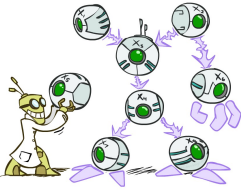


# CSE 473: Artificial Intelligence

## Bayes' Nets



Steve Tanimoto --- University of Washington

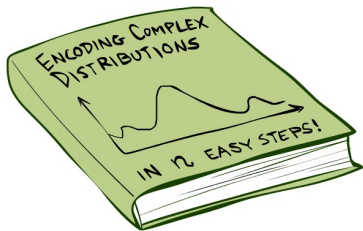
[These slides were created by Dan Klein and Pieter Abbeel for CS188 Intro to AI at UC Berkeley. All CS188 materials are available at <http://ai.berkeley.edu>.]

# Probabilistic Models

- Models describe how (a portion of) the world works
- Models are always simplifications
  - May not account for every variable
  - May not account for all interactions between variables
  - "All models are wrong; but some are useful."
    - George E. P. Box
- What do we do with probabilistic models?
  - We (or our agents) need to reason about unknown variables, given evidence
  - Example: explanation (diagnostic reasoning)
  - Example: prediction (causal reasoning)
  - Example: value of information

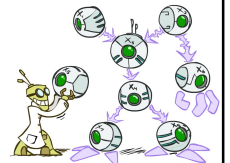


# Bayes' Nets: Big Picture

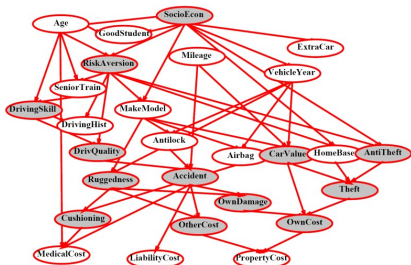


# Bayes' Nets: Big Picture

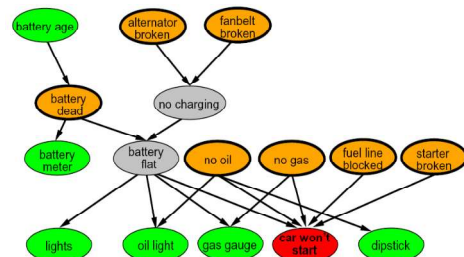
- Two problems with using full joint distribution tables as our probabilistic models:
  - Unless there are only a few variables, the joint is WAY too big to represent explicitly
  - Hard to learn (estimate) anything empirically about more than a few variables at a time
- Bayes' nets: a technique for describing complex joint distributions (models) using simple, local distributions (conditional probabilities)
  - More properly called graphical models
  - We describe how variables locally interact
  - Local interactions chain together to give global, indirect interactions
  - For about 10 min, we'll be vague about how these interactions are specified



# Example Bayes' Net: Insurance

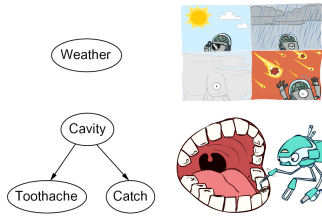


# Example Bayes' Net: Car



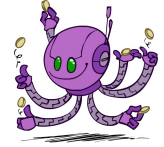
## Graphical Model Notation

- Nodes: variables (with domains)
  - Can be assigned (observed) or unassigned (unobserved)
- Arcs: interactions
  - Similar to CSP constraints
  - Indicate "direct influence" between variables
  - Formally: encode conditional independence (more later)
- For now: imagine that arrows mean direct causation (in general, they don't!)



## Example: Coin Flips

- N independent coin flips



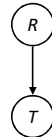
- No interactions between variables: absolute independence

## Example: Traffic

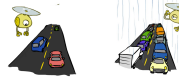
- Variables:
  - R: It rains
  - T: There is traffic
- Model 1: independence



- Model 2: rain causes traffic



- Why is an agent using model 2 better?



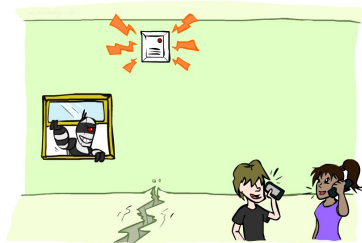
## Example: Traffic II

- Let's build a causal graphical model!
- Variables:
  - T: Traffic
  - R: It rains
  - L: Low pressure
  - D: Roof drips
  - B: Ballgame
  - C: Cavity



## Example: Alarm Network

- Variables:
  - B: Burglary
  - A: Alarm goes off
  - M: Mary calls
  - J: John calls
  - E: Earthquake!

