

More Search Methods

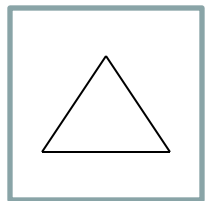
- Local Search
 - Hill Climbing
 - Simulated Annealing
 - Beam Search
 - Genetic Search
- Local Search in Continuous Spaces
- Searching with Nondeterministic Actions
- Online Search (agent is executing actions)

Local Search Algorithms and Optimization Problems

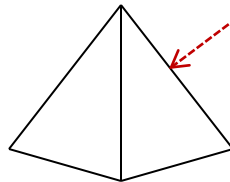
- **Complete state** formulation
 - For example, for the 8 queens problem, all 8 queens are on the board and need to be moved around to get to a goal state
- Equivalent to **optimization problems** often found in science and engineering
- Start somewhere and try to get to the solution from there
- **Local search** around the current state to decide where to go next

Pose Estimation Example

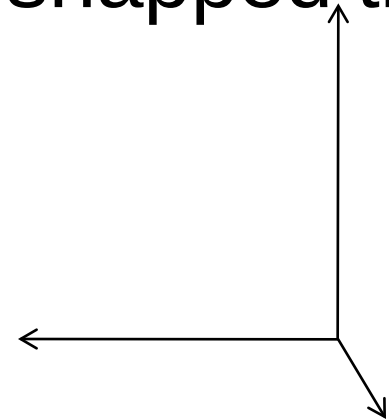
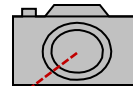
- Given a geometric model of a 3D object and a 2D image of the object.
- Determine the position and orientation of the object wrt the camera that snapped the image.



image



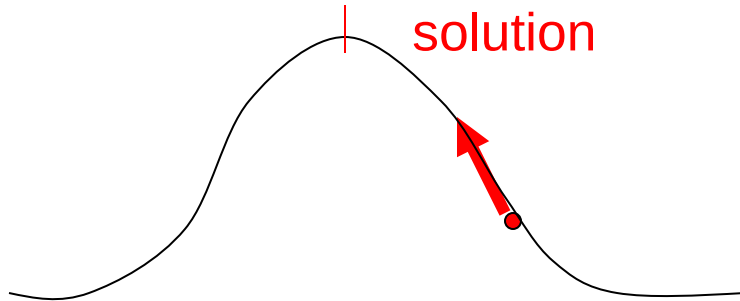
3D object



- State $(x, y, z, x\text{-angle}, y\text{-angle}, z\text{-angle})$

Hill Climbing

“Gradient ascent”



Note: solutions shown here as **max** not min.

Often used for numerical optimization problems.

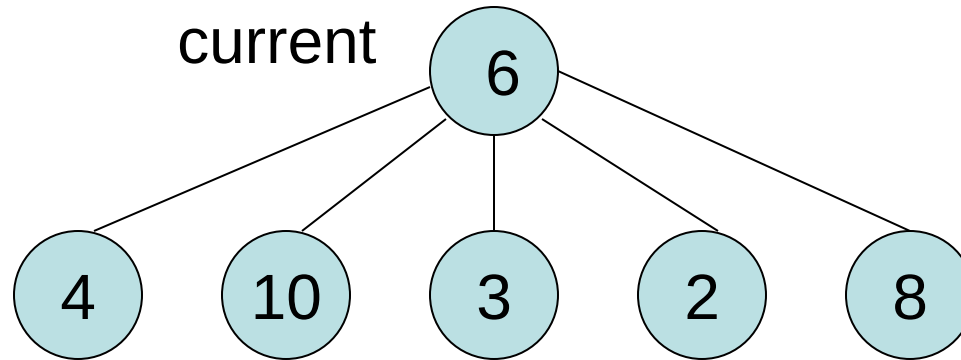
How does it work?

