

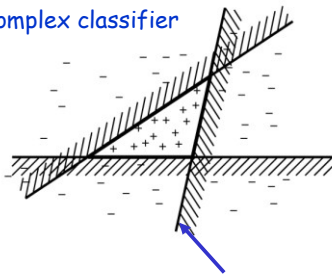
Ensemble Learning

Ensemble Learning

- Sometimes each learning technique yields a different hypothesis (or function)
- But no perfect hypothesis...
- Could we combine several imperfect hypotheses to get a better hypothesis?

Example

Combining 3 linear classifiers
⇒ More complex classifier



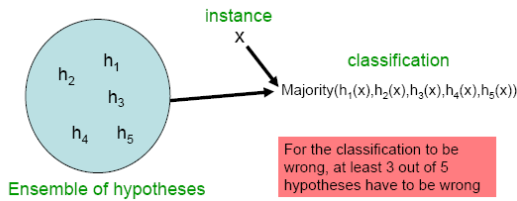
this line is one simple classifier saying that everything to the left is + and everything to the right is -

Ensemble Learning: Motivation

- Analogies:
 - Elections combine voters' choices to pick a good candidate (hopefully)
 - Committees combine experts' opinions to make better decisions
 - Students working together on Othello project
- Intuitions:
 - Individuals make mistakes but the "majority" may be less likely to
 - Individuals often have partial knowledge; a committee can pool expertise to make better decisions

Technique 1: Bagging

- Combine hypotheses via majority voting



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Bagging: Analysis

- Assumptions:
 - Each h_i makes error with probability p
 - The hypotheses are independent
- Majority voting of n hypotheses:
 - k hypotheses make an error: $\binom{n}{k} p^k (1-p)^{n-k}$
 - Majority makes an error: $\sum_{k > n/2} \binom{n}{k} p^k (1-p)^{n-k}$
 - With $n=5$, $p=0.1 \rightarrow \text{err}(\text{majority}) < 0.01$

Error probability went down from 0.1 to 0.01!

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Weighted Majority Voting

- In practice, hypotheses rarely independent
- Some hypotheses have less errors than others \Rightarrow all votes are not equal!
- Idea: Let's take a weighted majority

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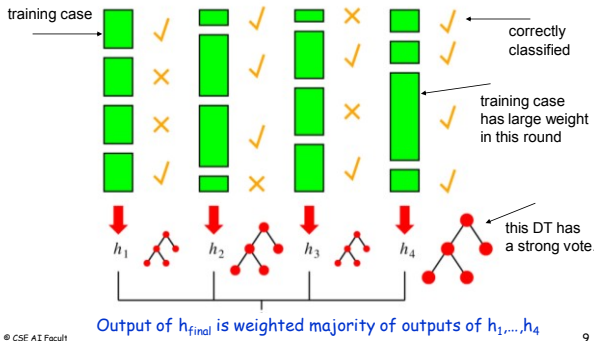
Technique 2: Boosting

- Most popular ensemble learning technique
 - Computes a weighted majority of hypotheses
 - Can "boost" performance of a "weak learner"
- Operates on a weighted training set
 - Each training example (instance) has a "weight"
 - Learning algorithm takes weight of input into account
- Idea: when an input is misclassified by a hypothesis, increase its weight so that the next hypothesis is more likely to classify it correctly

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Boosting Example with Decision Trees (DTs)



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AdaBoost Algorithm

(Adaptive Boosting)

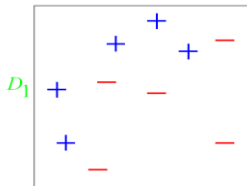
- $w_j \leftarrow 1/N \quad \forall_j$
- For $m=1$ to M do
 - $h_m \leftarrow \text{learn}(\text{dataset}, w)$
 - $\text{err} \leftarrow 0$
 - For each (x_j, y_j) in dataset do
 - If $h_m(x_j) \neq y_j$ then $\text{err} \leftarrow \text{err} + w_j$
 - For each (x_j, y_j) in dataset do
 - If $h_m(x_j) = y_j$ then $w_j \leftarrow w_j \text{err} / (1-\text{err})$
 - $w \leftarrow \text{normalize}(w)$
 - $z_m \leftarrow \log [(1-\text{err}) / \text{err}]$
- Return *weighted-majority*(h, z)

w : vector of N instance weights
 z : vector of M hypoth. weights

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AdaBoost Example



Original training set D_1 : Equal weights to all training inputs
 Goal: In round t , learn classifier h_t that minimizes error with respect to weighted training set
 h_t maps input to True (+1) or False (-1) $h_t : X \rightarrow \{-1, +1\}$