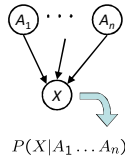


## Bayes' Net Semantics



## Bayes' Net Semantics

- A set of nodes, one per variable  $X$
- A directed, acyclic graph
- A conditional distribution for each node
  - A collection of distributions over  $X$ , one for each combination of parents' values



$$P(X|a_1 \dots a_n)$$

$$P(X|A_1 \dots A_n)$$

A Bayes net = Topology (graph) + Local Conditional Probabilities

## Probabilities in BNs

- Bayes' nets **implicitly** encode joint distributions
  - As a product of local conditional distributions
  - To see what probability a BN gives to a full assignment, multiply all the relevant conditionals together:

$$P(x_1, x_2, \dots, x_n) = \prod_{i=1}^n P(x_i | \text{parents}(X_i))$$

Example:



$$P(+cavity, +catch, -toothache)$$

## Probabilities in BNs

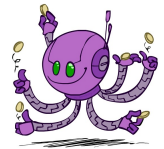
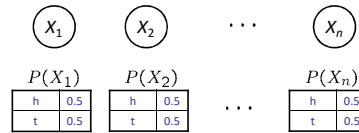
- Why are we guaranteed that setting

$$P(x_1, x_2, \dots, x_n) = \prod_{i=1}^n P(x_i | \text{parents}(X_i))$$

results in a proper joint distribution?

- Chain rule (valid for all distributions):  $P(x_1, x_2, \dots, x_n) = \prod_{i=1}^n P(x_i | x_1 \dots x_{i-1})$
- Assume conditional independences:  $P(x_i | x_1 \dots x_{i-1}) = P(x_i | \text{parents}(X_i))$ 
  - Consequence:  $P(x_1, x_2, \dots, x_n) = \prod_{i=1}^n P(x_i | \text{parents}(X_i))$
- Not every BN can represent every joint distribution
  - The topology enforces certain conditional independencies

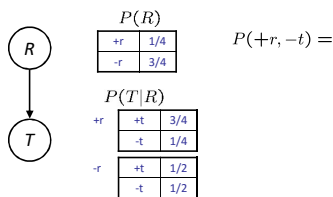
## Example: Coin Flips



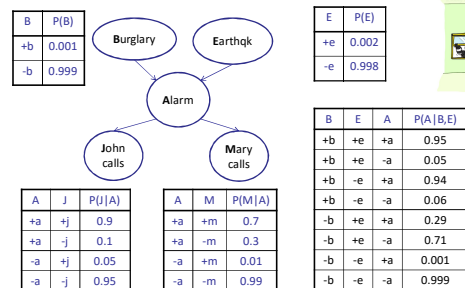
$$P(h, h, t, h) =$$

Only distributions whose variables are absolutely independent can be represented by a Bayes' net with no arcs.

## Example: Traffic

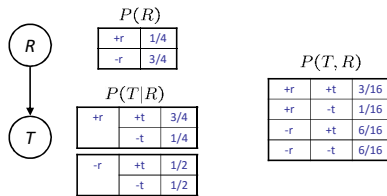


## Example: Alarm Network



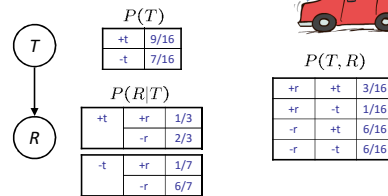
## Example: Traffic

### Causal direction



## Example: Reverse Traffic

### Reverse causality?



## Causality?

### When Bayes' nets reflect the true causal patterns:

- Often simpler (nodes have fewer parents)
- Often easier to think about
- Often easier to elicit from experts

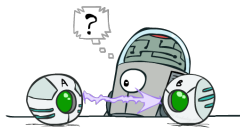
### BNs need not actually be causal

- Sometimes no causal net exists over the domain (especially if variables are missing)
- E.g. consider the variables *Traffic* and *Drips*
- End up with arrows that reflect correlation, not causation

### What do the arrows really mean?

- Topology may happen to encode causal structure
- Topology really encodes conditional independence

$$P(x_i|x_1, \dots, x_{i-1}) = P(x_i|\text{parents}(X_i))$$



## Bayes' Nets

### So far: how a Bayes' net encodes a joint distribution

### Next: how to answer queries about that distribution

- Today:
  - First assembled BNs using an intuitive notion of conditional independence as causality
  - Then saw that key property is conditional independence
- Main goal: answer queries about conditional independence and influence
- After that: how to answer numerical queries (inference)

