

## Example: service robot



states??:

operators??:

goal test??:

path cost??:

## Search algorithms

Basic idea:

offline, simulated exploration of state space  
by generating successors of already-explored states  
(a.k.a. *expanding* states)

```
function GENERAL-SEARCH(problem, strategy) returns a solution, or failure
  initialize the search tree using the initial state of problem
  loop do
    if there are no candidates for expansion then return failure
    choose a leaf node for expansion according to strategy
    if the node contains a goal state then return the corresponding solution
    else expand the node and add the resulting nodes to the search tree
  end
```

## Example: service robot



states??: real-valued coordinates of manipulator joint angles (retracted?)

real-valued position of robot (which room, floor?)

doors (where, open, closed) , people (where)

coffee machine (where, full)

operators??: continuous motions of robot (abstract navigation actions)

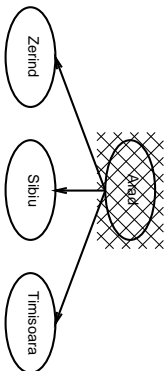
goal test??: coffee delivered to Henry

path cost??: time to execute

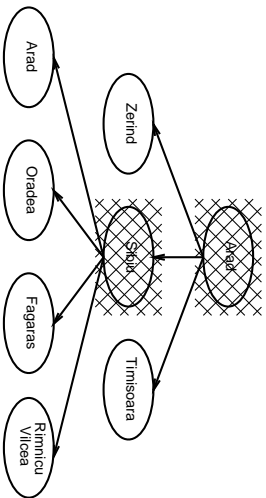
## General search example

Arad

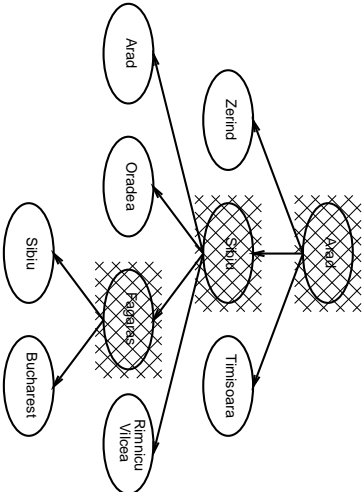
# General search example



# General search example



# General search example



# Implementation of search algorithms

```
function GENERAL-SEARCH(problem, QUEUING-FN) returns a solution, or failure
  nodes ← MAKE-QUEUE(MAKE-NODE(INITIAL-STATE[problem]))
  loop do
    if nodes is empty then return failure
    node ← REMOVE-FRONT(nodes)
    if GOAL-TEST[problem] applied to STATE(node) succeeds then return node
    nodes ← QUEUING-FN(nodes, EXPAND(node, OPERATORS[problem]))
  end
```

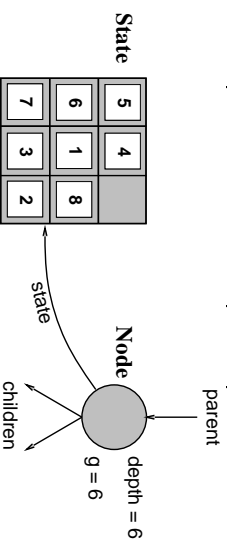
## Implementation contd: states vs. nodes

A *state* is a (representation of) a physical configuration

A *node* is a data structure constituting part of a search tree

includes *parent*, *children*, *depth*, *path cost*  $g(x)$

*States* do not have parents, children, depth, or path cost!



The EXPAND function creates new nodes, filling in the various fields and using the OPERATORS (or SUCCESSORFN) of the problem to create the corresponding states.

## Uninformed search strategies

*Uninformed* strategies use only the information available in the problem definition

Breadth-first search

Uniform-cost search

Depth-first search

Depth-limited search

Iterative deepening search

## Search strategies

A strategy is defined by picking the *order of node expansion*

Strategies are evaluated along the following dimensions:

completeness—does it always find a solution if one exists?

time complexity—number of nodes generated/expanded

space complexity—maximum number of nodes in memory

optimality—does it always find a least-cost solution?

