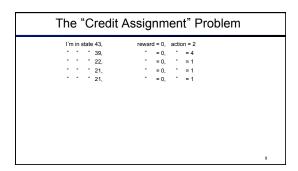


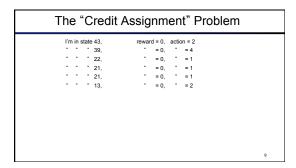
The "Credit Assignment" Problem

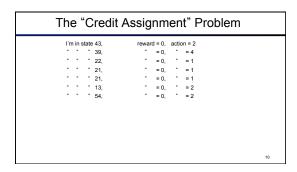
I'm in state 43, reward = 0, action = 2
- - - 39, - = 0, - = 4

The "Credit Assignment" Problem			
l'm in state 43, • • • 39, • • 22,	reward = 0, action = 2 " = 0, " = 4 " = 0, " = 1		
		6	

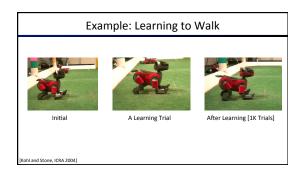
The "Credit Assignment" Problem		
I'm in state 43, 39, 22, 21,	reward = 0, action = 2 " = 0, " = 4 " = 0, " = 1 " = 0, " = 1	
		7



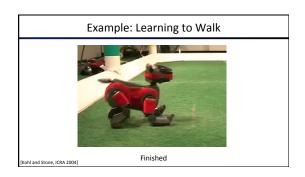


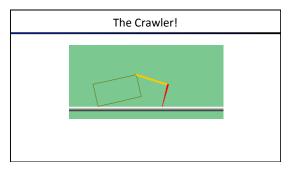


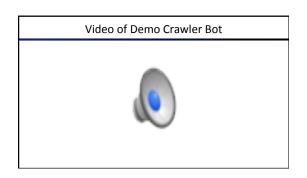
Exploration-Exploitation tradeoff You have visited part of the state space and found a reward of 100 • is this the best you can hope for??? Exploitation: should I stick with what I know and find a good policy w.r.t. this knowledge? • at risk of missing out on a better reward somewhere Exploration: should I look for states w/ more reward? • at risk of wasting time & getting some negative reward

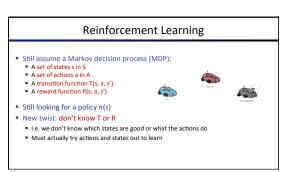


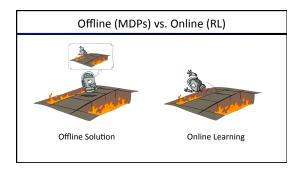


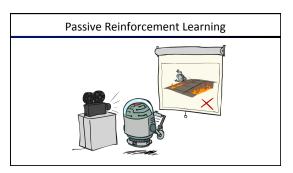


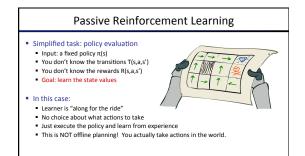


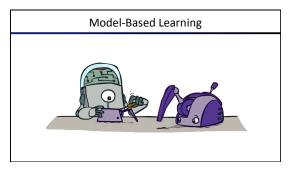


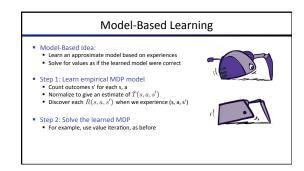


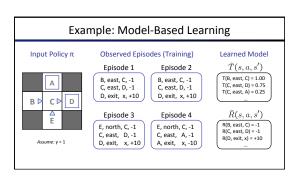


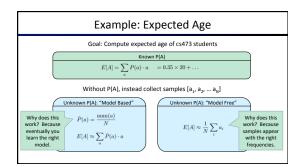


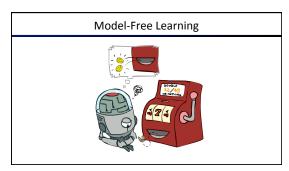








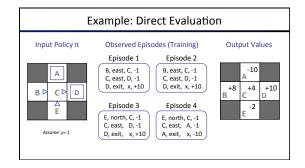




Direct Evaluation

- $\,\blacksquare\,$ Goal: Compute values for each state under π
- Idea: Average together observed sample values
 - Act according to π
 - Every time you visit a state, write down what the sum of discounted rewards turned out to be
 - Average those samples
- This is called direct evaluation





