Hierarchical Modeling

CSE 457
Required:
  • Angel, sections 8.1 – 8.6, 8.8

Optional:
  • *OpenGL Programming Guide*, chapter 3
Symbols and instances

Most graphics APIs support a few geometric primitives:

- spheres
- cubes
- cylinders

These symbols are instanced using an instance transformation.

Q: What is the matrix for the instance transformation above?
3D Example: A robot arm

Have to be constrained via a hierarchical model
“Number One” Playgroup – Duran Duboi
3D Example: A robot arm

Consider this robot arm with 3 degrees of freedom:

- Base rotates about its vertical axis by $\theta$
- Upper arm rotates in its $xy$-plane by $\phi$
- Lower arm rotates in its $xy$-plane by $\psi$

(Note that the angles are set to zero in the figure; i.e., the parts are shown in their “default” positions.)

Q: What matrix do we use to transform the base?

Q: What matrix for the upper arm?

Q: What matrix for the lower arm?
3D Example: A robot arm

An alternative interpretation is that we are taking the original coordinate frames...

...and translating and rotating them into place:
From parts to model to viewer

Model or object space

World space

Eye or camera space
Robot arm implementation

The robot arm can be displayed by keeping a global matrix and computing it at each step:

```c
Matrix M_model;
Matrix M_view;

main()
{
    . . .
    M_view = compute_view_transform();
    robot_arm();
    . . .
}

robot_arm()
{
    M_model = M_view*R_y(theta);
    base();
    M_model = M_view*R_y(theta)*T(0,h1,0)*R_z(phi);
    upper_arm();
    M_model = M_view*R_y(theta)*T(0,h1,0)*R_z(phi)*T(0,h2,0)*R_z(psi);
    lower_arm();
}
```

Do the matrix computations seem wasteful?
Instead of recalculating the global matrix each time, we can just update it \textit{in place} by concatenating matrices on the right:

Matrix $M_{\text{modelview}}$;

```c
main()
{
   . . .
   $M_{\text{modelview}} = \text{compute_view_transform}()$;
   robot_arm();
   . . .
}

robot_arm()
{
   $M_{\text{modelview}} = R_y(\theta)$;
   base();
   $M_{\text{modelview}} = T(0,h1,0)*R_z(\phi)$;
   upper_arm();
   $M_{\text{modelview}} = T(0,h2,0)*R_z(\psi)$;
   lower_arm();
}
```
Robot arm implementation, OpenGL

OpenGL maintains a global state matrix called the **model-view matrix**, which is updated by concatenating matrices on the *right*.

```c
main()
{
    . . .
    glMatrixMode( GL_MODELVIEW );
    Matrix M = compute_view_xform();
    glLoadMatrixf( M );
    robot_arm();
    . . .
}

robot_arm()
{
    glRotatef( theta, 0.0, 1.0, 0.0 );
    base();
    glTranslatef( 0.0, h1, 0.0 );
    glRotatef( phi, 0.0, 0.0, 1.0 );
    lower_arm();
    glTranslatef( 0.0, h2, 0.0 );
    glRotatef( psi, 0.0, 0.0, 1.0 );
    upper_arm();
}
```
Hierarchical modeling

Hierarchical models can be composed of instances using trees or DAGs:

- edges contain geometric transformations
- nodes contain geometry (and possibly drawing attributes)

How might we draw the tree for the robot arm?
Q: What’s the most sensible way to traverse this tree?
Implementing hierarchies:

A matrix stack that you can push/pop (LIFO).

Recursive algorithm that descends the model tree:
- Load identity matrix
- For each node:
  - Push a new matrix onto stack
  - Concatenate transformations onto current
  - Recursively descend the tree
  - Pop matrix out of stack
- For each leaf node:
  - Draw using the current transformation matrix
figure()
{
    torso();
    glPushMatrix();
    glTranslatef( ... );
    glRotatef( ... );
    head();
    glPopMatrix();
    glPushMatrix();
    glTranslatef( ... );
    glRotatef( ... );
    left_upper_arm();
    glPushMatrix();
    glTranslatef( ... );
    glRotatef( ... );
    left_lower_arm();
    glPopMatrix();
    glPopMatrix();
    . . .
}
Animation

The above examples are called articulated models:

- rigid parts
- connected by joints

They can be animated by specifying the joint angles (or other display parameters) as functions of time.
Key-frame animation

The most common method for character animation in production is **key-frame animation**.

- Each joint specified at various **key frames** (not necessarily the same as other joints)
- System does interpolation or **in-betweening**

Doing this well requires:

- A way of smoothly interpolating key frames: **splines**
- A good interactive system
- A lot of skill on the part of the animator
Scene graphs

The idea of hierarchical modeling can be extended to an entire scene, encompassing:

- many different objects
- lights
- camera position

This is called a **scene tree** or **scene graph**.

![Scene graph diagram]
Summary

Here’s what you should take home from this lecture:

- All the **boldfaced terms**.
- How primitives can be instanced and composed to create hierarchical models using geometric transforms.
- How the notion of a model tree or DAG can be extended to entire scenes.
- How OpenGL transformations can be used in hierarchical modeling.
- How keyframe animation works.