AI Hill Climbing

Steepest-Ascent Hill Climbing

- *current* $\leftarrow$ start node
- loop do
 - *neighbor* $\leftarrow$ a highest-valued successor of *current*
 - if *neighbor*.Value $\leq$ *current*.Value then return *current*.State
 - *current* $\leftarrow$ *neighbor*
- end loop

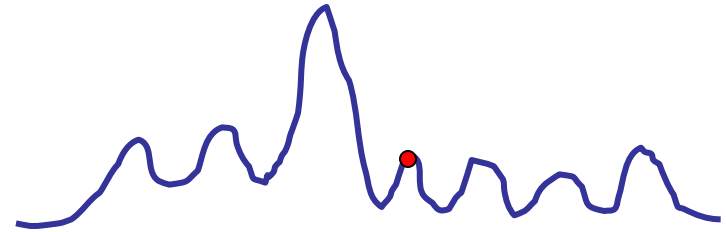
Hill Climbing Search



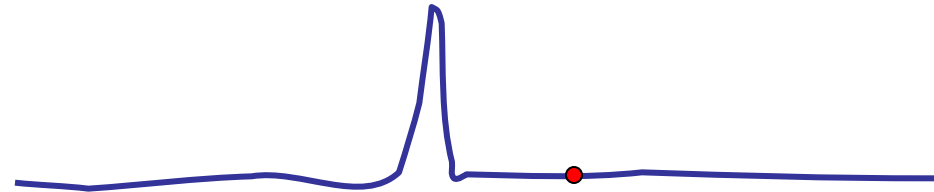
What if current had a value of 12?

Hill Climbing Problems

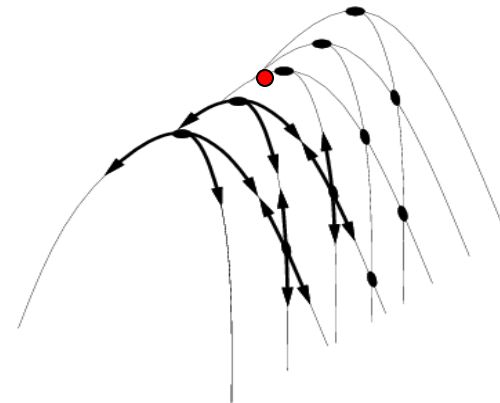
Local maxima



Plateaus



Diagonal ridges



What is it sensitive to?
Does it have any advantages?

Solving the Problems

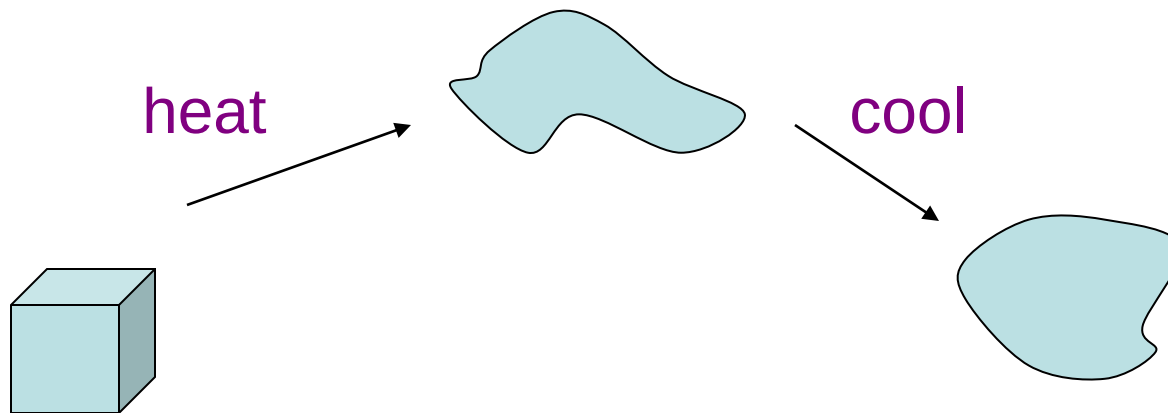
- **Allow backtracking** (What happens to complexity?)
- **Stochastic hill climbing**: choose at random from uphill moves, using steepness for a probability
- **Random restarts**: “If at first you don’t succeed, try, try again.”
- **Several moves** in each of several directions, then test
- **Jump** to a different part of the search space

Simulated Annealing

- Variant of hill climbing (so up is good)
- Tries to **explore** enough of the search space **early on**, so that the final solution is less sensitive to the start state
- May make some **downhill moves** before finding a good way to move uphill.

