

# Hierarchical Modeling

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CSE 457  
Autumn 2017

## Reading

Optional:

- Angel, sections 8.1 – 8.6, 8.8

Further reading:

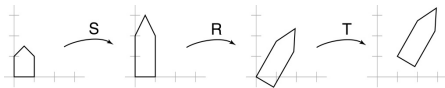
- *OpenGL Programming Guide*, chapter 3

## Symbols and instances

Most graphics APIs support a few geometric primitives:

- spheres
- cubes
- cylinders

These symbols are **instanced** using an **instance transformation**.



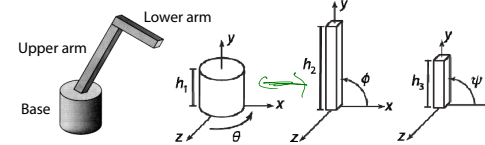
Q: What is the matrix for the instance transformation above?

$$TRS \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

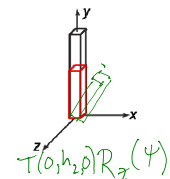
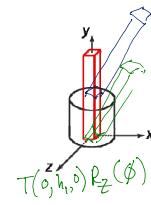
## 3D Example: A robot arm

Let's build a robot arm out of a cylinder and two cuboids, with the following 3 degrees of freedom:

- Base rotates about its vertical axis by  $\theta$
- Upper arm rotates in its  $xy$ -plane by  $\phi$
- Lower arm rotates in its  $xy$ -plane by  $\psi$



[Angel, 2011]



(Note that the angles are set to zero in the figures on the right; i.e., the parts are shown in their "default" positions.)

Suppose we have transformations  $R_x(\cdot), R_y(\cdot), R_z(\cdot), T(\cdot, \cdot, \cdot)$ .

Q: What matrix do we use to transform the base?

Q: What matrix product for the upper arm?

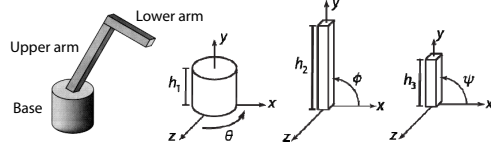
Q: What matrix product for the lower arm?

$$R_z(\theta) T(0, h_1, 0) R_z(\theta) T(0, h_2, 0) R_z(\psi)$$

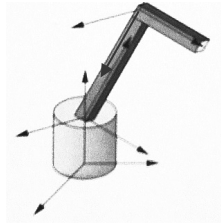
Handwritten annotations: "base" under the first T, "VA" under the first R\_z, and "LA" under the second R\_z.

### 3D Example: A robot arm

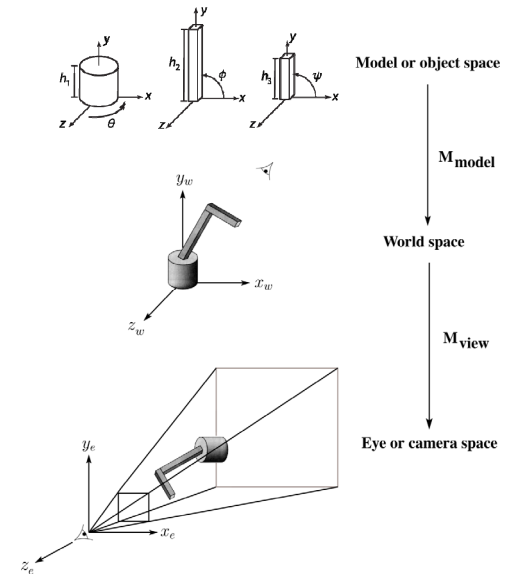
An alternative interpretation is that we are taking the original coordinate frames...



...and translating and rotating them into place:



### From parts to model to viewer



### Robot arm implementation

The robot arm can be displayed by keeping a global matrix and computing it at each step:

Matrix  $M$ ,  $M\_model$ ,  $M\_view$ ;

```
main()
{
    . . .
    M_view = compute_view_transform();
    robot_arm();
    . . .
}

robot_arm()
{
    M_model = R_y(theta);
    M = M_view*M_model;
    base();
    M_model = R_y(theta)*T(0,h1,0)*R_z(phi);
    M = M_view*M_model;
    upper_arm();
    M_model = R_y(theta)*T(0,h1,0)*R_z(phi)*T(0,h2,0)*R_z(psi);
    M = M_view*M_model;
    lower_arm();
}
```

Do the matrix computations seem wasteful?

