	10	1.2			
	25	1.08			
-	100	1.02			
L					

Assuming 10M nodes/sec & sufficient memory					
BFS Iter. Deep. <mark>Nodes</mark> Time <mark>Nodes</mark> Time					
8 Puzzle	10 ⁵	.01 sec	10 ⁵	.01 sec	
2x2x2 Rubik's	10 ⁶	.2 sec	10 ⁶	.2 sec	
15 Puzzle	10 ¹³	6 days 1Mx	10 ¹⁷	20k yrs	
3x3x3 Rubik's	10 ¹⁹	68k yrs _{8x}	10 ²⁰	574k yrs	
24 Puzzle	10 ²⁵	12B yrs	10 ³⁷	10 ²³ yrs	
Why the difference? Rubik has higher branch factor 15 puzzle has greater depth # of duplicates					























Uniform Cost Search							
Algorithm		Complete	Optimal	Time	Space		
DFS	w/ Path Checking	Y if finite	N	$O(b^m)$	O(bm)		
BFS		Y	Y*	$O(b^d)$	$O(b^d)$		
UCS		Y*	Y	$O(b^{C^{*/\varepsilon}})$	$O(b^{C^{*/\varepsilon}})$		
C^*/ε tiers $C^* = Optimal cost$ $\varepsilon = Minimum cost of an action$							

























