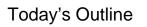
#### CSE 473: Artificial Intelligence Spring 2012

#### **Reinforcement Learning**

Dan Weld

Many slides adapted from either Dan Klein, Stuart Russell, Luke Zettlemoyer or Andrew Moore



- Reinforcement Learning
  - Passive Learning
  - TD Updates
  - Q-value iteration
  - Q-learning
  - Linear function approximation

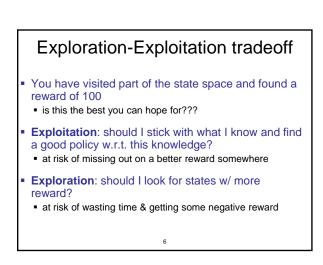


- Still have an MDP
  - Still looking for policy π
- New twist: don't know T or R
  - Don't know what actions do
  - Nor which states are good!
- Must actually try out actions to learn

#### Formalizing the reinforcement learning problem

- Given a set of states S and actions A
- Interact with world at each time step t.
- $\hfill \hfill \hfill$
- you give next action a<sub>t</sub>
- Goal: (quickly) learn policy that (approximately) maximizes long-term expected discounted reward

The "	'C	re	dit	Ass	ignr	ne	nt"	Problem
I'm in state 43,			rewa	reward = 0, action = $2$				
"	"	"	39,	"	= 0,	"	= 4	
"	"	"	22,	"	= 0,	"	= 1	
"	"	"	21,	"	= 0,	"	= 1	
"	"	"	21,	"	= 0,	"	= 1	
"	"	"	13,	"	= 0,	"	= 2	
"	"	"	54,	"	= 0,	"	= 2	
"	"	"	26,	"	= <b>100</b> ,			
Yippee! I got to a state with a big reward! But which of my actions along the way actually helped me get there?? This is the Credit Assignment problem.								



## Two main reinforcement learning approaches

#### Model-based approaches:

- explore environment & learn model, T=P(s' |s,a) and R(s,a), (almost) everywhere
- use model to plan policy, MDP-style
- approach leads to strongest theoretical results
- often works well when state-space is manageable

#### Model-free approach:

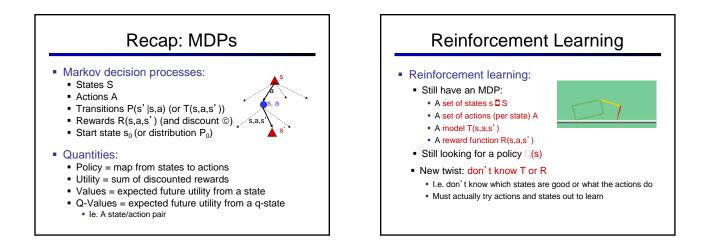
- don't learn a model; learn value function or policy directly
- weaker theoretical results
- often works better when state space is large

#### Passive vs. Active learning

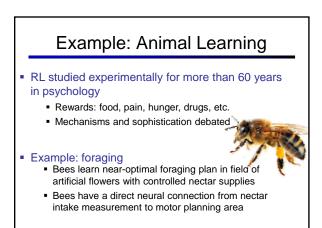
- Passive learning
  - The agent has a *fixed policy*
  - Tries to learn utilities of states by observing world go by
  - Analogous to policy evaluation
    - Often serves as a component of active learning algorithms
    - Often inspires active learning algorithms

#### Active learning

- Agent tries to find a good policy by acting in the world
- Analogous to solving the underlying MDP
  - But without first being given the MDP model

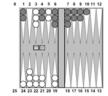


What is it doing?							
QuickTime™ and a H.24 decompressor are needed to see this picture.							



## Example: Backgammon

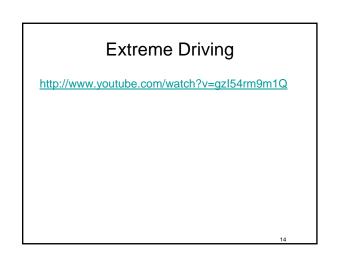
- Reward only for win / loss in terminal states, zero otherwise
- TD-Gammon learns a function approximation to V(s) using a neural network
  Combined with depth 3



• You could imagine training Pacman this way...

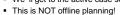
search, one of the top 3 players in the world

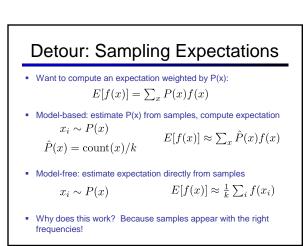
... but it's tricky! (It's also P3)