Time and space complexity are measured in terms of

$b$ —maximum branching factor of the search tree

$d$ —depth of the least-cost solution

$m$ —maximum depth of the state space (may be  $\infty$ )

## Breadth-first search

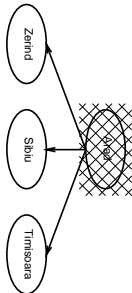
Expand shallowest unexpanded node

Implementation:

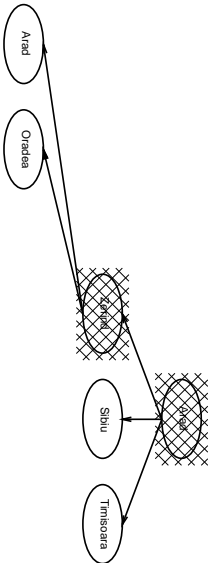
QUEUEENGFN = put successors at end of queue



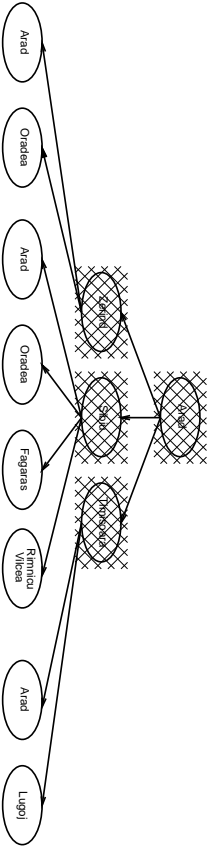
Breadth-first search



Breadth-first search



Breadth-first search



Properties of breadth-first search

Complete??

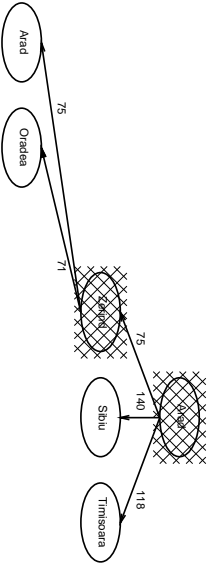
Time??

Space??

Optimal??



Uniform-cost search



Properties of uniform-cost search

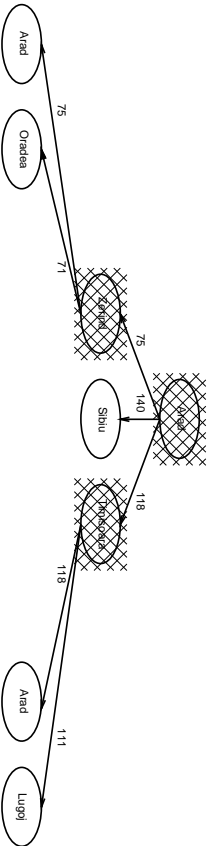
Complete?? Yes, if step cost  $\geq \epsilon$

Time?? # of nodes with  $g \leq$  cost of optimal solution

Space?? # of nodes with  $g \leq$  cost of optimal solution

Optimal?? Yes

Uniform-cost search



Depth-first search

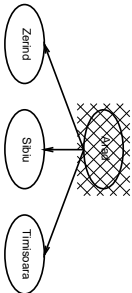
Expand deepest unexpanded node

Implementation:

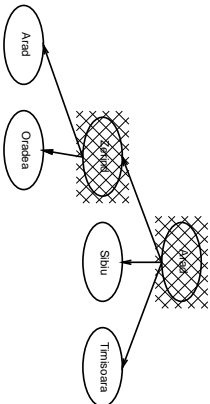
QUEUEINGFN = insert successors at front of queue



