CSE 473: Artificial Intelligence Spring 2012

$\begin{array}{c} \mbox{Adversarial Search: } \alpha\mbox{-}\beta\mbox{ Pruning} \\ \mbox{Dan Weld} \end{array}$

Based on slides from Dan Klein, Stuart Russell, Andrew Moore and Luke Zettlemoyer

Space of Search Strategies

- Blind Search
- DFS, BFS, IDS
- Informed Search
 - Systematic: Uniform cost, greedy, A*, IDA*
 - Stochastic: Hill climbing w/ random walk & restarts
- Constraint Satisfaction
- Backtracking=DFS, FC, k-consistency, exploiting structure
- **Adversary Search**
- Mini-max
- Alpha-beta
- Evaluation functions
- Expecti-max













































Alpha-Beta Pruning Properties

- This pruning has no effect on final result at the root
- Values of intermediate nodes might be wrong!
 but, they are bounds
- Good child ordering improves effectiveness of pruning

• With "perfect ordering":

- Time complexity drops to O(b^{m/2})
- Doubles solvable depth!
- Full search of, e.g. chess, is still hopeless...











Why Pacman Starves

- He knows his score will go up by eating the dot now
- He knows his score will go up just as much by eating the dot later on
- There are no point-scoring opportunities after eating the dot
- Therefore, waiting seems just as good as eating











A random variable represents an event whose outcome is unknown A random variable represents an event whose outcome is unknown A probability distribution is an assignment of weights to outcomes Example: traffic on freeway? Andom variable: T = wheth there's traffic Outcomes: T in {none, light, heavy} Distribution: P(T=none) = 0.25, P(T=light) = 0.55, P(T=heavy) = 0.20 Some laws of probability (more later): Probabilities are always non-negative Probabilities over all possible outcomes sum to one Aswe get more evidence, probabilities may change: P(T=heavy) = 0.20, P(T=heavy | Hour=Bam) = 0.61 We'll talk about methods for reasoning and updating probabilities later

What are Probabilities?

Objectivist / frequentist answer:

- Averages over repeated experiments
- E.g. empirically estimating P(rain) from historical observation
- E.g. pacman's estimate of what the ghost will do, given what it has done in the past
- Assertion about how future experiments will go (in the limit)
 Makes one think of *inherently random* events, like rolling dice
- Subjectivist / Bayesian answer:
 - Degrees of belief about unobserved variables
 - E.g. an agent's belief that it's raining, given the temperature
 - E.g. pacman's belief that the ghost will turn left, given the state
 - Often *learn* probabilities from past experiences (more later)
 - New evidence updates beliefs (more later)

Uncertainty Everywhere

Not just for games of chance!

- I'm sick: will I sneeze this minute? Email contains "FREE!": is it spam?
- Tooth hurts: have cavity? 60 min enough to get to the airport?
- Robot rotated wheel three times, how far did it advance?
- Safe to cross street? (Look both ways!)
- Sources of uncertainty in random variables:
 - Inherently random process (dice, etc) .
 - Insufficient or weak evidence
 - Ignorance of underlying processes
 - Unmodeled variables
 - The world's just noisy it doesn't behave according to plan!

Reminder: Expectations

- We can define function f(X) of a random variable X
- The expected value of a function is its average value, weighted by the probability distribution over inputs
- Example: How long to get to the airport? Length of driving time as a function of traffic:
 - L(none) = 20, L(light) = 30, L(heavy) = 60 What is my expected driving time?
 - Notation: E_{P(T)}[L(T)]
 - Remember, P(T) = {none: 0.25, light: 0.5, heavy: 0.25}
 - E[L(T)] = L(none) * P(none) + L(light) * P(light) + L(heavy) * P(heavy)
 - E[L(T)] = (20 * 0.25) + (30 * 0.5) + (60 * 0.25) = 35













Expectimax for Pacman

- Notice that we've gotten away from thinking that the ghosts are trying to minimize pacman's score
- Instead, they are now a part of the environment
- Pacman has a belief (distribution) over how they will act
- Quiz: Can we see minimax as a special case of expectimax?
- Quiz: what would pacman's computation look like if we assumed that the ghosts were doing 1-ply minimax and taking the result 80% of the time, otherwise moving randomly?