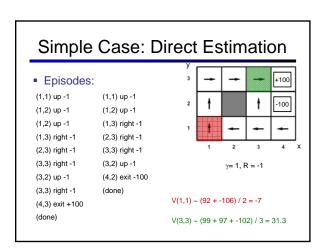




War planning, evacuation planning



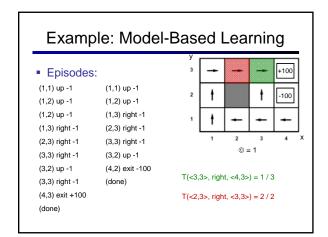


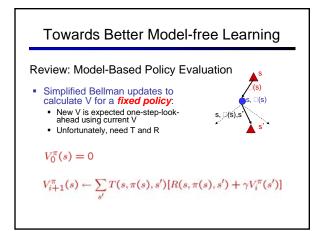


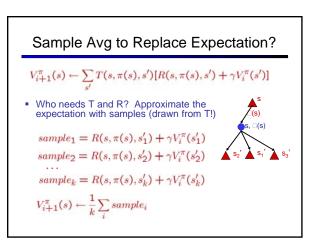
#### Model-Based Learning

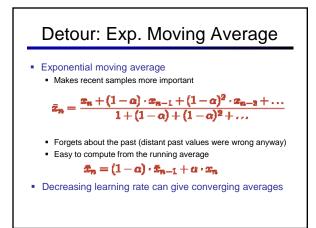
Idea:

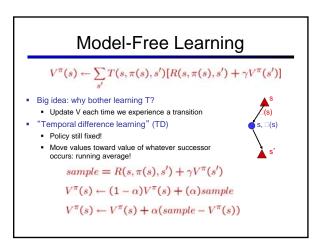
- Learn the model empirically (rather than values)
- Solve the MDP as if the learned model were correct
- Better than direct estimation?
- Empirical model learning
  - Simplest case:
    - Count outcomes for each s,a
    - Normalize to give estimate of T(s,a,s')
    - Discover R(s,a,s') the first time we experience (s,a,s')
  - More complex learners are possible (e.g. if we know that all squares have related action outcomes, e.g. "stationary noise")

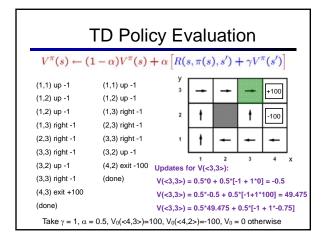


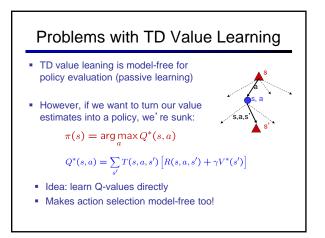


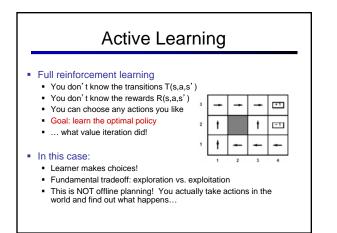


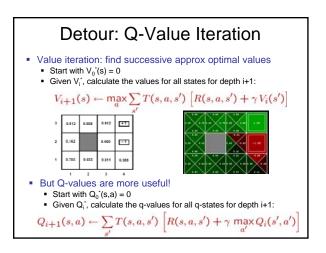


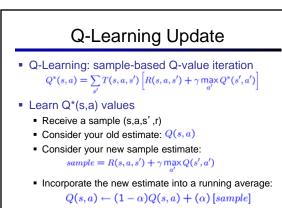


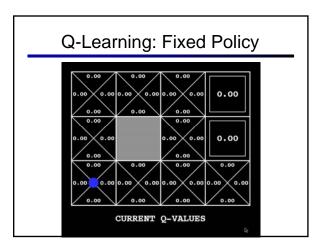






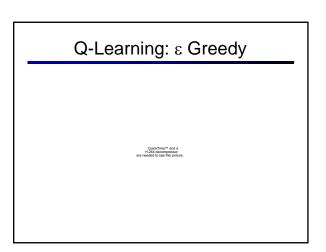


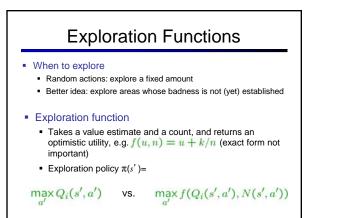


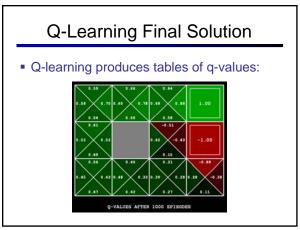


#### Exploration / Exploitation

- Several schemes for action selection
  - Simplest: random actions (*ε greedy*)
    Every time step, flip a coin
    - With probability  $\epsilon$  , act randomly
    - With probability 1- ε, act according to current policy
  - Problems with random actions?
    - You do explore the space, but keep thrashing
    - around once learning is done One solution: lower ε over time
    - Another solution: exploration functions







## **Q-Learning Properties**

- Amazing result: Q-learning converges to optimal policy
  - If you explore enough
  - If you make the learning rate small enough
  - ... but not decrease it too quickly!
  - Not too sensitive to how you select actions (!)