### Robot arm implementation, better

Instead of recalculating the global matrix each time, we can just update it *in place* by concatenating matrices on the right:

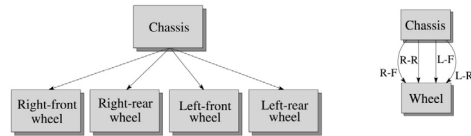
```
Matrix M_modelview;

main()
{
    . . .
    M_modelview = compute_view_transform();
    robot_arm();
    . . .
}

robot_arm()
{
    M_modelview *= R_y(theta);
    base();
    M_modelview *= T(0,h1,0)*R_z(phi);
    upper_arm();
    M_modelview *= T(0,h2,0)*R_z(psi);
    lower_arm();
}
```

## Hierarchical modeling

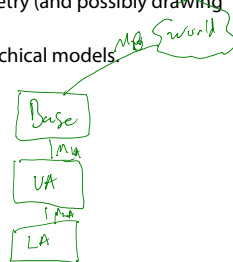
Hierarchical models can be composed of instances using trees or DAGs:



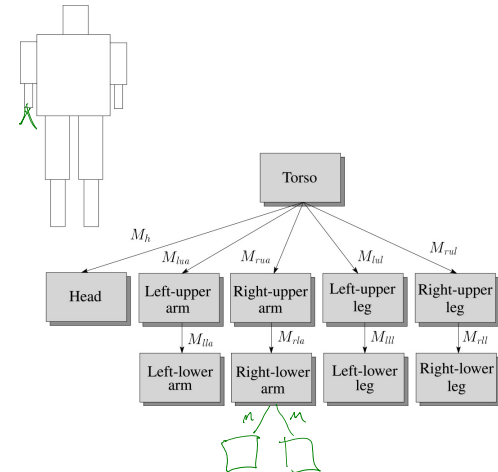
- edges contain geometric transformations
- nodes contain geometry (and possibly drawing attributes)

We will use trees for hierarchical models.

How might we draw the tree for the robot arm?



## A complex example: human figure

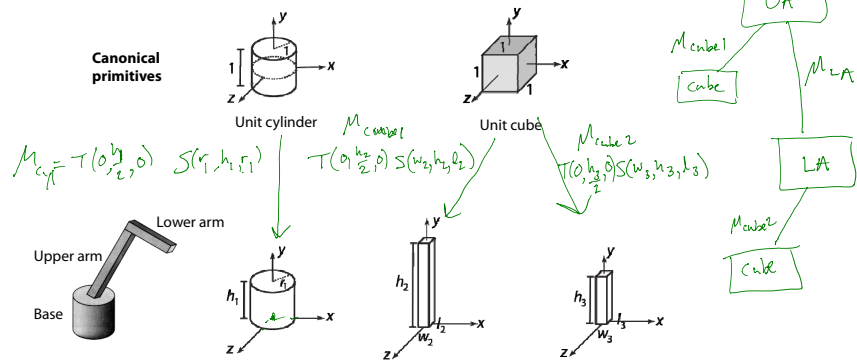


Q: What's the most sensible way to traverse this tree?  
*depth first traversal*      *Stack*

## Using canonical primitives

Consider building the robot arm again, but this time the building blocks are canonical primitives like a unit cylinder and a unit cube.

What additional transformations are needed?  
 What does the hierarchy look like now?



## Animation

The above examples are called **articulated models**:

- rigid parts
- connected by joints

They can be animated by specifying the joint angles (or other display parameters) as functions of time.

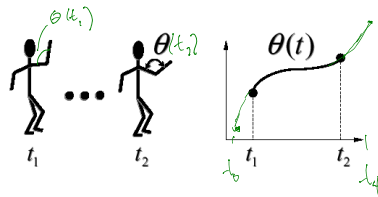
## Key-frame animation

The most common method for character animation in production is **key-frame animation**.

- ◆ Each joint specified at various **key frames** (not necessarily the same as other joints)
- ◆ System does interpolation or **in-betweening**

Doing this well requires:

- ◆ A way of smoothly interpolating key frames: **splines**
- ◆ A good interactive system
- ◆ A lot of skill on the part of the animator



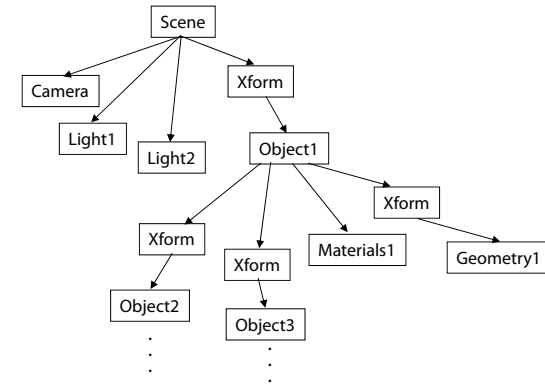
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## Scene graphs

The idea of hierarchical modeling can be extended to an entire scene, encompassing:

- ◆ many different objects
- ◆ lights
- ◆ camera position

This is called a **scene tree** or **scene graph**.



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## Summary

Here's what you should take home from this lecture:

- ◆ All the **boldfaced terms**.
- ◆ How primitives can be instantiated and composed to create hierarchical models using geometric transforms.
- ◆ How the notion of a model tree or DAG can be extended to entire scenes.
- ◆ How OpenGL transformations can be used in hierarchical modeling.
- ◆ How keyframe animation works.

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