## Where we are in the Course

- More fun in the Network Layer!
- We've covered packet forwarding
- Now we'll learn about routing

| Application |
| :---: |
| Transport |
| Network |
| Link |
| Physical |

## Improving on the Spanning Tree

- Spanning tree provides basic connectivity
- e.g., some path $B \rightarrow C$

- Routing uses all links to find "best" paths
- e.g., use BC, BE, and CE



## Perspective on Bandwidth Allocation

- Routing allocates network bandwidth adapting to failures; other mechanisms used at other timescales

| Mechanism | Timescale / Adaptation |
| :--- | :--- |
| Load-sensitive routing | Seconds / Traffic hotspots |
| Routing | Minutes / Equipment failures |
| Traffic Engineering | Hours / Network load |
| Provisioning | Months / Network customers |

## Delivery Models

- Different routing used for different delivery models



Anycast
(§5.2.9)


## Goals of Routing Algorithms

- We want several properties of any routing scheme:

| Property | Meaning |
| :--- | :--- |
| Correctness | Finds paths that work |
| Efficient paths | Uses network bandwidth well |
| Fair paths | Doesn't starve any nodes |
| Fast convergence | Recovers quickly after changes |
| Scalability | Works well as network grows large |

## Rules of Routing Algorithms

- Decentralized, distributed setting
- All nodes are alike; no controller
- Nodes only know what they learn by exchanging messages with neighbors
- Nodes operate concurrently
- May be node/link/message failures



## Topic

- Defining "best" paths with link costs
- These are shortest path routes



## What are "Best" paths anyhow?

- Many possibilities:
- Latency, avoid circuitous paths
- Bandwidth, avoid slow links
- Money, avoid expensive links
- Hops, to reduce switching
- But only consider topology
- Ignore workload, e.g., hotspots



## Shortest Paths

We'll approximate "best" by a cost function that captures the factors

- Often call lowest "shortest"

1. Assign each link a cost (distance)
2. Define best path between each pair of nodes as the path that has the lowest total cost (or is shortest)
3. Pick randomly to any break ties

## Shortest Paths (2)

- Find the shortest path $\mathrm{A} \rightarrow \mathrm{E}$
- All links are bidirectional, with equal costs in each direction
- Can extend model to unequal costs if needed



## Shortest Paths (3)

- $A B C E$ is a shortest path
- $\operatorname{dist}(\mathrm{ABCE})=4+2+1=7$
- This is less than:
$-\operatorname{dist}(\mathrm{ABE})=8$
$-\operatorname{dist}(A B F E)=9$
$-\operatorname{dist}(\mathrm{AE})=10$
$-\operatorname{dist}(\mathrm{ABCDE})=10$



## Shortest Paths (4)

- Optimality property:
- Subpaths of shortest paths are also shortest paths
- $A B C E$ is a shortest path



## Sink Trees

- Sink tree for a destination is the union of all shortest paths towards the destination
- Similarly source tree
- Find the sink tree for E



## Sink Trees (2)

- Implications:
- Only need to use destination to follow shortest paths
- Each node only need to send to the next hop
- Forwarding table at a node



## Topic

- How to compute shortest paths given the network topology
- With Dijkstra's algorithm



## Edsger W. Dijkstra (1930-2002)

- Famous computer scientist
- Programming languages
- Distributed algorithms
- Program verification
- Dijkstra's algorithm, 1969
- Single-source shortest paths, given network with non-negative link costs


## Dijkstra’s Algorithm

Algorithm:

- Mark all nodes tentative, set distances from source to 0 (zero) for source, and $\infty$ (infinity) for all other nodes
- While tentative nodes remain:
- Extract N , a node with lowest distance
- Add link to $N$ to the shortest path tree
- Relax the distances of neighbors of $N$ by lowering any better distance estimates


## Dijkstra’s Algorithm (2)

- Initialization



## Dijkstra's Algorithm (3)

- Relax around A



## Dijkstra's Algorithm (4)

- Relax around B



## Dijkstra's Algorithm (5)

- Relax around C



## Dijkstra's Algorithm (6)

- Relax around G (say)



## Dijkstra’s Algorithm (7)

- Relax around F (say)



## Dijkstra's Algorithm (8)

- Relax around E



## Dijkstra's Algorithm (9)

- Relax around D



## Dijkstra's Algorithm (10)

- Finally, H ... done



## Dijkstra Comments

- Finds shortest paths in order of increasing distance from source
- Leverages optimality property
- Runtime depends on efficiency of extracting min-cost node
- Superlinear in network size (grows fast)
- Gives complete source/sink tree
- More than needed for forwarding!
- But requires complete topology


## Topic

- How to compute shortest paths in a distributed network
- The Distance Vector (DV) approach



## Distance Vector Routing

- Simple, early routing approach
- Used in ARPANET, and RIP
- One of two main approaches to routing
- Distributed version of Bellman-Ford
- Works, but very slow convergence after some failures
- Link-state algorithms are now typically used in practice
- More involved, better behavior


## Distance Vector Setting

Each node computes its forwarding table in a distributed setting:

1. Nodes know only the cost to their neighbors; not the topology
2. Nodes can talk only to their neighbors using messages
3. All nodes run the same algorithm concurrently
4. Nodes and links may fail, messages may be lost

## Distance Vector Algorithm

Each node maintains a vector of distances (and next hops) to all destinations

1. Initialize vector with 0 (zero) cost to self, $\infty$ (infinity) to other destinations
2. Periodically send vector to neighbors
3. Update vector for each destination by selecting the shortest distance heard, after adding cost of neighbor link