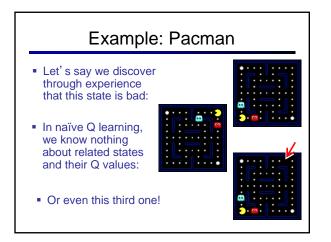
#### Neat property: off-policy learning

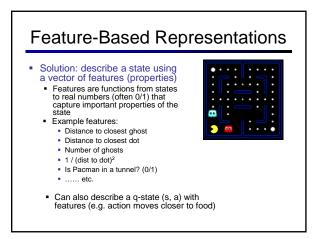
learn optimal policy without following it (some caveats)



## Q-Learning

- In realistic situations, we cannot possibly learn about every single state!
  - Too many states to visit them all in training
  - Too many states to hold the q-tables in memory
- Instead, we want to generalize:
  - Learn about some small number of training states from experience
  - Generalize that experience to new, similar states
  - This is a fundamental idea in machine learning, and we'll see it over and over again

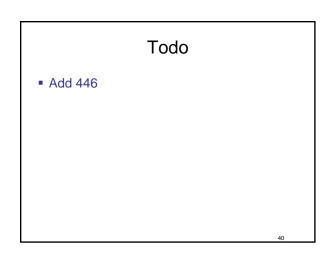


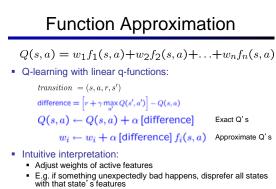


# • Using a feature representation, we can write a q function (or value function) for any state using a linear combination of a few weights: $V(s) = w_1 f_1(s) + w_2 f_2(s) + \ldots + w_n f_n(s)$

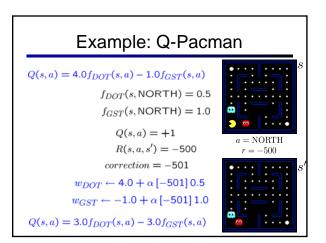
 $Q(s,a) = w_1 f_1(s,a) + w_2 f_2(s,a) + \ldots + w_n f_n(s,a)$ 

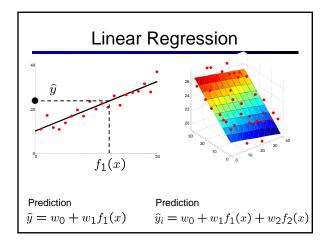
- Advantage: our experience is summed up in a few powerful numbers
- Disadvantage: states may share features but actually be very different in value!

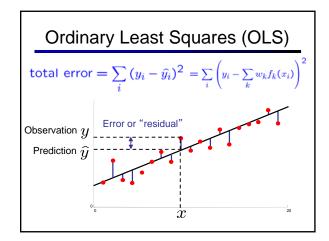


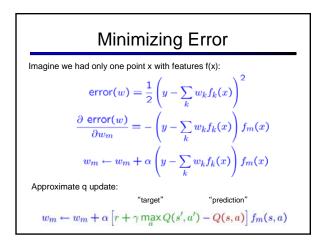


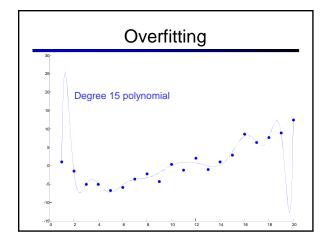
Formal justification: online least squares

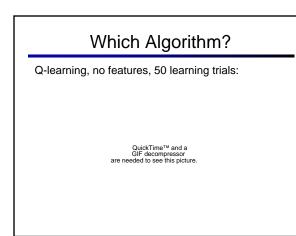


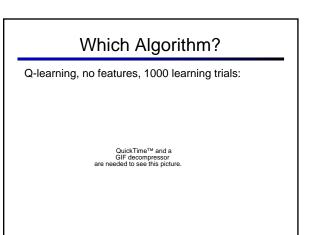








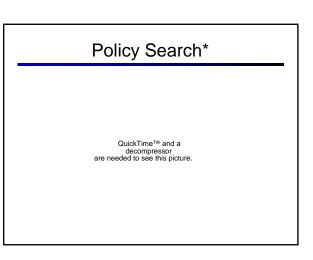




#### Which Algorithm?

Q-learning, simple features, 50 learning trials:

QuickTime™ and a GIF decompressor are needed to see this picture



## Policy Search\*

- Problem: often the feature-based policies that work well aren't the ones that approximate V / Q best
  - E.g. your value functions from project 2 were probably horrible estimates of future rewards, but they still produced good decisions
  - We'll see this distinction between modeling and prediction again later in the course
- Solution: learn the policy that maximizes rewards rather than the value that predicts rewards
- This is the idea behind policy search, such as what controlled the upside-down helicopter

## Policy Search\*

- Simplest policy search:
  - Start with an initial linear value function or q-function
  - Nudge each feature weight up and down and see if your policy is better than before

#### Problems:

- How do we tell the policy got better?
- Need to run many sample episodes!
- If there are a lot of features, this can be impractical

## Policy Search\*

- Advanced policy search:
  - Write a stochastic (soft) policy:

 $\pi_w(s) \propto e^{\sum_i w_i f_i(s,a)}$ 

- Turns out you can efficiently approximate the derivative of the returns with respect to the parameters w (details in the book, optional material)
- Take uphill steps, recalculate derivatives, etc.