

# Link Layer

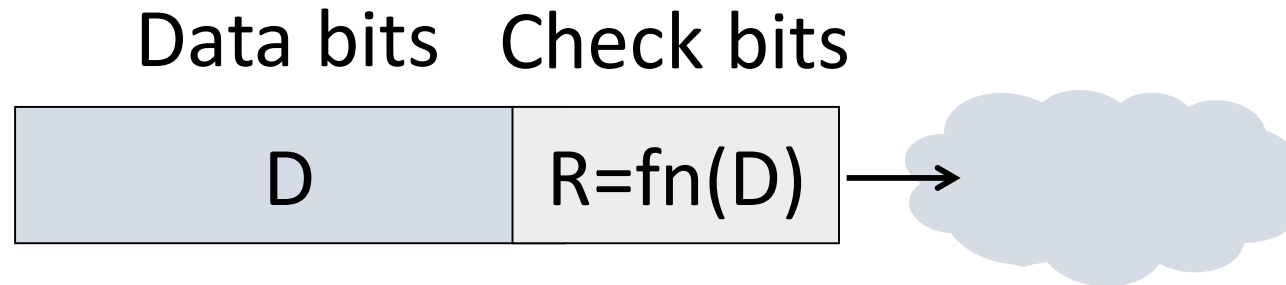
(continued)

# Topics

1. Framing
  - Delimiting start/end of frames
2. Error detection and **correction**
  - Handling errors
3. Retransmissions
  - Handling loss
4. Multiple Access
  - 802.11, classic Ethernet
5. Switching
  - Modern Ethernet

# Using Error Codes

- Codeword consists of  $D$  data plus  $R$  check bits (=systematic block code)

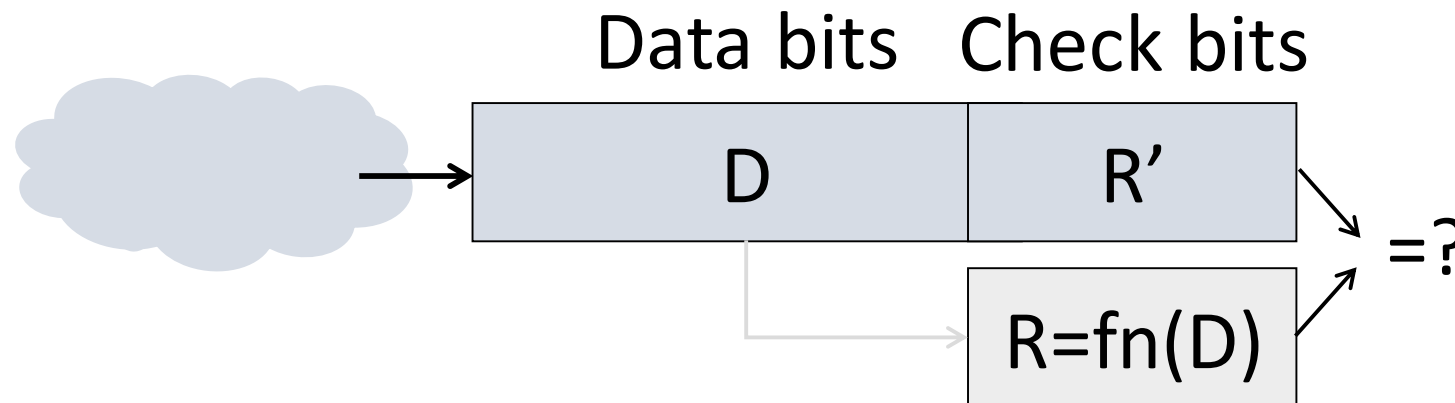


- Sender:
  - Compute  $R$  check bits based on the  $D$  data bits; send the codeword of  $D+R$  bits

# Using Error Codes

- Receiver:

- Receive  $D+R$  bits with unknown errors
- Recompute  $R$  check bits based on the  $D$  data bits; error if  $R$  doesn't match  $R'$



