

CSE 473
Automated Planning

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(With slides by UW AI faculty & Dana Nau)

I have a plan - a plan that cannot possibly fail.

- Inspector Clousseau



Popular Application



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Overview

- Introduction & Agents
- Search, Heuristics & CSPs
- Adversarial Search
- **Logical Knowledge Representation**
- **Planning** & MDPs
- Reinforcement Learning
- Uncertainty & Bayesian Networks
- Machine Learning
- NLP & Special Topics

Planning & Logic

- Actions specified using first-order logic
- Planning implemented using SAT solver
 - E.g., DPLL or WalkSAT
- Also an example of solving FOL using propositional SAT

Logistics

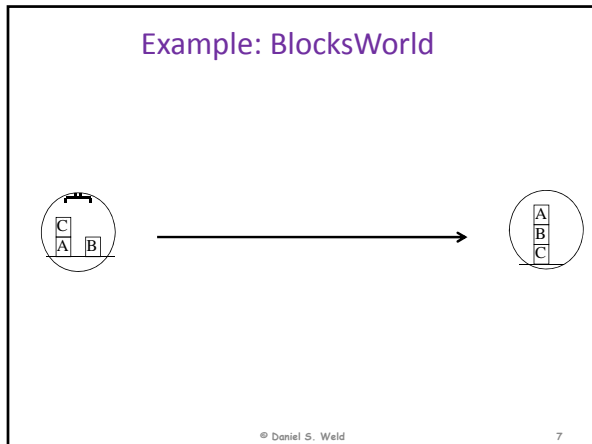
- PS2 due today
- HW1 due in one week
 - Parts due in between:
 - Friday written problem
 - Monday feedback on another person's answer
 - Wed revise your answer

Planning

- Given
 - a logical description of the **initial situation**,
 - a logical description of the **goal conditions**, and
 - a logical description of a set of **possible actions**,
- Find
 - a **sequence of actions** (a **plan of actions**) that brings us from the initial situation to a situation in which the goal conditions hold.

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- ### Planning Input: State Variables/Propositions
- Types: block --- a, b, c
 - (on-table a) (on-table b) (on-table c) *on-table(a)*
 - (clear a) (clear b) (clear c)
 - (arm-empty)
 - (holding a) (holding b) (holding c)
 - (on a b) (on a c) (on b a) (on b c) (on c a) (on c b)
- No. of state variables = 16
 No. of states = 2^{16}
 No. of reachable states = ?
- (on-table ?b); clear (?b)
 - (arm-empty); holding (?b)
 - (on ?b1 ?b2)
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- ### Planning Input: Actions
- pickup a b, pickup a c, ...
 - place a b, place a c, ...
 - pickup-table a, pickup-table b, ...
 - place-table a, place-table b, ...
 - pickup ?b1 ?b2
 - place ?b1 ?b2
 - pickup-table ?b
 - place-table ?b
- Total: $6 + 6 + 3 + 3 = 18$ "ground" actions
 Total: 4 action schemata
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- ### Planning Input: Actions (contd)
- :action pickup ?b1 ?b2**
 - :precondition**
 - (on ?b1 ?b2)
 - (clear ?b1)
 - (arm-empty)
 - :effect**
 - (holding ?b1)
 - (not (on ?b1 ?b2))
 - (clear ?b2)
 - (not (arm-empty))
 - :action pickup-table ?b**
 - :precondition**
 - (on-table ?b)
 - (clear ?b)
 - (arm-empty)
 - :effect**
 - (holding ?b)
 - (not (on-table ?b))
 - (not (arm-empty))
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- ### Planning Input: Initial State
-
- (on-table a) (on-table b)
 - (arm-empty)
 - (clear c) (clear b)
 - (on c a)
 - All other propositions false
 - not mentioned → assumed false
 - "Closed world assumption"
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- ### Planning Input: Goal
-
- (on-table c) AND (on b c) AND (on a b)
 - Is this a state?
 - In planning a goal is a *set of states*
 - Like the goal test in problem solving search
 - But specified declaratively (in logic) rather than with code
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Planning vs. Problem-Solving ?