Simulated Annealing

- Comes from the physical process of annealing in which substances are raised to high energy levels (melted) and then cooled to solid state.



- The probability of moving to a higher energy state, instead of lower is $p = e^{(-\Delta E/kT)}$ where ΔE is the positive change in energy level, T is the temperature, and k is Boltzmann's constant.

Simulated Annealing

- At the beginning, the temperature is high.
- As the temperature becomes lower
 - kT becomes lower
 - $\Delta E/kT$ gets bigger
 - $(-\Delta E/kT)$ gets smaller
 - $e^{(-\Delta E/kT)}$ gets smaller
- As the process continues, the probability of a downhill move gets smaller and smaller.

For Simulated Annealing

- ΔE represents the change in the value of the objective function.
- Since the physical relationships no longer apply, drop k . So $p = e^{(-\Delta E/T)}$
- We need an **annealing schedule**, which is a sequence of values of T : $T_0, T_1, T_2, \dots$

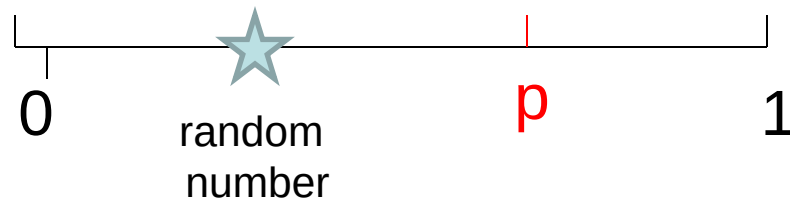
Simulated Annealing Algorithm

- $current \leftarrow$ start node;
- for each T on the schedule /* need a schedule */
 - $next \leftarrow$ randomly selected successor of $current$
 - evaluate next; if it's a goal, return it
 - $\Delta E \leftarrow next.Value - current.Value$ /* already negated */
 - if $\Delta E > 0$
 - then $current \leftarrow next$ /* better than current */
 - else $current \leftarrow next$ with probability $e^{(\Delta E/T)}$

How would you do this probabilistic selection?

Probabilistic Selection

- Select *next* with probability p



- Generate a random number
- If it's $\leq p$, select *next*

Simulated Annealing Properties

- At a fixed “temperature” T , state occupation probability reaches the Boltzman distribution

$$p(x) = \alpha e^{(E(x)/kT)}$$

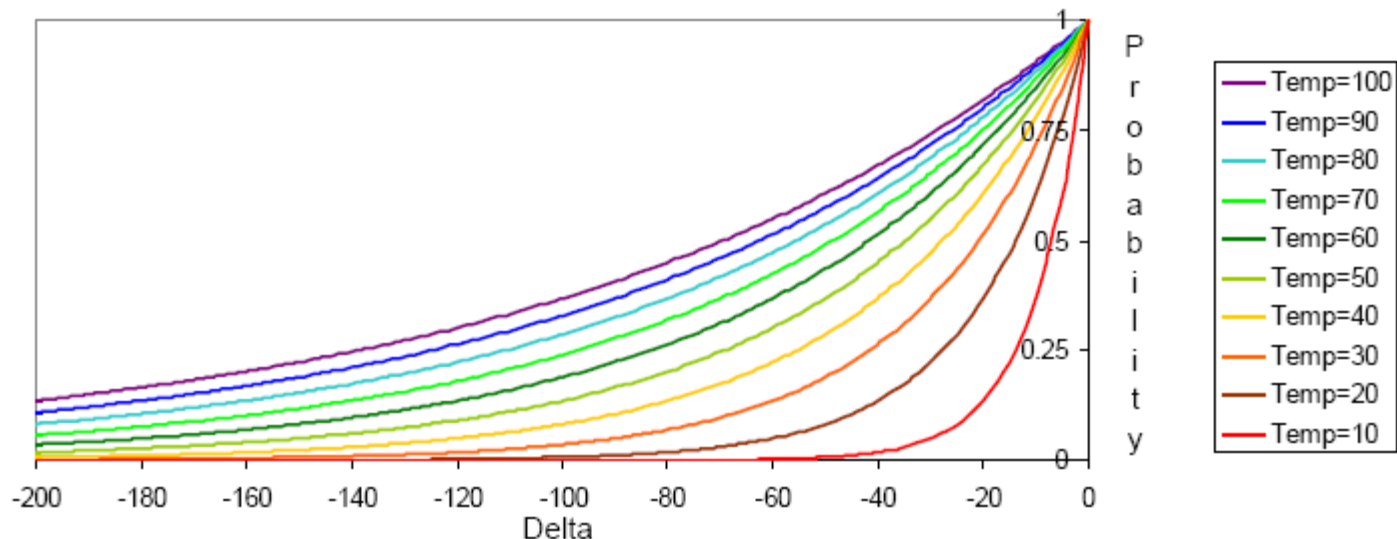
- If T is decreased slowly enough (very slowly), the procedure will reach the best state.
- Slowly enough has proven too slow for some researchers who have developed alternate schedules.