# Why Error Correction is Hard

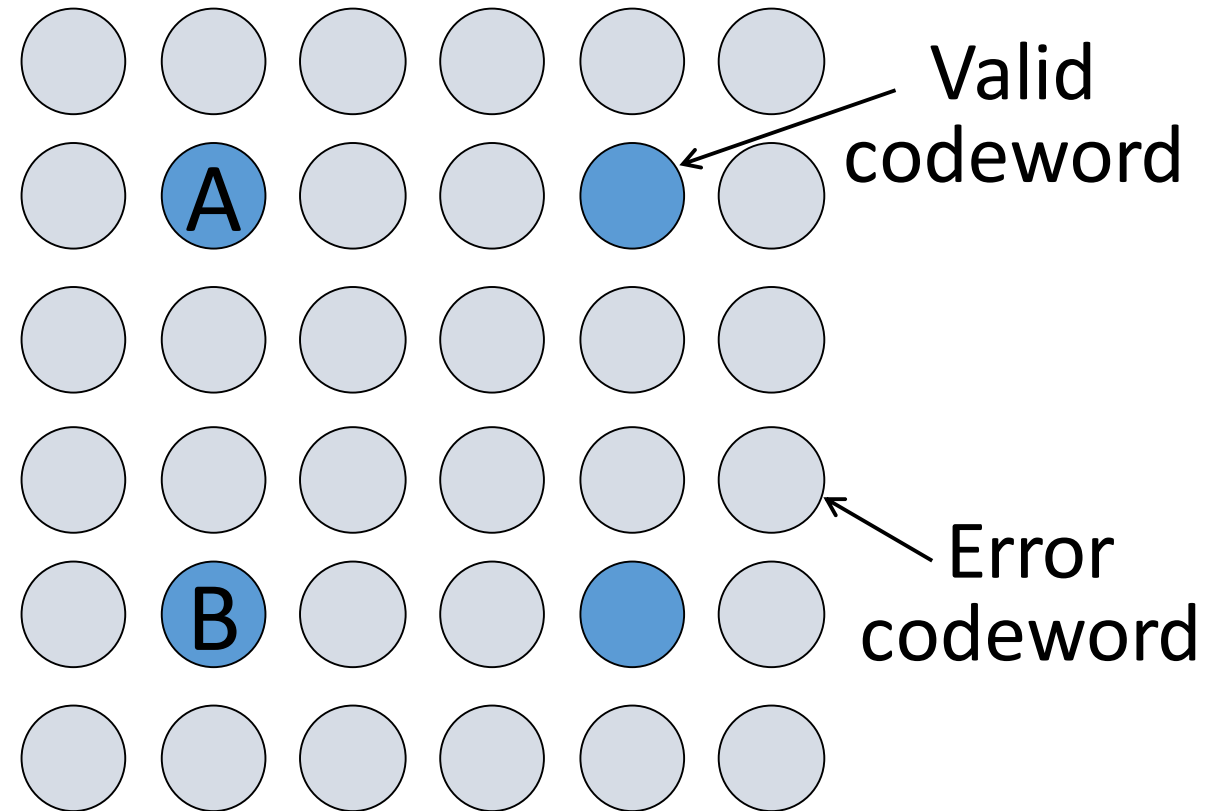
- If we had reliable check bits we could use them to narrow down the position of the error
  - Then correction would be easy
- But error could be in the check bits as well as the data bits!
  - Data might even be correct

# Intuition for Error Correcting Code

- Suppose we construct a code with a Hamming distance of at least 3
  - Need  $\geq 3$  bit errors to change one valid codeword into another
  - Single bit errors will be closest to a unique valid codeword
- If we assume errors are only 1 bit, we can correct them by mapping an error to the closest valid codeword
  - Works for  $d$  errors if  $HD \geq 2d + 1$