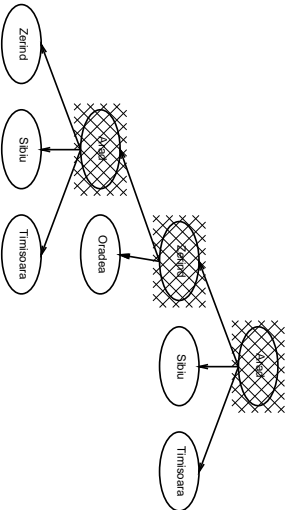
Depth-first search



Depth-first search



Depth-first search

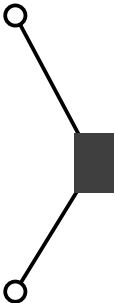


I.e., depth-first search can perform infinite cyclic excursions  
Need a finite, non-cyclic search space (or repeated-state checking)

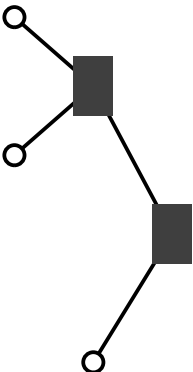
DFS on a depth-3 binary tree

O

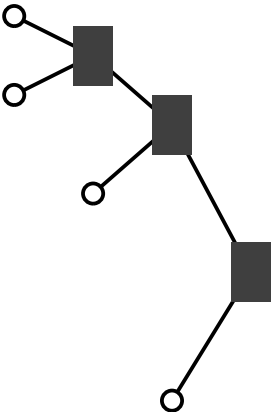
DFS on a depth-3 binary tree



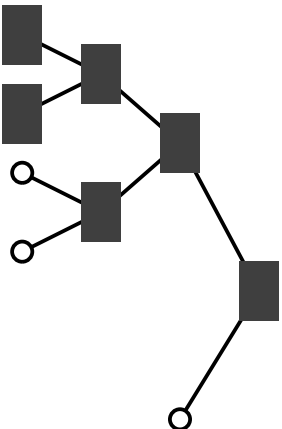
DFS on a depth-3 binary tree



DFS on a depth-3 binary tree

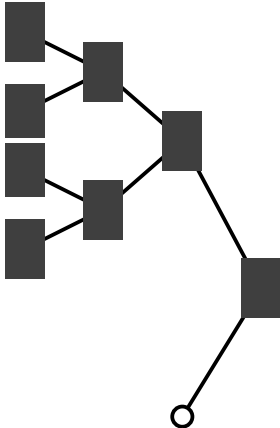


DFS on a depth-3 binary tree

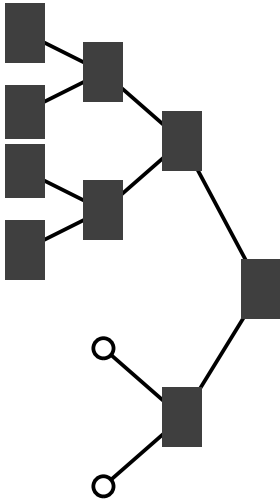




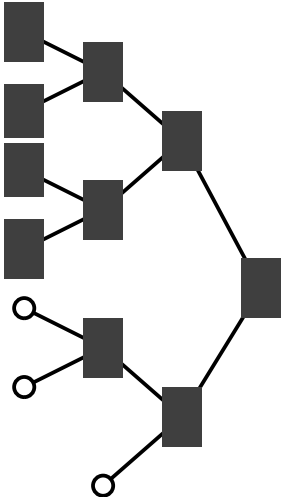
DFS on a depth-3 binary tree, contd.



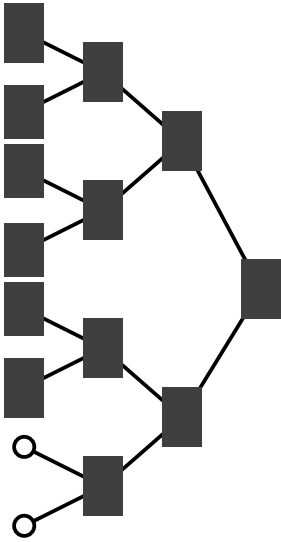
DFS on a depth-3 binary tree



DFS on a depth-3 binary tree



DFS on a depth-3 binary tree



# Properties of depth-first search

Complete??

Time??

Space??

Optimal??