Simulated Annealing Schedules

- Acceptance criterion and cooling schedule

if ($\Delta \geq 0$) accept

else if ($\text{random} < e^{\Delta / \text{Temp}}$) accept, else reject /* $0 \leq \text{random} \leq 1$ */



Initially temperature is very high (most bad moves accepted)

Temp slowly goes to 0, with multiple moves attempted at each temperature

Final runs with temp=0 (always reject bad moves) greedily “quench” the system

Simulated Annealing Applications

- Basic Problems
 - Traveling salesman
 - Graph partitioning
 - Matching problems
 - Graph coloring
 - Scheduling
- Engineering
 - VLSI design
 - Placement
 - Routing
 - Array logic minimization
 - Layout
 - Facilities layout
 - Image processing
 - Code design in information theory

Local Beam Search

- Keeps more previous states in memory
 - Simulated annealing just kept one previous state in memory.
 - This search keeps k states in memory.
 - randomly generate k initial states
 - if any state is a goal, terminate
 - else, generate all successors and select best k
 - repeat

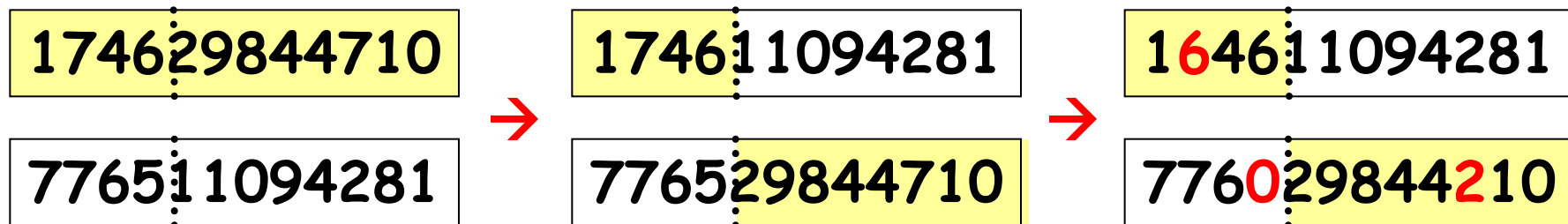
Pros? Cons?

Genetic Algorithms

- Start with random population of states
 - Representation serialized (ie. strings of characters or bits)
 - States are ranked with “fitness function”
- Produce new generation
 - Select random pair(s) using probability:
 - probability $\sim$ fitness
 - Randomly choose “crossover point”
 - Offspring mix halves
 - Randomly mutate bits

Crossover

Mutation



Genetic Algorithm

- Given: population **P** and fitness-function **f**
- repeat
 - **newP** $\leftarrow$ empty set
 - for $i = 1$ to **size(P)**
 - $x \leftarrow \text{RandomSelection}(\mathbf{P}, \mathbf{f})$
 - $y \leftarrow \text{RandomSelection}(\mathbf{P}, \mathbf{f})$
 - $child \leftarrow \text{Reproduce}(x, y)$
 - if (small random probability) then $child \leftarrow \text{Mutate}(child)$
 - add $child$ to **newP**
 - **P** $\leftarrow$ **newP**
- until some individual is fit enough or enough time has elapsed
- return the best individual in **P** according to **f**