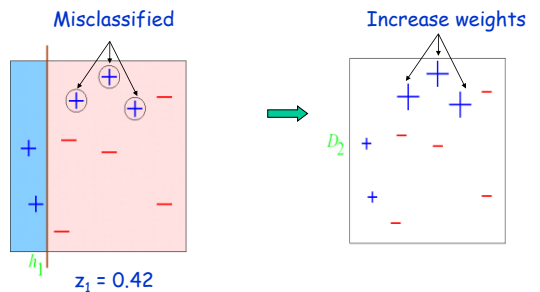
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Taken from "A Tutorial on Boosting" by Yoav Freund and Rob Schapire

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AdaBoost Example

ROUND 1

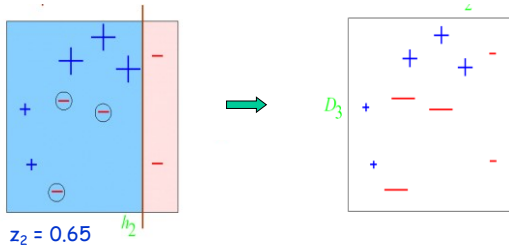


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AdaBoost Example

ROUND 2

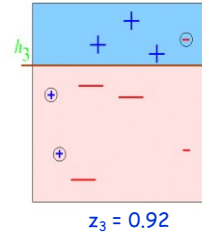


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AdaBoost Example

ROUND 3



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AdaBoost Example

$$h_{\text{final}} = \text{sign} \left(0.42 \left[\begin{array}{|c|} \hline \text{blue} \\ \hline \text{pink} \end{array} \right] + 0.65 \left[\begin{array}{|c|} \hline \text{blue} \\ \hline \text{pink} \end{array} \right] + 0.92 \left[\begin{array}{|c|} \hline \text{blue} \\ \hline \text{pink} \end{array} \right] \right)$$

$\text{sign}(x) = +1$ if $x > 0$ and -1 otherwise

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Example 1: Semantic Mapping

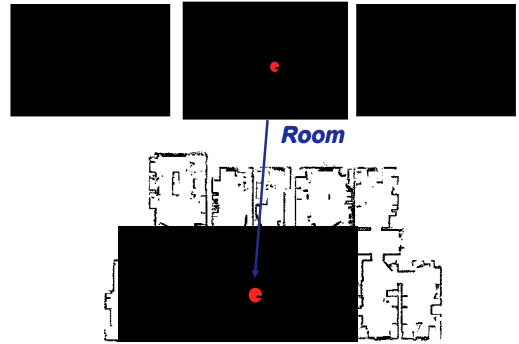


Motivation

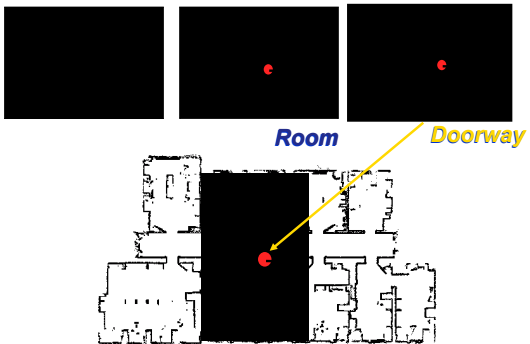


- **Human-Robot interaction:**
 - **User:** "Go to the corridor"