Basic difference: **Explicit, logic-based representation**

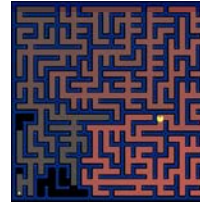
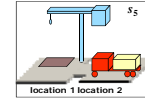
- **States/Situations:** descriptions of the world by logical formulae
→ agent can explicitly reason about the world.
- **Goal conditions** as logical formulae vs. goal test (black box)
→ agent can reflect on its goals.
- **Operators/Actions:** Transformations on logical formulae
→ agent can reason about the effects of actions
by inspecting the definition of its operators.

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One Planner Solves Many Domains

“no code required”



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Specifying a Planning Problem

- **Description of initial state of world**
 - Set of propositions
- **Description of goal:**
 - E.g., Logical conjunction
 - Any world satisfying conjunction is a goal
- **Description of available actions**

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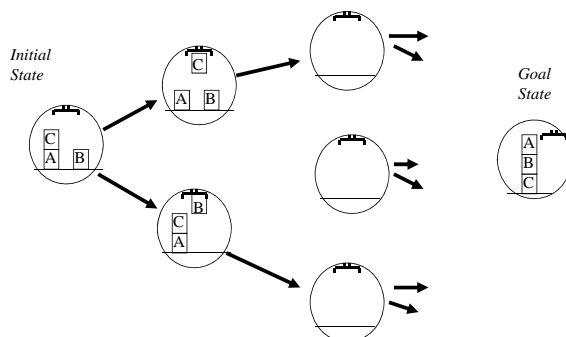
Classical Planning

- **Simplifying assumptions**
 - Atomic time
 - Agent is omniscient (no sensing necessary).
 - Agent is sole cause of change
 - Actions have deterministic effects
- **STRIPS representation**
 - World = set of true propositions (conjunction)
 - Actions:
 - Precondition: (conjunction of *positive* literals, no functions)
 - Effects (conjunction of literals, no functions)
 - Goal = conjunction of *positive* literals
 $on(A,B) \wedge on(B,C)$

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Forward World-Space Search



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Forward State-Space Search

- **Initial state:** set of positive ground literals
 - CWA: literals not appearing are false
- **Actions:**
 - applicable if preconditions satisfied
 - add positive effect literals
 - remove negative effect literals
- **Goal test:** does state logically satisfy goal?
- **Step cost:** typically 1

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Heuristics for State-Space Search

- Count number of false goal propositions in current state
 - Admissible?
 - NO
- Subgoal independence assumption:
 - Cost of solving conjunction is sum of cost of solving each subgoal independently
 - Optimistic: ignores negative interactions
 - Pessimistic: ignores redundancy
 - Admissible? No
 - Can you make this admissible?

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Heuristics for State Space Search (contd)

- Delete all preconditions from actions, solve easy relaxed problem, use length

Admissible?

YES

- action pickup-table ?b
 - precondition (and (on-table ?b) (clear ?b) (arm-empty))
 - effect (and (holding ?b) ~~(not (on-table ?b))~~ ~~(not (arm-empty)))~~)

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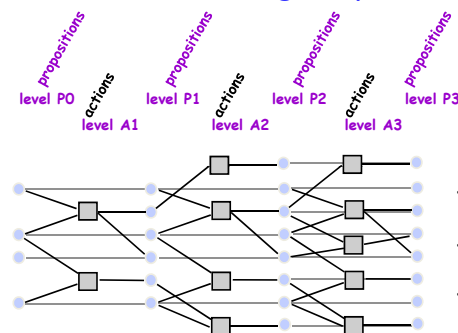
Planning Graph: Basic idea

- Construct a planning graph: encodes constraints on possible plans
- Use this planning graph to compute an informative heuristic (Forward A*)
- Planning graph can be built for each problem in polynomial time

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The Planning Graph



Note: a few noops missing for clarity

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Regression search

- States
- Operators
- Initial State
- Goal

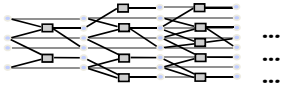
Planning Graphs

- Planning graphs consists of a seq of levels that correspond to time steps in the plan.
 - Level 0 is the initial state.
 - Each level consists of a set of literals and a set of actions that represent what *might be* possible at that step in the plan
 - Might be* is the key to efficiency
 - Records only a restricted subset of possible negative interactions among actions.