Using Genetic Algorithms

- 2 important aspects to using them
 - 1. How to encode your real-life problem
 - 2. Choice of fitness function
- Research Example
 - We want to generate a new operator for finding interesting points on images
 - The operator will be some function of a set of values $v_1, v_2, \dots, v_K$.
 - Idea: weighted sums, weighted mins, weighted maxs. $a_1, \dots, a_K, b_1, \dots, b_K, c_1, \dots, c_K$

Local Search in Continuous Spaces

- Given a continuous state space
 $S = \{(x_1, x_2, \dots, x_N) \mid x_i \in \mathbb{R}\}$
- Given a continuous objective function
 $f(x_1, x_2, \dots, x_N)$
- The **gradient** of the objective function is a vector $\nabla f = (\partial f / \partial x_1, \partial f / \partial x_2, \dots, \partial f / \partial x_N)$
- The gradient gives the magnitude and direction of the steepest slope at a point.

Local Search in Continuous Spaces

- To find a maximum, the basic idea is to set $\nabla f = 0$
- Then updating of the current state becomes $x \leftarrow x + \alpha \nabla f(x)$
where α is a small constant.
- Theory behind this is taught in numerical methods classes.
- Your book suggests the Newton-Raphson method. Luckily there are packages.....

Computer Vision Pose Estimation Example



Figure 18: The pose computed from six point correspondence using the algorithm described in Section 5.2.



Figure 19: The pose computed from an ellipse-circle correspondence using the algorithm described in Section 5.6.

and

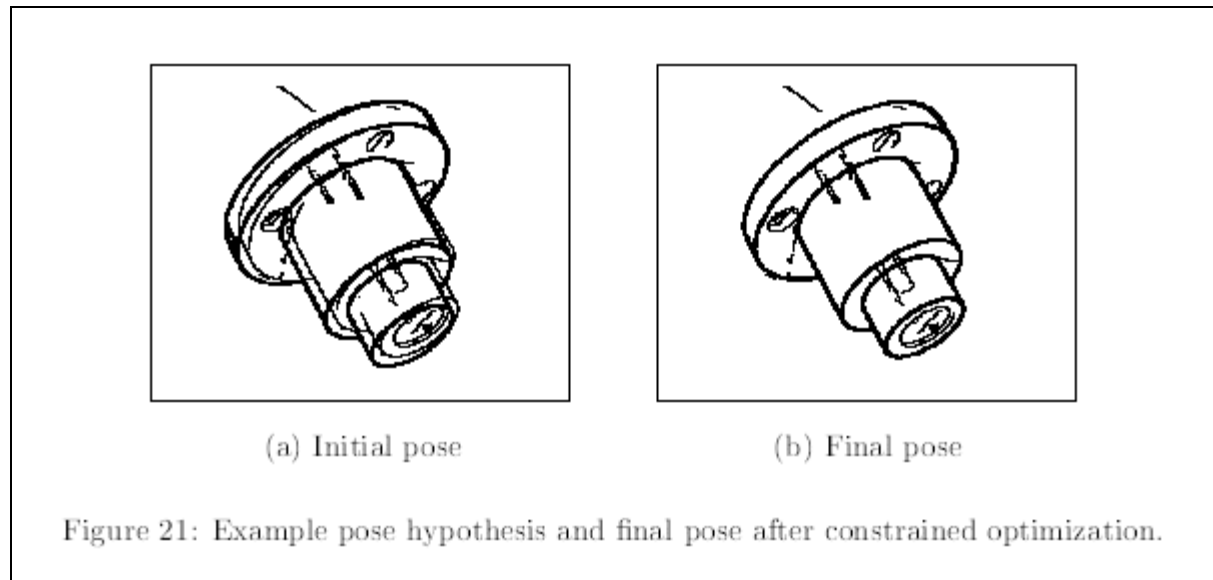
$$R = \begin{pmatrix} s^2 + l^2 - m^2 - n^2 & 2(lm - sn) & 2(ln + sm) \\ 2(lm + sn) & s^2 - l^2 + m^2 - n^2 & 2(mn - sl) \\ 2(ln - sm) & 2(mn + sl) & s^2 - l^2 - m^2 + n^2 \end{pmatrix}. \quad (52)$$

Powell's method [19] in the seven-dimensional space of the pose solution (four quaternion parameters and the translation t) is used, along with the constraint that the sum of the squares of the quaternion parameters must equal 1, as seen in equation (51). Figure 21 shows an initial pose estimate for a single-object image as



Figure 20: The pose computed from six point correspondence and one ellipse-circle correspondence using the generalized methodology.

