

# Texture Mapping

CSE 457  
Winter 2014

## Reading

### Required

- ♦ Angel, 7.4-7.10

### Recommended

- ♦ Paul S. Heckbert. Survey of texture mapping. **IEEE Computer Graphics and Applications** 6(11): 56–67, November 1986.

### Optional

- ♦ Woo, Neider, & Davis, Chapter 9
- ♦ James F. Blinn and Martin E. Newell. Texture and reflection in computer generated images. **Communications of the ACM** 19(10): 542–547, October 1976.

## Texture mapping



Texture mapping (Woo et al., fig. 9-1)

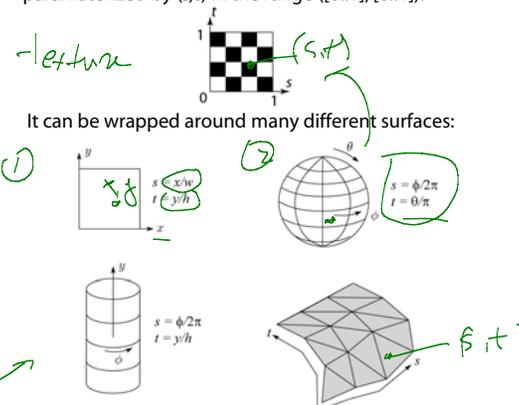
Texture mapping allows you to take a simple polygon and give it the appearance of something much more complex.

- ♦ Due to Ed Catmull, PhD thesis, 1974
- ♦ Refined by Blinn & Newell, 1976

A texture can modulate just about any parameter – diffuse color, specular color, specular exponent, ...

## Implementing texture mapping

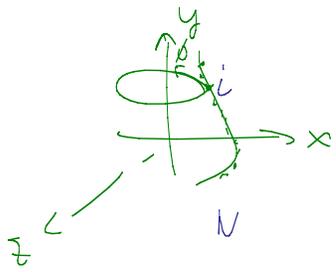
A texture lives in its own abstract image coordinates parameterized by  $(s,t)$  in the range  $([0..1], [0..1])$ :



With a ray caster, we can do the sphere and cylinder mappings directly (as we will see later). For z-buffers, everything gets converted to a triangle mesh with associated  $(s,t)$  coordinates.

Note: if the surface moves/deforms, the texture goes with it.

### Texture coordinates on a surface of revolution



$$s = \phi / 2\pi$$

$$t = i / N \quad v = \# \text{ samples}$$

$$t = \frac{\sum_{j=1}^i d_{j,j-1}}{\sum_{j=1}^N d_{j,j-1}}$$

Do this

arc length parametriz.

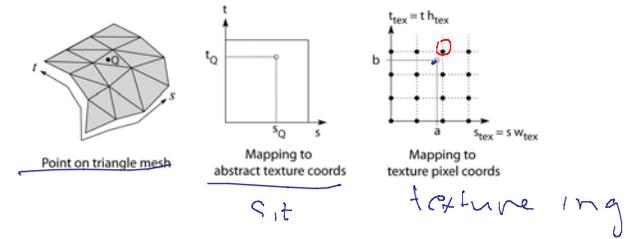
### Mapping to texture image coords

The texture is usually stored as an image. Thus, we need to convert from abstract texture coordinate:

$(s, t)$  in the range  $([0..1], [0..1])$

to texture image coordinates:

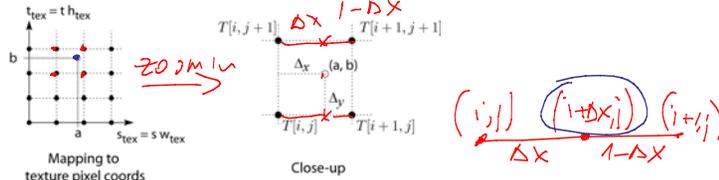
$(s_{tex}, t_{tex})$  in the range  $([0..w_{tex}], [0..h_{tex}])$



Q: What do you do when the texture sample you need lands between texture pixels?

### Texture resampling

We need to resample the texture:



Thus, we seek to solve for:  $T(a, b) = T(i + \Delta_x, j + \Delta_y)$

A common choice is **bilinear interpolation**:

$$T(i + \Delta_x, j) = (1 - \Delta_x) T(i, j) + \Delta_x T(i + 1, j)$$

$$T(i + \Delta_x, j + 1) = (1 - \Delta_x) T(i, j + 1) + \Delta_x T(i + 1, j + 1)$$

$$T(i + \Delta_x, j + \Delta_y) = (1 - \Delta_y) T(i + \Delta_x, j) + \Delta_y T(i + \Delta_x, j + 1)$$

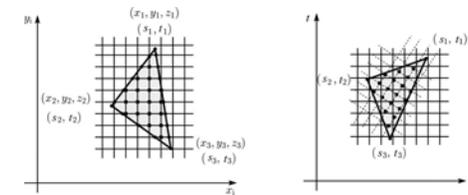
$$= (1 - \Delta_x)(1 - \Delta_y) T(i, j) + \Delta_x(1 - \Delta_y) T(i + 1, j) + (1 - \Delta_y)\Delta_y T(i, j + 1) + \Delta_x\Delta_y T(i + 1, j + 1)$$

### Texture mapping and the z-buffer

Texture-mapping can also be handled in z-buffer algorithms.

