

| Representation: Particles |  |
| :---: | :---: |
| - Our representation of $P(X)$ is now a list of $N$ particles (samples) <br> - Generally, N << $\|\mathrm{X}\|$ <br> - Storing map from X to counts would defeat the point <br> - $P(x)$ approximated by number of particles with value $x$ <br> - So, many $x$ may have $P(x)=0$ ! <br> - More particles, more accuracy <br> - For now, all particles have a weight of 1 |  $\ddots$ $\ddots$ <br> -  $\vdots$ <br>    <br> Particles: $(3,3)$ $(2,3)$ $(3,3)$ $(3,2)$ $(3,3)$ $(3,2)$ $(1,2)$ $(3,3)$ $(3,3)$ $(2,3)$ |


| Particle Filtering: Elapse Time |  |  |  |
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| - Each particle is moved by sampling its next position from the transition model $x^{\prime}=\operatorname{sample}\left(P\left(X^{\prime} \mid x\right)\right)$ <br> - This is like prior sampling - samples' frequencies reflect the transition probabilities <br> - Here, most samples move clockwise, but some move in another direction or stay in place <br> - This captures the passage of time <br> - If enough samples, close to exact values before and after (consistent) |  |  |  |


| Particle Filtering: Observe |  |  |  |  |
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| - Slightly trickier: <br> - Don't sample observation, fix it <br> - Similar to likelihood weighting, downweight samples based on the evidence $\begin{aligned} w(x) & =P(e \mid x) \\ B(X) & \propto P(e \mid X) B^{\prime}(X) \end{aligned}$ <br> - As before, the probabilities don't sum to one, since all have been downweighted (in fact they now sum to ( N times) an approximation of $\mathrm{P}(\mathrm{e})$ ) |  |  |  | $:$ <br> 0 <br> $\bullet$ <br> 0 <br> $\vdots$ <br> 0 <br> 0 |


| Particle Filtering: Resample |  |  |
| :---: | :---: | :---: |
| - Rather than tracking weighted samples, we resample <br> - $N$ times, we choose from our weighted sample distribution (i.e. draw with replacement) <br> - This is equivalent to renormalizing the distribution <br> - Now the update is complete for this time step, continue with the next one | Particles <br> (3,2) w <br> $(2,3) W=.2$ $(3,2) w=.9$ <br> $(3,3) w=.4$ <br> $(3,2) w=.9$ $(1,3) w=1$ <br> $(2,3) w=.2$ <br> $(2,2) w=-4$ <br> $\left(\begin{array}{ll}(N e w) \\ (3,2) \\ (2,2) \\ (3,2) \\ (2,2) \\ (2,3) \\ (3,3) \\ (1,2) \\ (1,3) \\ (2,3) \\ (3,2) \\ (3,2)\end{array}\right.$ |  |



## DBN Particle Filters

- A particle is a complete sample for a time step
- Initialize: Generate prior samples for the $t=1$ Bayes net - Example particle: $\mathbf{G}_{1}{ }^{a}=(3,3) G_{1}{ }^{b}=(5,3)$
- Elapse time: Sample a successor for each particle - Example successor: $\mathbf{G}_{\mathbf{2}}{ }^{\mathbf{a}}=(2,3) \mathbf{G}_{\mathbf{2}}{ }^{\mathbf{b}}=(6,3)$
- Observe: Weight each entire sample by the likelihood of the evidence conditioned on the sample
- Likelihood: $P\left(E_{1}{ }^{a} \mid G_{1}{ }^{a}\right)^{*} P\left(E_{1}{ }^{b} \mid G_{1}{ }^{b}\right)$
- Resample: Select prior samples (tuples of values) in proportion to their likelihood