Computer Vision Pose Estimation Example



Read the “Airports in Romania” example in the text.

Searching with Nondeterministic Actions

- Vacuum World (actions = {left, right, suck})

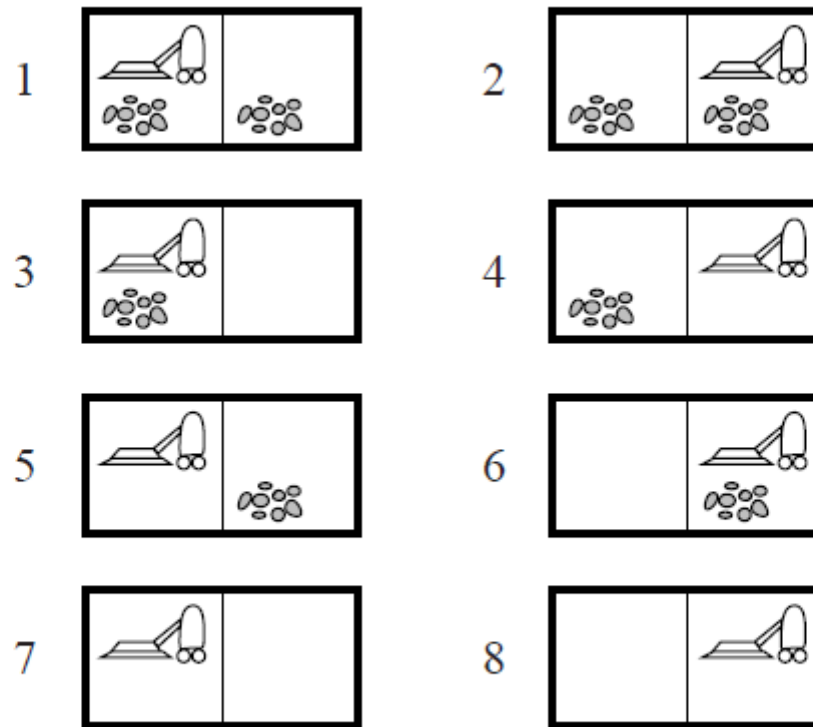


Figure 4.9 The eight possible states of the vacuum world; states 7 and 8 are goal states.

Searching with Nondeterministic Actions

In the **nondeterministic** case, the result of an action can vary.

Erratic Vacuum World:

- When sucking a dirty square, it cleans it and sometimes cleans up dirt in an adjacent square.
- When sucking a clean square, it sometimes deposits dirt on the carpet.

Generalization of State-Space Model

1. Generalize the **transition function** to return a set of possible outcomes.

$$\text{oldf: } S \times A \rightarrow S \quad \text{newf: } S \times A \rightarrow 2^S$$

