

## Shading

1

## Reading

Required:

- ♦ Angel 6.1-6.5, 6.7-6.8

Optional:

- ♦ OpenGL red book, chapter 5.

2

## Introduction

So far, we've talked exclusively about geometry.

- ♦ What is the shape of an object?
- ♦ How do I place it in a virtual 3D space?
- ♦ How do I know which pixels it covers?
- ♦ How do I know which of the pixels I should actually draw?

Once we've answered all those, we have to ask one more important question:

- ♦ To what value do I set each pixel?

Answering this question is the job of the **shading model**.

Other names:

- ♦ Lighting model
- ♦ Light reflection model
- ♦ Local illumination model
- ♦ Reflectance model
- ♦ BRDF

3

## An abundance of photons

Properly determining the right color is *really hard*.

Look around the room. Each light source has different characteristics. Trillions of photons are pouring out every second.

These photons can:

- ♦ interact with the atmosphere, or with things in the atmosphere
- ♦ strike a surface and
  - be absorbed
  - be reflected (scattered)
  - cause fluorescence or phosphorescence.
- ♦ interact in a wavelength-dependent manner
- ♦ generally bounce around and around

4

## Our problem

We're going to build up to an *approximation* of reality called the **Phong illumination model**.

It has the following characteristics:

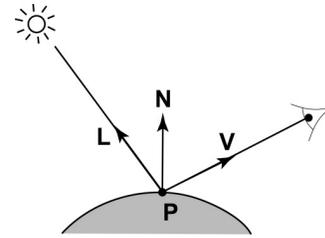
- ♦ *not* physically based
- ♦ gives a first-order *approximation* to physical light reflection
- ♦ very fast
- ♦ widely used

In addition, we will assume **local illumination**, i.e., light goes: light source -> surface -> viewer.

No interreflections, no shadows.

5

## Setup...



Given:

- ♦ a point **P** on a surface visible through pixel  $p$
- ♦ The normal **N** at **P**
- ♦ The lighting direction, **L**, and intensity,  $L$ , at **P**
- ♦ The viewing direction, **V**, at **P**
- ♦ The shading coefficients at **P**

Compute the color,  $I$ , of pixel  $p$ .

Assume that the direction vectors are normalized:

$$\|\mathbf{N}\| = \|\mathbf{L}\| = \|\mathbf{V}\| = 1$$

6

## "Iteration zero"

The simplest thing you can do is...

Assign each polygon a single color:

$$I = k_e$$

where

- ♦  $I$  is the resulting intensity
- ♦  $k_e$  is the **emissivity** or intrinsic shade associated with the object

This has some special-purpose uses, but not really good for drawing a scene.

[Note:  $k_e$  is omitted in Angel.]

7

## "Iteration one"

Let's make the color at least dependent on the overall quantity of light available in the scene:

$$I = k_e + k_a L_a$$

- ♦  $k_a$  is the **ambient reflection coefficient**.
  - really the reflectance of ambient light
  - "ambient" light is assumed to be equal in all directions
- ♦  $L_a$  is the **ambient light intensity**.

Physically, what is "ambient" light?

8

## Wavelength dependence

Really,  $k_e$ ,  $k_a$ , and  $L_a$  are functions over all wavelengths  $\lambda$ .

Ideally, we would do the calculation on these functions. For the ambient shading equation, we would start with:

$$I(\lambda) = k_a(\lambda)L_a(\lambda)$$

then we would find good RGB values to represent the spectrum  $I(\lambda)$ .

Traditionally, though,  $k_a$  and  $L_a$  are represented as RGB triples, and the computation is performed on each color channel separately:

$$I_R = k_{a,R} L_{a,R}$$

$$I_G = k_{a,G} L_{a,G}$$

$$I_B = k_{a,B} L_{a,B}$$

9

## Diffuse reflection

Let's examine the ambient shading model:

- ♦ objects have different colors
- ♦ we can control the overall light intensity
  - what happens when we turn off the lights?
  - what happens as the light intensity increases?
  - what happens if we change the color of the lights?