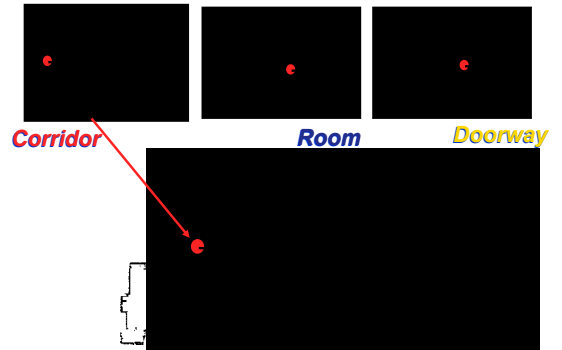
Shape



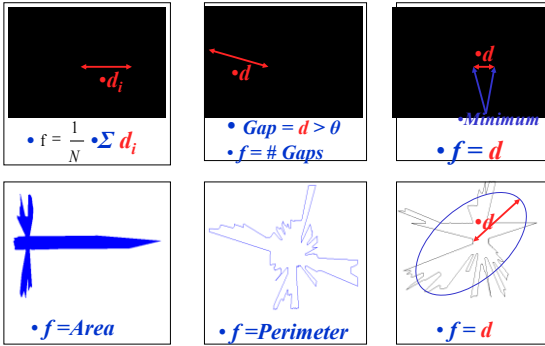
Observations



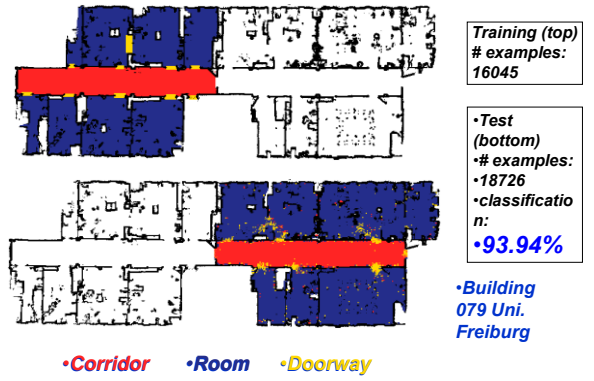
Observations



Simple Features



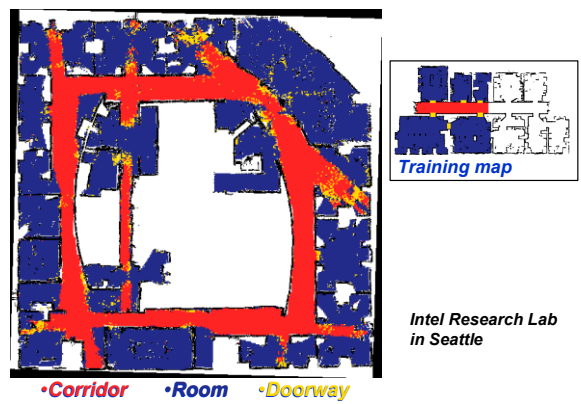
Experiments



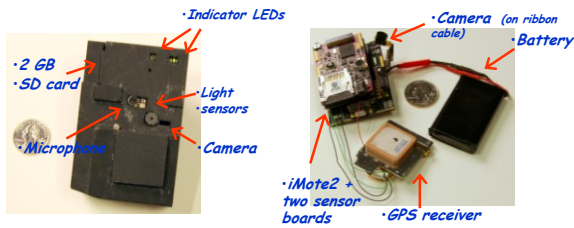
Application to a New Environment



Application to a New Environment



Example 2: Wearable Multi-Sensor Unit

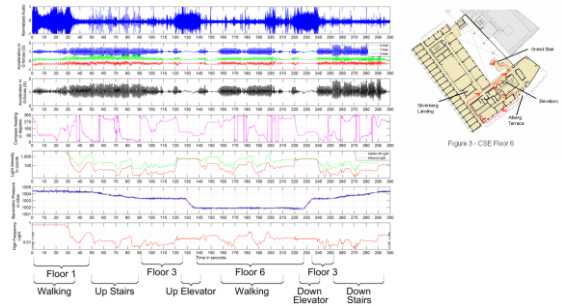


- Records 4 hours of audio, images (1/sec), GPS, and sensor data (accelerometer, barometric pressure, light intensity, gyroscope, magnetometer)

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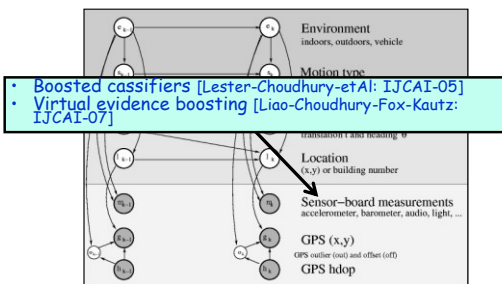
Data Stream

Courtesy of G. Borriello



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Activity Recognition Model



Accuracy: 88% activities, 93% environment

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Boosting

- Extremely flexible framework
- Handles high-dimensional continuous data
- Easy to implement
- Limitation: Only models local classification problems

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