2. Generalize the **solution** to a contingency plan.

if state=s then action-set-1 else action-set-2

3. Generalize the search tree to an AND-OR tree.

AND-OR Search Tree

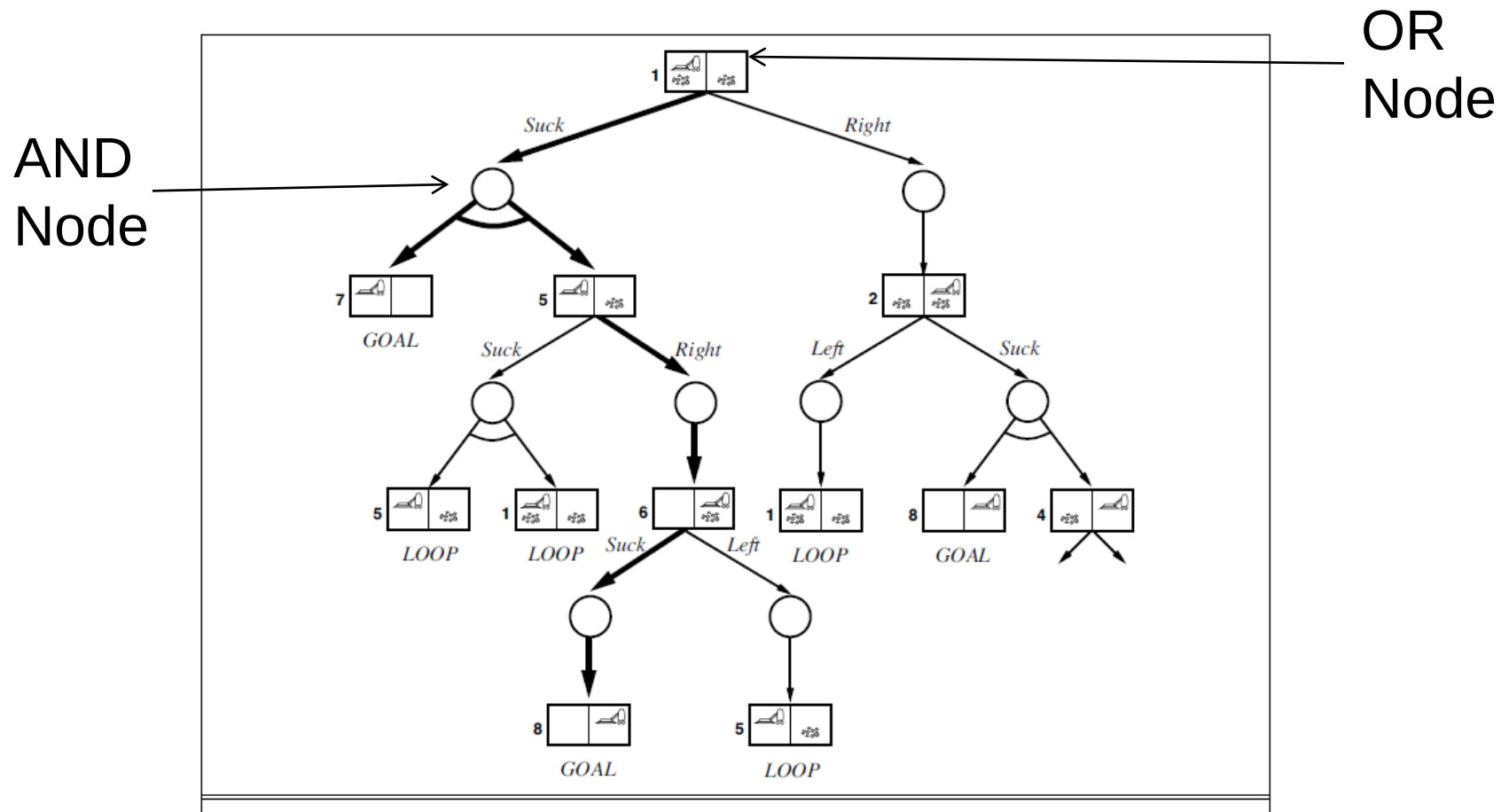


Figure 4.10 The first two levels of the search tree for the erratic vacuum world. State nodes are OR nodes where some action must be chosen. At the AND nodes, shown as circles, every outcome must be handled, as indicated by the arc linking the outgoing branches. The solution found is shown in bold lines.

Searching with Partial Observations

- The agent does not always know its state!
- Instead, it maintains a **belief state: a set of possible states it might be in.**
- **Example:** a robot can be used to build a map of a hostile environment. It will have sensors that allow it to “see” the world.