Method:

- Scan conversion is done in screen space, as usual
- Each pixel is colored according to the texture
- Texture coordinates are found by Gouraud-style interpolation

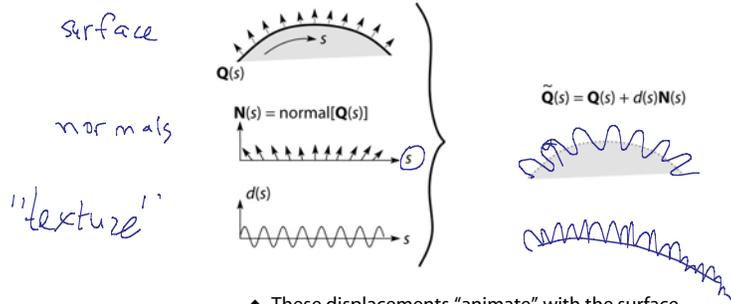


Note: Mapping is more complicated to handle perspective correctly!

## Displacement mapping

Textures can be used for more than just color.

In **displacement mapping**, a texture is used to perturb the surface geometry itself. Here's the idea in 2D:



- These displacements "animate" with the surface
- In 3D, you would of course have (s,t) parameters instead of just s.

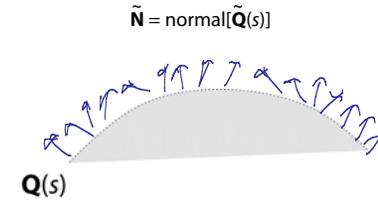
Suppose  $Q$  is a simple surface, like a cube. Will it take more work to render the modified surface  $\tilde{Q}$ ?

9

## Bump mapping

In **bump mapping**, a texture is used to perturb the normal:

- Use the original, simpler geometry,  $Q(s)$ , for hidden surfaces
- Use the normal from the displacement map for shading:



→ What artifacts in the images would reveal that bump mapping is a fake?

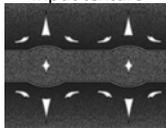
no silhouettes  
no occlusions

cast shadows  
perspective effects

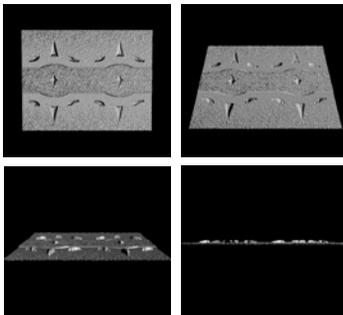
10

## Displacement vs. bump mapping

Input texture



Rendered as displacement map over a rectangular surface



11

## Displacement vs. bump mapping (cont'd)



Original rendering

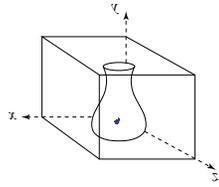
Rendering with bump map wrapped around a cylinder

Bump map and rendering by Wyvern Aldinger

12

## Solid textures

**Q:** What kinds of artifacts might you see from using a marble veneer instead of real marble?



One solution is to use **solid textures**:

- Use model-space coordinates to index into a 3D texture
- Like "carving" the object from the material

One difficulty of solid texturing is coming up with the textures.

13

## Solid textures (cont'd)

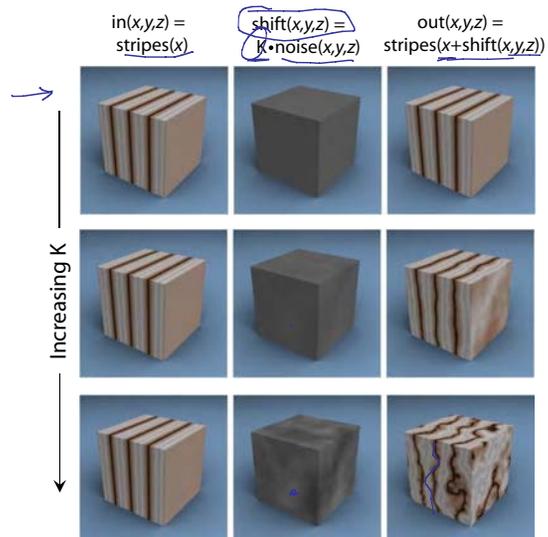
Here's an example for a vase cut from a solid marble texture:



*Solid marble texture by Ken Perlin, (Foley, IV-21)*

14

## Solid textures (cont'd)



15

## Environment mapping



In **environment mapping** (also known as **reflection mapping**), a texture is used to model an object's environment:

- Rays are bounced off objects into environment
- Color of the environment used to determine color of the illumination
- Environment mapping works well when there is just a single object – or in conjunction with ray tracing

This can be readily implemented (without interreflection) using a fragment shader, where the texture is stored in a "cube map" instead of a sphere.

With a ray tracer, the concept is easily extended to handle refraction as well as reflection (and interreflection).

16

## Summary

What to take home from this lecture:

1. The meaning of the boldfaced terms.
2. Familiarity with the various kinds of texture mapping, including their strengths and limitations.