So far, objects are uniformly lit.

- ♦ not the way things really appear
- ♦ in reality, light sources are localized in position or direction

**Diffuse**, or **Lambertian** reflection will allow reflected intensity to vary with the direction of the light.

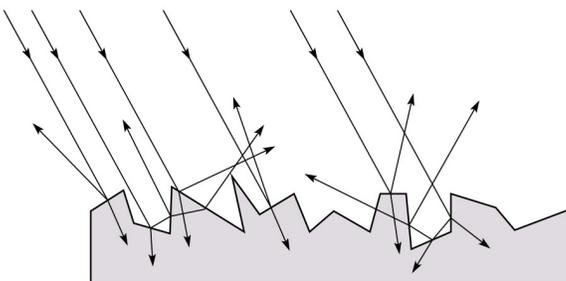
10

## Diffuse reflectors

Diffuse reflection occurs from dull, matte surfaces, like latex paint, or chalk.

These **diffuse** or **Lambertian** reflectors reradiate light equally in all directions.

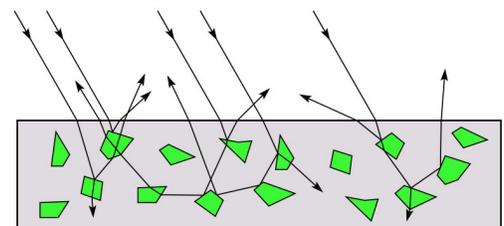
Picture a rough surface with lots of tiny **microfacets**.



11

## Diffuse reflectors

...or picture a surface with little pigment particles embedded beneath the surface (neglect reflection at the surface for the moment):



The microfacets and pigments distribute light rays in all directions.

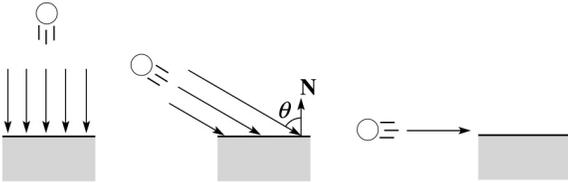
Embedded pigments are responsible for the coloration of diffusely reflected light in plastics and paints.

Note: the figures above are intuitive, but not strictly (physically) correct.

12

## Diffuse reflectors, cont.

The reflected intensity from a diffuse surface does not depend on the direction of the viewer. The incoming light, though, does depend on the direction of the light source:



13

## "Iteration two"

The incoming energy is proportional to \_\_\_\_\_, giving the diffuse reflection equations:

$$I = k_e + k_a L_a + k_d L \cos \theta$$

$$= k_e + k_a I_a + k_d L ( \cos \theta )$$

where:

- ♦  $k_d$  is the **diffuse reflection coefficient**
- ♦  $L$  is the intensity of the light source
- ♦  $\mathbf{N}$  is the normal to the surface (unit vector)
- ♦  $\mathbf{L}$  is the direction to the light source (unit vector)
- ♦  $(x)_+$  means  $\max\{0, x\}$

[Note: Angel uses  $L_d$  instead of  $L$ .]

14

## Specular reflection

**Specular reflection** accounts for the highlight that you see on some objects.

It is particularly important for *smooth, shiny* surfaces, such as:

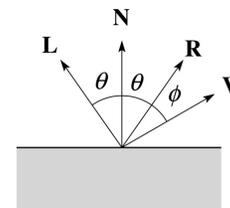
- ♦ metal
- ♦ polished stone
- ♦ plastics
- ♦ apples
- ♦ skin

Properties:

- ♦ Specular reflection depends on the viewing direction  $\mathbf{V}$ .
- ♦ For non-metals, the color is determined solely by the color of the light.
- ♦ For metals, the color may be altered (e.g., brass)