Belief State Space for Sensorless Agent

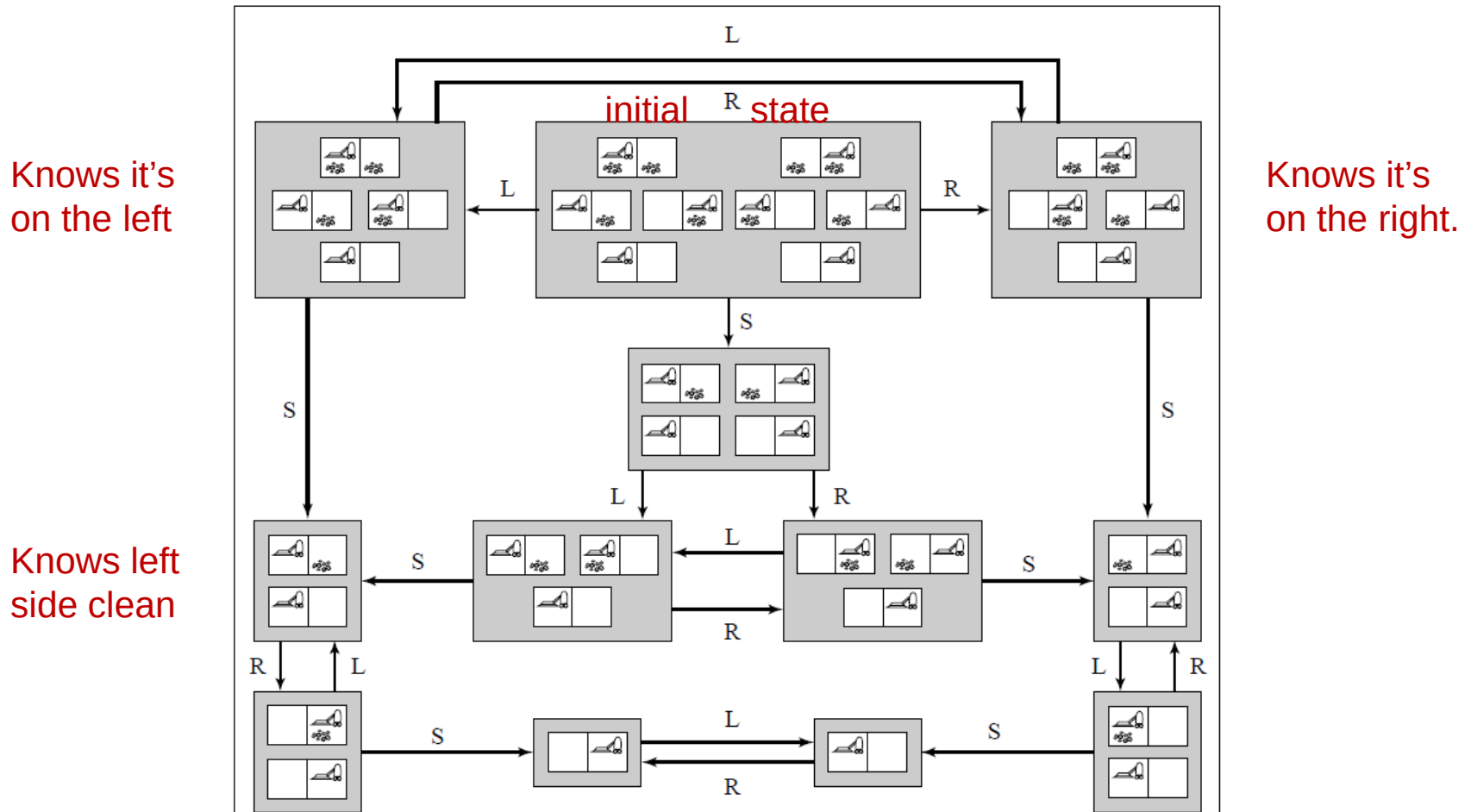


Figure 4.14 The reachable portion of the belief-state space for the deterministic, sensorless vacuum world. Each shaded box corresponds to a single belief state. At any given point, the agent is in a particular belief state but does not know which physical state it is in. The initial belief state (complete ignorance) is the top center box. Actions are represented by labeled links. Self-loops are omitted for clarity.

Online Search Problems

- **Active agent**
 - executes actions
 - acquires percepts from sensors
 - deterministic and fully observable
 - has to perform an action to know the outcome
- **Examples**
 - Web search
 - Autonomous vehicle