Planning Graphs

- **Alternate levels**

- *Literals* = all those that *could* be true at that time step, depending upon the actions executed at preceding time steps.
- *Actions* = all those actions that *could* have their preconditions satisfied at that time step, depending on which of the literals actually hold.



PG Example

Init(Have(Cake))
Goal(Have(Cake) \wedge Eaten(Cake))
Action(Eat(Cake),
 PRECOND: Have(Cake)
 EFFECT: \neg Have(Cake) \wedge Eaten(Cake))
Action(Bake(Cake),
 PRECOND: \neg Have(Cake)
 EFFECT: Have(Cake))

PG Example

S_0 A_0 S_1
 Have(Cake)

 \neg Eaten(Cake)

 Create level 0 from initial problem state.

Graph Expansion

Proposition level 0
 initial conditions
Action level i
 no-op for each proposition at level i-1
 action for each operator instance whose preconditions exist at level i-1
Proposition level i
 effects of each no-op and action at level i

No-op-action(P),
 PRECOND: P
 EFFECT: P
 Have a no-op action for each ground fact

PG Example

S_0 A_0 S_1
 Have(Cake) Eat(Cake) \neg Have(Cake)

 \neg Eaten(Cake) Eaten(Cake)

Add all applicable actions.
 Add all effects to the next state.

PG Example

S_0 A_0 S_1
 Have(Cake) Eat(Cake) Have(Cake)

 \neg Eaten(Cake) Eaten(Cake) \neg Eaten(Cake)

Add *persistence actions* (aka no-ops) to map all literals in state S_i to state S_{i+1} .

Mutual Exclusion

Two actions are mutex if

- one clobbers the other's effects or preconditions
- they have mutex preconditions

Two proposition are mutex if

- one is the negation of the other
- all ways of achieving them are mutex

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PG Example

Identify *mutual exclusions* between actions and literals based on potential conflicts.

Cake example

- Level S_1 contains all literals that might result from picking any subset of actions in A_0
 - Conflicts between literals that can not occur together (as a consequence of the selection action) are represented by mutex links.
 - S_1 defines multiple states and the mutex links are the constraints that define this set of states.

Cake example

Observation 1

Propositions monotonically increase
(always carried forward by no-ops)

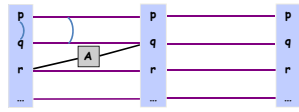
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Observation 2

Actions monotonically increase

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Observation 3

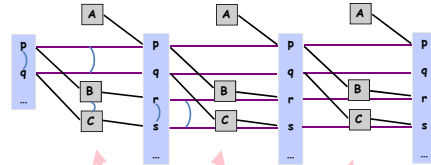


Proposition mutex relationships monotonically decrease

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Observation 4



Action mutex relationships monotonically decrease

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Observation 5

Planning Graph 'levels off'.

- After some time k all levels are identical
- Because it's a finite space, the set of literals never decreases and mutexes don't reappear.

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Properties of Planning Graph

- If goal is absent from last level?
 - Then goal cannot be achieved!
- If there exists a plan to achieve goal?
 - Then goal is present in the last level &
 - No mutexes between conjuncts
- If goal is present in last level (w/ no mutexes) ?
 - There still may not exist any viable plan

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Heuristics based on Planning Graph

- Construct planning graph starting from s
- $h(s)$ = level at which goal appears non-mutex
 - Admissible?
 - YES
- Relaxed Planning Graph Heuristic
 - Remove negative preconditions build plan. graph
 - Use heuristic as above
 - Admissible? YES
 - More informative? NO
 - Speed: FASTER

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FF

- Topmost classical planner until 2009
- State space local search
 - Guided by relaxed planning graph
 - Full best-first search to escape plateaus
 - A few other bells and whistles...