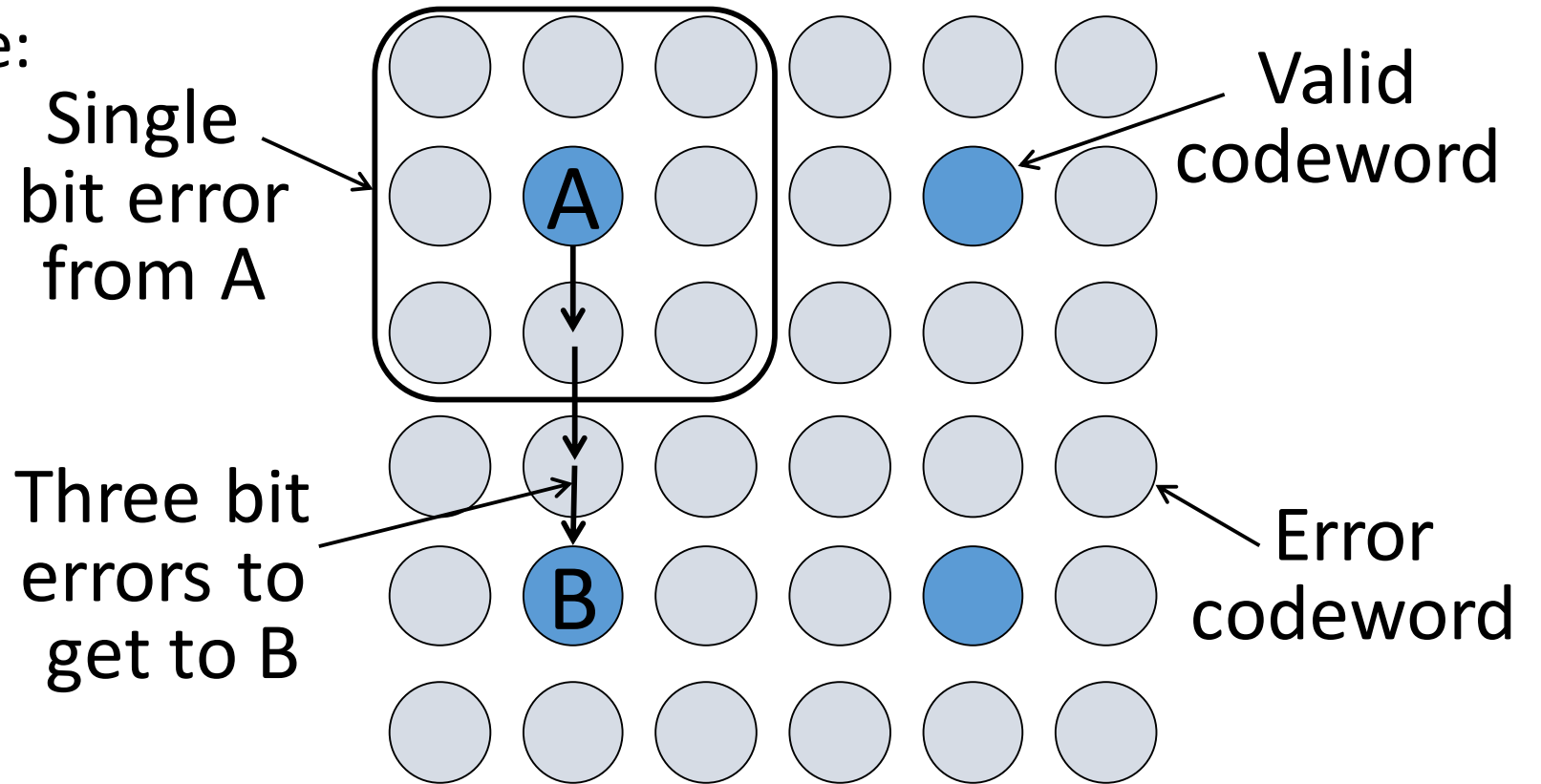
# Intuition

- Visualization of code:



# Intuition (3)

- Visualization of code:





# Hamming Code

- Gives a method for constructing a code with a distance of 3
  - Uses  $n = 2^k - k - 1$ , e.g.,  $n=4, k=3$
  - Put check bits in positions  $p$  that are powers of 2, starting with position 1
  - Check bit in position  $p$  is parity of positions with a  $p$  term in their values
- Plus an easy way to correct

# Hamming Code (2)

- Example: data=0101, 3 check bits
  - 7 bit code, check bit positions 1, 2, 4
  - Check 1 covers positions 1, 3, 5, 7
  - Check 2 covers positions 2, 3, 6, 7
  - Check 4 covers positions 4, 5, 6, 7

1 2 3 4 5 6 7

# Hamming Code (3)

- Example: data=0101, 3 check bits
  - 7 bit code, check bit positions 1, 2, 4
  - Check 1 covers positions 1, 3, 5, 7
  - Check 2 covers positions 2, 3, 6, 7
  - Check 4 covers positions 4, 5, 6, 7

0 1 0 0 1 0 1     $\longrightarrow$   
1 2 3 4 5 6 7

$$p_1 = 0 + 1 + 1 = 0, \quad p_2 = 0 + 0 + 1 = 1, \quad p_4 = 1 + 0 + 1 = 0$$

# Hamming Code (4)

- To decode:
  - Recompute check bits (with parity sum including the check bit)
  - Arrange as a binary number
  - Value (syndrome) tells error position
  - Value of zero means no error
  - Otherwise, flip bit to correct

# Hamming Code (5)

- Example, continued

→ 0 1 0 0 1 0 1  
1 2 3 4 5 6 7

$p_1 =$

$p_2 =$

$p_4 =$

Syndrome =

Data =

# Hamming Code (6)

- Example, continued

→ 0 1 0 0 1 0 1  
1 2 3 4 5 6 7

$$p_1 = 0+0+1+1 = 0, \quad p_2 = 1+0+0+1 = 0,$$

$$p_4 = 0+1+0+1 = 0$$

Syndrome = 000, no error

Data = 0 1 0 1

# Hamming Code (7)

- Example, continued

→ 0 1 0 0 1 **1** 1  
1 2 3 4 5 6 7

$p_1 =$

$p_2 =$

$p_4 =$

Syndrome =

Data =

# Hamming Code (8)

- Example, continued

→ 0 1 0 0 1 **1** 1  
1 2 3 4 5 6 7

$$p_1 = 0+0+1+1 = 0, \quad p_2 = 1+0+\mathbf{1}+1 = \mathbf{1},$$

$$p_4 = 0+1+\mathbf{1}+1 = \mathbf{1}$$

Syndrome = **1 1** 0, flip position 6

Data = 0 1 0 1 (correct after flip!)



# Other Error Correction Codes

- Codes used in practice are more involved than Hamming
- Convolutional codes (§3.2.3)
  - Take a stream of data and output a mix of the input bits
  - Makes each output bit less fragile
  - Decode using Viterbi algorithm (which can use bit confidence values)