Problems with Direct Evaluation

- What's good about direct evaluation?
 - It's easy to understand
 - It doesn't require any knowledge of T, R
 - It eventually computes the correct average values, using just sample transitions
- What's bad about it?
 - It wastes information about state connections
 - Each state must be learned separately
 - So, it takes a long time to learn

Output Values



If B and E both go to C under this policy, how can their values be different?

Why Not Use Policy Evaluation?

- Simplified Bellman updates calculate V for a fixed policy:
 Each round, replace V with a one-step-look-ahead layer over V

 $V_0^{\pi}(s) = 0$ $V_{k+1}^{\pi}(s) \leftarrow \sum_{s'} T(s, \pi(s), s') [R(s, \pi(s), s') + \gamma V_k^{\pi}(s')]$



- This approach fully exploited the connections between the states
 Unfortunately, we need T and R to do it!
- Key question: how can we do this update to V without knowing T and R?
 In other words, how do we take a weighted average without knowing the weights?

Sample-Based Policy Evaluation?

- We want to improve our estimate of V by computing these averages: $\textstyle V_{k+1}^{\pi}(s) \leftarrow \sum_{t} T(s,\pi(s),s')[R(s,\pi(s),s') + \gamma V_k^{\pi}(s')]$
- Idea: Take samples of outcomes s' (by doing the action!) and average

$$\begin{split} sample_1 &= R(s,\pi(s),s_1') + \gamma V_k^\pi(s_1') \\ sample_2 &= R(s,\pi(s),s_2') + \gamma V_k^\pi(s_2') \\ &\cdots \\ sample_n &= R(s,\pi(s),s_n') + \gamma V_k^\pi(s_n') \end{split}$$





Temporal Difference Learning

- Big idea: learn from every experience!
 Update V(s) each time we experience a transition (s, a, s', r)
 Likely outcomes s' will contribute updates more often
- Temporal difference learning of values
 - Policy still fixed, still doing evaluation! Move values toward value of whatever successor occurs: running average

Sample of V(s): $sample = R(s,\pi(s),s') + \gamma V^{\pi}(s')$ Update to V(s): $V^{\pi}(s) \leftarrow (1-\alpha)V^{\pi}(s) + (\alpha)sample$

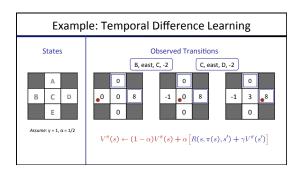
Same update: $V^{\pi}(s) \leftarrow V^{\pi}(s) + \alpha(sample - V^{\pi}(s))$

Exponential Moving Average

- Exponential moving average
 - ullet The running interpolation update: $ar{x}_n = (1-lpha) \cdot ar{x}_{n-1} + lpha \cdot x_n$
 - Makes recent samples more important:

$$\bar{x}_n = \frac{x_n + (1 - \alpha) \cdot x_{n-1} + (1 - \alpha)^2 \cdot x_{n-2} + \dots}{1 + (1 - \alpha) + (1 - \alpha)^2 + \dots}$$

- Forgets about the past (distant past values were wrong anyway)
- Decreasing learning rate (alpha) can give converging averages



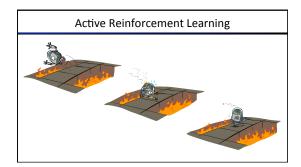
Problems with TD Value Learning

- TD value leaning is a model-free way to do policy evaluation, mimicking Bellman updates with running sample averages
- However, if we want to turn values into a (new) policy, we're sunk:

$$\begin{split} \pi(s) &= \arg\max_{a} Q(s, a) \\ Q(s, a) &= \sum_{} T(s, a, s') \left[R(s, a, s') + \gamma V(s') \right] \end{split}$$

- Idea: learn Q-values, not values
- Makes action selection model-free too!