15

## Specular reflection "derivation"



For a perfect mirror reflector, light is reflected about  $\mathbf{N}$ , so

$$I = \begin{cases} L & \text{if } \mathbf{V} = \mathbf{R} \\ 0 & \text{otherwise} \end{cases}$$

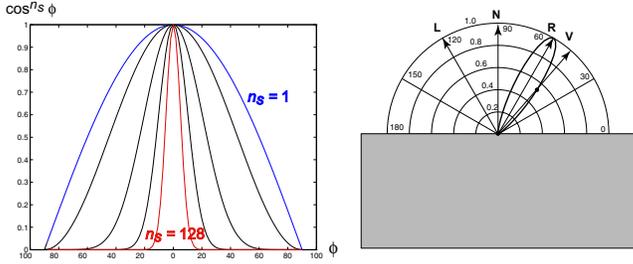
For a near-perfect reflector, you might expect the highlight to fall off quickly with increasing angle  $\phi$ .

Also known as:

- ♦ **"rough specular" reflection**
- ♦ **"directional diffuse" reflection**
- ♦ **"glossy" reflection**

16

## Derivation, cont.



One way to get this effect is to take  $(\mathbf{R} \cdot \mathbf{V})$ , raised to a power  $n_s$ .

As  $n_s$  gets larger,

- ♦ the dropoff becomes {more,less} gradual
- ♦ gives a {larger,smaller} highlight
- ♦ simulates a {more,less} mirror-like surface

17

## “Iteration three”

The next update to the Phong shading model is then:

$$I = k_e + k_a I_a + k_d L(\mathbf{N} \cdot \mathbf{L})_+ + k_s L(\mathbf{V} \cdot \mathbf{R})_+^{n_s}$$

where:

- ♦  $k_s$  is the **specular reflection coefficient**
- ♦  $n_s$  is the **specular exponent** or **shininess**
- ♦  $\mathbf{R}$  is the reflection of the light about the normal (unit vector)
- ♦  $\mathbf{V}$  is viewing direction (unit vector)

[Note: Angel uses  $\alpha$  instead of  $n_s$ , and maintains a separate  $L_d$  and  $L_s$ , instead of a single  $L$ . This choice reflects the flexibility available in OpenGL.]

18

## Lights

OpenGL supports different kinds of lights: point, directional, and spot.

For point light sources, the laws of physics state that the intensity of a point light source must drop off inversely with the square of the distance.

We can incorporate this effect by multiplying  $L$  by  $1/d^2$ .

Sometimes, this distance-squared dropoff is considered too “harsh.” A common alternative is:

$$\frac{1}{a + bd + cd^2}$$

with user-supplied constants for  $a$ ,  $b$ , and  $c$ .

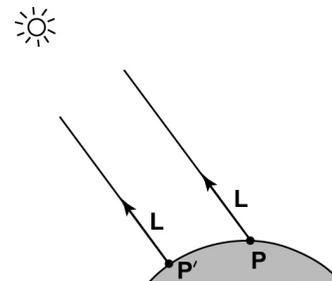
19

## Lights

OpenGL supports three different kinds of lights: ambient, directional, and point. Spot lights are also supported as a special form of point light.

We’ve seen ambient light sources, which are not really geometric.

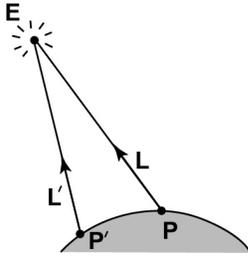
**Directional light** sources have a single direction and intensity associated with them.



