CSE 473: Artificial Intelligence

Constraint Satisfaction

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Slides adapted from Dan Klein, Stuart Russell, Andrew Moore & Luke Zettlemoyer

Space of Search Strategies

- Blind Search
- DFS, BFS, IDS
- Informed Search
 - Systematic: Uniform cost, greedy, A*, IDA*
 - Stochastic: Hill climbing w/ random walk & restarts
- Constraint Satisfaction
- Backtracking=DFS, FC, k-consistency
- Adversary Search

Recap: Search Problem

States

- configurations of the world
- Successor function:
 - function from states to lists of triples (state, action, cost)
- Start state
- Goal test

Recap: Constraint Satisfaction Kind of search in which States are factored into sets of variables Search = assigning values to these variables Goal test is encoded with constraints → Gives structure to search space Exploration of one part informs others Special techniques add speed Propagation

- Variable ordering
- Preprocessing







Chinese Food, Family Style

- Suppose k people…
 - Variables & Domains?
 - Constraints?









Standard Search Formulation

- States are defined by the values assigned so far
- Initial state: the empty assignment, {}
- Successor function:
 - assign value to an unassigned variable
- Goal test:
 - the current assignment is complete &
 - satisfies all constraints



Backtracking Search

- Note 1: Only consider a single variable at each point
 - Variable assignments are commutative, so *fix ordering of variables* I.e., [WA = red then NT = blue] same as
 [NT = blue then WA = red]
 - What is branching factor of this search?

Backtracking Search

Note 2: Only allow legal assignments at each point

- I.e. Ignore values which conflict previous assignments
- Might need some computation to eliminate such conflicts
- "Incremental goal test"





Improving Backtracking

- General-purpose ideas give huge gains in speed
- Ordering:
 - Which variable should be assigned next?
 - In what order should its values be tried?
- Filtering: Can we detect inevitable failure early?
- Structure: Can we exploit the problem structure?

















































- CSPs are a special kind of search problem:
- States defined by values (domains) of a fixed set of variables
- Goal test defined by constraints on variable values
- Backtracking = DFS one legal variable assigned per node
- Variable ordering and value selection heuristics help
- · Forward checking prevents assignments that fail later
- Constraint propagation (e.g., arc consistency)
- does additional work to constrain values and detect inconsistencies
- Constraint graph representation
- Allows analysis of problem structure
- Tree-structured CSPs can be solved in linear time
- Iterative min-conflicts is usually effective in practice
- Local (stochastic) search