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Planning Summary

- Problem solving algorithms that operate on explicit propositional representations of states and actions.
- Make use of domain-independent **heuristics**.
- **STRIPS**: restrictive propositional language
- **Heuristic search**
 - forward (progression)
 - backward (regression) search [didn't cover]
- **Local search** FF [didn't cover]

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Generative Planning

Input

- Description of (initial state of) world (*in some KR*)
- Description of goal (*in some KR*)
- Description of available actions (*in some KR*)

Output

Controller

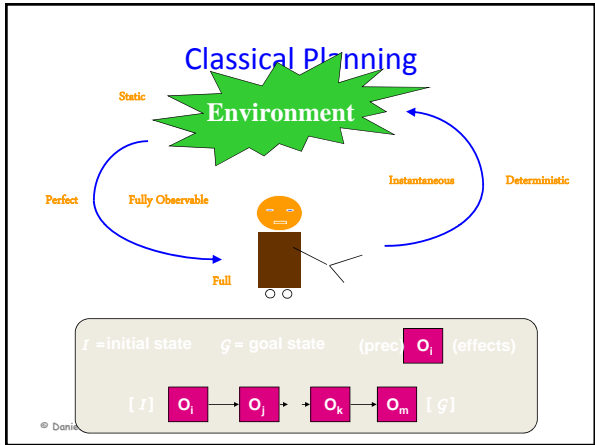
- E.g. Sequence of actions
- E.g. Plan with loops and conditionals
- E.g. Policy = $f: \text{states} \rightarrow \text{actions}$

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Input Representation

- **Description of initial state of world**
 - E.g., Set of propositions:
 - ((**block a**) (**block b**) (**block c**) (**on-table a**) (**on-table b**) (**clear a**) (**clear b**) (**clear c**) (**arm-empty**))
- **Description of goal: i.e. set of worlds or ??**
 - E.g., Logical conjunction
 - Any world satisfying conjunction is a goal
 - (**and (on a b) (on b c)**)
- **Description of available actions**

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Compilation to SAT

- Init state
- Actions
- Goal

→ ?

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The Idea

- Suppose a plan of length n exists
- Encode this hypothesis in SAT
 - Init state true at t_0
 - Goal true at T_n
 - Actions imply effects, etc
- Look for **satisfying** assignment
- Decode into plan

RISC: The Revolutionary Excitement

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Axioms

Axiom	Description / Example
Init	The initial state holds at $t=0$
Goal	The goal holds at $t=2n$
$A \Rightarrow P, E$	$\text{Paint}(A, \text{Red}, t) \Rightarrow \text{Block}(A, t-1)$ $\text{Paint}(A, \text{Red}, t) \Rightarrow \text{Color}(A, \text{Red}, t+1)$
Frame	
At-least-one	
Exclude	

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Space of Encodings

- Action Representations
 - Regular
 - Simply-Split
 - Overloaded-Split
 - Bitwise
- Frame Axioms
 - Classical
 - Explanatory

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Frame Axioms

- Classical
 - $\forall P, A, t$ if $P@t-1 \wedge$
 - $A@t \wedge$
 - A doesn't affect P
 - then $P@t+1$
- Explanatory

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Action Representation

Representation	One Propositional Variable per	Example	more vars
Regular	fully-instantiated action	$\text{Paint-A-Red}, \text{Paint-A-Blue}, \text{Move-A-Table}$	↑ ↓ more clauses
Simply-split	fully-instantiated action's argument	$\text{Paint-Arg1-A} \wedge \text{Paint-Arg2-Red}$	
Overloaded-split	fully-instantiated argument	$\text{Act-Paint} \wedge \text{Arg1-A} \wedge \text{Arg2-Red}$	
Bitwise	Binary encodings of actions	$\text{Bit1} \wedge \sim \text{Bit2} \wedge \text{Bit3}$	

$\text{Paint-A-Red} = 5$

more clauses

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Optimization 1: Factored Splitting

- use partially-instantiated actions
- $\text{HasColor-A-Blue-(t-1)} \wedge \text{Paint-Arg1-B-t} \wedge$
 $\text{Paint-Arg2-Red-t} \Rightarrow \text{HasColor-A-Blue-(t+1)}$

factored unfactored	Explanatory Frames	
	Simple	Overloaded
Variables	.46	.69
Clauses	.30	.50
Literals	.20	.38

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Optimization 2: Types

- A *type* is a fluent which no actions affects.
- type interference
 - prune impossible operator instantiations
 - type elimination

Type opts
No type opts

Literals	Regular	Simple	Overloaded	Bitwise
Classical	.27	.39	.34	.30
Explanatory	.10	.97	.67	.74

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