- Use the best neighbor for forwarding


## Distance Vector (2)

- Consider from the point of view of node $A$
- Can only talk to nodes B and E

Initial $\longrightarrow$
vector

| To | Cost |
| :---: | :---: |
| A | 0 |
| B | $\infty$ |
| C | $\infty$ |
| D | $\infty$ |
| E | $\infty$ |
| F | $\infty$ |
| G | $\infty$ |
| H | $\infty$ |



## Distance Vector (3)

- First exchange with $B$, $E$; learn best 1-hop routes

| To | $\begin{array}{\|c\|} \hline \text { B } \\ \text { says } \end{array}$ | $\begin{gathered} \mathrm{E} \\ \text { says } \end{gathered}$ | $\begin{gathered} \text { B } \\ +4 \end{gathered}$ | $\begin{gathered} \mathrm{E} \\ +10 \end{gathered}$ | $\rightarrow$ | A's Cost | A's Next |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| A | $\infty$ | $\infty$ | $\infty$ | $\infty$ |  | 0 | -- |
| B | 0 | $\infty$ | 4 | $\infty$ |  | 4 | B |
| C | $\infty$ | $\infty$ | $\infty$ | $\infty$ |  | $\infty$ | -- |
| D | $\infty$ | $\infty$ | $\infty$ | $\infty$ |  | $\infty$ | -- |
| E | $\infty$ | 0 | $\infty$ | 10 |  | 10 | E |
| F | $\infty$ | $\infty$ | $\infty$ | $\infty$ |  | $\infty$ | -- |
| G | $\infty$ | $\infty$ | $\infty$ | $\infty$ |  | $\infty$ | -- |
| H | $\infty$ | $\infty$ | $\infty$ | $\infty$ |  | $\infty$ | -- |



## Distance Vector (4)

- Second exchange; learn best 2-hop routes

| To | B <br> says | E <br> says |
| :---: | :---: | :---: |
| A | 4 | 10 |
| B | 0 | 4 |
| C | 2 | 1 |
| D | $\infty$ | 2 |
| E | 4 | 0 |
| F | 3 | 2 |
| G | 3 | $\infty$ |
| $H$ | $\infty$ | $\infty$ |$\quad$| B <br> $\mathbf{+ 4}$ | E <br> $\mathbf{+ 1 0}$ |
| :---: | :---: |
| 8 | 20 |
| 4 | 14 |
| 6 | 11 |
| $\infty$ | 12 |
| 8 | 10 |
| 7 | 12 |
| 7 | $\infty$ |
| $\infty$ | $\infty$ |$\quad \rightarrow$| A's <br> Cost | A's <br> Next |
| :---: | :---: |
| 0 | -- |
| 4 | B |
| 6 | B |
| 12 | E |
| 8 | B |
| 7 | B |
| 7 | B |
| $\infty$ | -- |



## Distance Vector (4)

- Third exchange; learn best 3-hop routes

| To | $\begin{gathered} \mathrm{B} \\ \text { says } \end{gathered}$ | $\begin{gathered} \mathrm{E} \\ \text { says } \end{gathered}$ | $\begin{gathered} B \\ +4 \end{gathered}$ | $\begin{gathered} E \\ +10 \end{gathered}$ |  | A's Cost | $\begin{aligned} & \text { A's } \\ & \text { Vext } \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| A | 4 | 8 | 8 | 18 |  | 0 | -- |
| B | 0 | 3 | 4 | 13 |  | 4 | B |
| C | 2 | 1 | 6 | 11 |  | 6 | B |
| D | 4 | 2 | 8 | 12 |  | 8 | B |
| E | 3 | 0 | 7 | 10 |  | 7 | B |
| F | 3 | 2 | 7 | 12 |  | 7 | B |
| G | 3 | 6 | 7 | 16 |  | 7 | B |
| H | 5 | 4 | 9 | 14 |  | 9 | B |



## Distance Vector (5)

- Subsequent exchanges; converged

| To | B <br> says | E <br> says |
| :---: | :---: | :---: |
| A | 4 | 7 |
| B | 0 | 3 |
| C | 2 | 1 |
| D | 4 | 2 |
| E | 3 | 0 |
| F | 3 | 2 |
| G | 3 | 6 |
| H | 5 | 4 |$\quad$| B <br> $\mathbf{+ 4}$ | E <br> $\mathbf{+ 1 0}$ |
| :---: | :---: |
| 8 | 17 |
| 4 | 13 |
| 6 | 11 |
| 8 | 12 |
| 7 | 10 |
| 7 | 12 |
| 7 | 16 |
| 9 | 14 |$\quad$| A's <br> Cost | A's <br> Next |
| :---: | :---: |
| 0 | -- |
| 4 | B |
| 6 | B |
| 8 | B |
| 8 | B |
| 7 | B |
| 7 | B |
| 9 | B |



## Distance Vector Dynamics

- Adding routes:
- News travels one hop per exchange
- Removing routes
- When a node fails, no more exchanges, other nodes forget
- But partitions (unreachable nodes in divided network) are a problem
- "Count to infinity" scenario


## DV Dynamics (2)

- Good news travels quickly, bad news slowly (inferred)


Desired convergence

"Count to infinity" scenario

## DV Dynamics (3)

- Various heuristics to address
- e.g., "Split horizon, poison reverse" (Don't send route back to where you learned it from.)
- But none are very effective
- Link state now favored in practice
- Except when very resource-limited