Active Reinforcement Learning

- Full reinforcement learning: optimal policies (like value iteration)
 You don't know the transitions T(s,a,s')

 - You don't know the rewards R(s,a,s')
 - You choose the actions now
 - Goal: learn the optimal policy / values



- Learner makes choices!
- Fundamental tradeoff: exploration vs. exploitation
- This is NOT offline planning! You actually take actions in the world and find out what happens...

Detour: Q-Value Iteration

- Value iteration: find successive (depth-limited) values
 Start with V₀(s) = 0, which we know is right
 Given V_w calculate the depth k+1 values for all states:

$$V_{k+1}(s) \leftarrow \max_{a} \sum_{s'} T(s, a, s') \left[R(s, a, s') + \gamma V_k(s') \right]$$

- But Q-values are more useful, so compute them instead
 Start with Q₀(s,a) = 0, which we know is right
 Given Q_v, calculate the depth k+1 q-values for all q-states:

$$Q_{k+1}(s, a) \leftarrow \sum_{s} T(s, a, s') \left[R(s, a, s') + \gamma \max_{a'} Q_k(s', a') \right]$$

Q-Learning

Q-Learning: sample-based Q-value iteration

$$Q_{k+1}(s, a) \leftarrow \sum_{s} T(s, a, s') \left[R(s, a, s') + \gamma \max_{a'} Q_k(s', a') \right]$$

- Learn Q(s,a) values as you go
- Receive a sample (s,a,s',r)
 Consider your old estimate: Q(s,a)
- Consider your new sample estimate:

$$sample = R(s, a, s') + \gamma \max_{a'} Q(s', a')$$

• Incorporate the new estimate into a running average:

$$Q(s,a) \leftarrow (1-\alpha)Q(s,a) + (\alpha) [sample]$$



Q-Learning

- Forall s, aInitialize Q(s, a) = 0
- Repeat Forever
 Where are you? s
 Choose some action a Execute it in real world: (s, a, r, s') Do update:

$$Q(s, a) \leftarrow (1 - \alpha)Q(s, a) + (\alpha) \left[r + \gamma \max_{a'} Q(s', a') \right]$$

Video of Demo Q-Learning -- Gridworld



Video of Demo Q-Learning -- Crawler



Q-Learning Properties

- Amazing result: Q-learning converges to optimal policy even if you're acting suboptimally!
- This is called off-policy learning
- Caveats:
 - You have to explore enough
 - You have to eventually make the learning rate small enough

 - ... but not decrease it too quickly
 Basically, in the limit, it doesn't matter how you select actions (!)

Two main reinforcement learning approaches

- Model-based approaches:
- explore environment & learn model, T=P(s'|s,a) and R(s,a), (almost) everywhere
- use model to plan policy, MDP-style
- approach leads to strongest theoretical results
- often works well when state-space is manageable
- Model-free approach:
 - don't learn a model; learn value function or policy directly
 - weaker theoretical results
- often works better when state space is large

The Story So Far: MDPs and RL

Known MDP: Offline Solution

Compute V*, Q*, π*

Value / policy iteration Evaluate a fixed policy π Policy evaluation

Unknown MDP: Model-Based

Technique VI/PI on approx. MDP Compute V*, Q*, π* Evaluate a fixed policy π PE on approx. MDP

Unknown MDP: Model-Free

Compute V*, Q*, π* Q-learning Evaluate a fixed policy π Value Learning

Two main reinforcement learning approaches

■ Model-based approaches:

Learn T + R |S|²|A| + |S||A| parameters (40,400)

• Model-free approach:

Learn Q

|S||A| parameters

Video of Demo Q-Learning Auto Cliff Grid