# Depth-limited search

= depth-first search with depth limit  $l$

Implementation:

Nodes at depth  $l$  have no successors

# Properties of depth-first search

Complete?? No: fails in infinite-depth spaces, spaces with loops

Modify to avoid repeated states along path

⇒ complete in finite spaces

Time??  $O(b^m)$ : terrible if  $m$  is much larger than  $d$

but if solutions are dense, may be much faster than breadth-first

Space??  $O(bm)$ , i.e., linear space!

Optimal?? No

# Iterative deepening search

```
function ITERATIVE-DEEPENING-SEARCH(problem) returns a solution sequence
  inputs: problem, a problem
  for depth ← 0 to ∞ do
    result ← DEPTH-LIMITED-SEARCH(problem, depth)
    if result ≠ cutoff then return result
  end
```

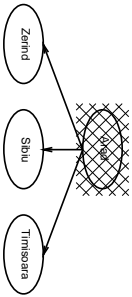
Iterative deepening search  $l = 0$



Iterative deepening search  $l = 1$



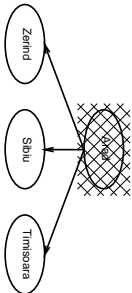
Iterative deepening search  $l = 1$



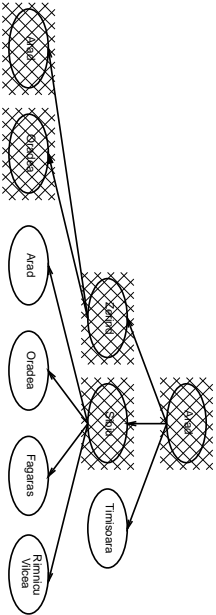
Iterative deepening search  $l = 2$



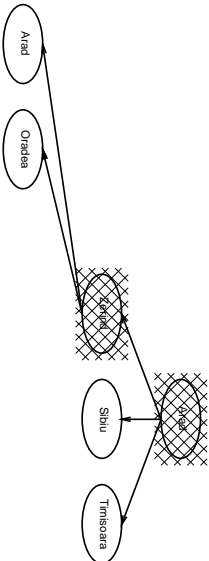
Iterative deepening search  $l = 2$



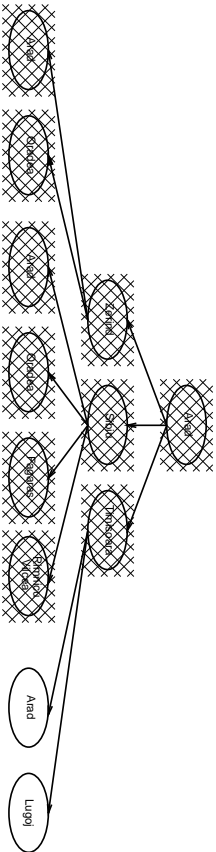
Iterative deepening search  $l = 2$



Iterative deepening search  $l = 2$



Iterative deepening search  $l = 2$



## Properties of iterative deepening search

Complete??

Time??

Space??

Optimal??

## Properties of iterative deepening search

Complete?? Yes

Time??  $(d + 1)b^0 + db^1 + (d - 1)b^2 + \dots + b^d = O(b^d)$

Space??  $O(bd)$

Optimal?? Yes, if step cost = 1

Breadth-first:	1 + 10 + 100 + 1,000 + 10,000 + 100,000 = 111,111
Iterative deepening:	6 + 50 + 400 + 3,000 + 20,000 + 100,000 = 123,456

For  $b = 10$ , iterative deepening search expands only 11% more nodes than breadth-first search!

## Properties of iterative deepening search

Complete?? Yes

Time??  $(d + 1)b^0 + db^1 + (d - 1)b^2 + \dots + b^d = O(b^d)$

Space??  $O(bd)$

Optimal?? Yes, if step cost = 1

## Summary

Problem formulation usually requires abstracting away real-world details to define a state space that can feasibly be explored

Variety of uninformed search strategies

Iterative deepening search uses only linear space and not much more time than other uninformed algorithms