## CSE 473: Artificial Intelligence Spring 2012

Reasoning about Uncertainty &

#### Hidden Markov Models

Daniel Weld

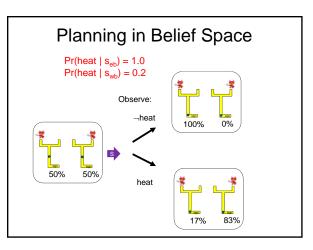
Many slides adapted from Dan Klein, Stuart Russell, Andrew Moore & Luke Zettlemoyer

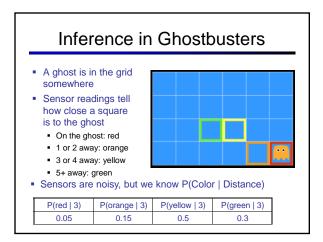
### Outline

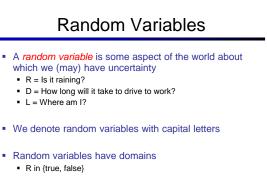
- Probability review
  - Random Variables and Events
  - Joint / Marginal / Conditional Distributions
  - Product Rule, Chain Rule, Bayes' Rule
  - Probabilistic Inference
- Probabilistic sequence models (and inference)
  - Markov Chains
  - Hidden Markov Models
  - Particle Filters

# Probability Review

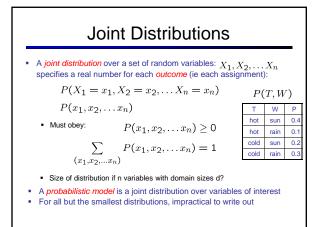
- Probability
  - Random Variables
  - Joint and Marginal Distributions
  - Conditional Distribution
  - Product Rule, Chain Rule, Bayes' Rule
  - Inference
- You'll need all this stuff A LOT for the next few weeks, so make sure you go over it now!

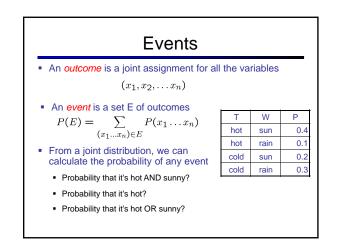


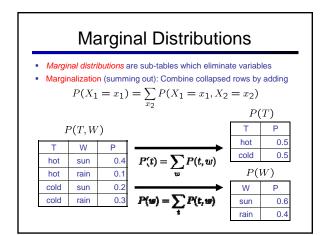


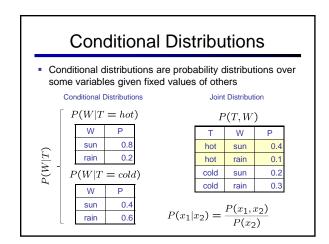


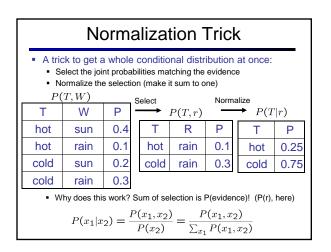
- D in [0, 1)
- L in possible locations, maybe {(0,0), (0,1), ...}

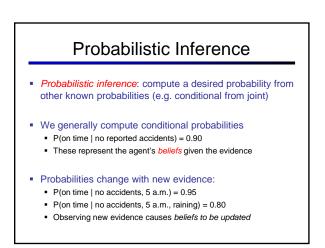










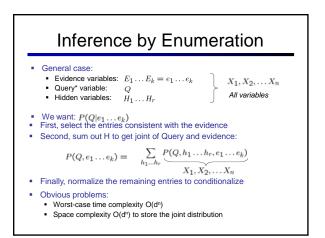


Infere	nce by Enu	mera	ation	
P(sun)?	S	т	W	Р
	summer	hot	sun	0.30
	summer	hot	rain	0.05
	summer	cold	sun	0.10
	summer	cold	rain	0.05
	winter	hot	sun	0.10
	winter	hot	rain	0.05
	winter	cold	sun	0.15
	winter	cold	rain	0.20

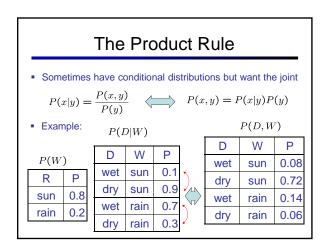
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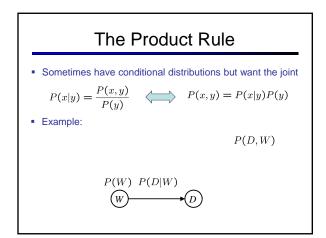
Inference	by Enu	mera	ation	1
· ·	S	Т	W	Р
	summer	hot	sun	0.30
P(sun   winter)?	summer	hot	rain	0.05
	summer	cold	sun	0.10
	summer	cold	rain	0.05
	winter	hot	sun	0.10
	winter	hot	rain	0.05
	winter	cold	sun	0.15
	winter	cold	rain	0.20
	-			

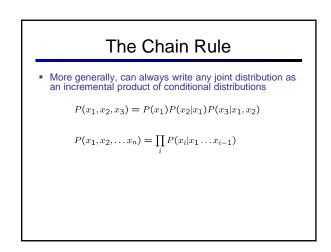
Inference by Enumeration				
÷	S	т	W	Р
	summer	hot	sun	0.30
	summer	hot	rain	0.05
	summer	cold	sun	0.10
P(sun   winter, hot)?	summer	cold	rain	0.05
	winter	hot	sun	0.10
	winter	hot	rain	0.05
	winter	cold	sun	0.15
	winter	cold	rain	0.20
	-			

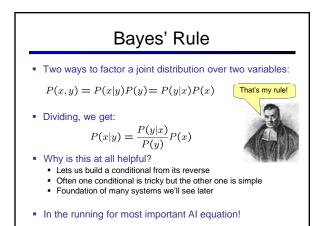


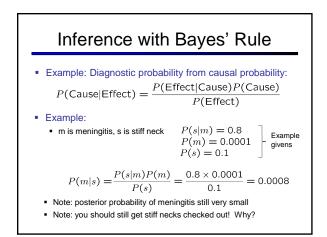
Supremacy of the Joint Distribution				
P(sun)?	S	т	W	Р
	summer	hot	sun	0.30
P(sun   winter)?	summer	hot	rain	0.05
	summer	cold	sun	0.10
	summer	cold	rain	0.05
	winter	hot	sun	0.10
P(sun   winter, hot)?	winter	hot	rain	0.05
	winter	cold	sun	0.15
	winter	cold	rain	0.20

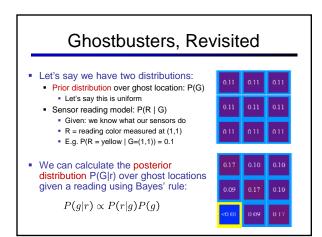


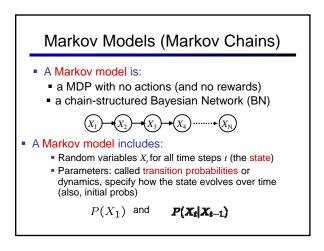












#### Markov Models (Markov Chains)

$$(X_1) \rightarrow (X_2) \rightarrow (X_3) \rightarrow (X_4) \cdots \rightarrow (X_N)$$

A Markov model defines
 a joint probability distribution:

$$P(X_1,\ldots,X_n)=P(X_1)\prod_{t=0}^N P(X_t|X_{t-1})$$

One common inference problem:
Compute marginals P(X<sub>t</sub>) for all time steps t