20

## Point lights

The direction of a **point light** sources is determined by the vector from the light position to the surface point.



$$\mathbf{L} = \frac{\mathbf{E} - \mathbf{P}}{\|\mathbf{E} - \mathbf{P}\|}$$

$$d = \|\mathbf{E} - \mathbf{P}\|$$

Physics tells us the intensity must drop off inversely with the square of the distance:

$$f_{\text{atten}} = \frac{1}{d^2}$$

Sometimes, this distance-squared dropoff is considered too "harsh." A common alternative is:

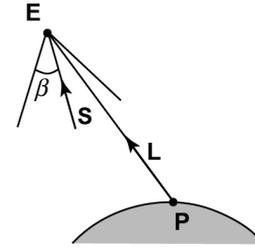
$$f_{\text{atten}} = \frac{1}{a + bd + cd^2}$$

with user-supplied constants for  $a$ ,  $b$ , and  $c$ .

21

## Spotlights

OpenGL also allows one to apply a *directional attenuation* of a point light source, giving a **spotlight** effect.



The spotlight intensity factor is computed in OpenGL as:

$$f_{\text{spot}} = (\mathbf{L} \cdot \mathbf{S})_{\beta}^e$$

where

- $\mathbf{L}$  is the direction to the point light.
- $\mathbf{S}$  is the center direction of the spotlight.
- $\beta$  is the cutoff angle for the spotlight
- $e$  is the angular falloff coefficient
- $(x)_{\beta}^e = [\max\{\cos(x) - \beta, 0\}]^e$

22

## "Iteration four"

Since light is additive, we can handle multiple lights by taking the sum over every light.

Our equation is now:

$$I = k_e + k_a L_a + \sum_j \frac{(\mathbf{L}_j \cdot \mathbf{S}_j)_{\beta_j}^{e_j}}{a + bd_j + cd_j^2} L_j \left[ k_d (\mathbf{N} \cdot \mathbf{L}_j)_+ + k_s (\mathbf{V} \cdot \mathbf{R}_j)_+^{n_s} \right]$$

This is the Phong illumination model.

Which quantities are spatial vectors?

Which are RGB triples?

Which are scalars?

23

## Choosing the parameters

Experiment with different parameter settings. To get you started, here are a few suggestions:

- Try  $n_s$  in the range  $[0, 100]$
- Try  $k_a + k_d + k_s < 1$
- Use a small  $k_a$  ( $\sim 0.1$ )

|         | $n_s$  | $k_d$                    | $k_s$                 |
|---------|--------|--------------------------|-----------------------|
| Metal   | large  | Small, color of metal    | Large, color of metal |
| Plastic | medium | Medium, color of plastic | Medium, white         |
| Planet  | 0      | varying                  | 0                     |

24

## Materials in OpenGL

The OpenGL code to specify the surface shading properties is fairly straightforward. For example:

```
GLfloat ke[] = { 0.1, 0.15, 0.05, 1.0 };
GLfloat ka[] = { 0.1, 0.15, 0.1, 1.0 };
GLfloat kd[] = { 0.3, 0.3, 0.2, 1.0 };
GLfloat ks[] = { 0.2, 0.2, 0.2, 1.0 };
GLfloat ns[] = { 50.0 };
glMaterialfv(GL_FRONT, GL_EMISSION, ke);
glMaterialfv(GL_FRONT, GL_AMBIENT, ka);
glMaterialfv(GL_FRONT, GL_DIFFUSE, kd);
glMaterialfv(GL_FRONT, GL_SPECULAR, ks);
glMaterialfv(GL_FRONT, GL_SHININESS, ns);
```

Notes:

- The `GL_FRONT` parameter tells OpenGL that we are specifying the materials for the front of the surface.
- Only the alpha value of the diffuse color is used for blending. It's usually set to 1.

25

## Shading in OpenGL

The OpenGL lighting model allows you to associate different lighting colors according to material properties they will influence.

Thus, our original shading equation:

$$I = k_e + k_a L_a + \sum_j \frac{(\mathbf{L}_j \cdot \mathbf{S}_j)^{e_j}}{a + b d_j + c d_j^2} L_j \left[ k_d (\mathbf{N} \cdot \mathbf{L}_j)_+ + k_s (\mathbf{V} \cdot \mathbf{R}_j)_+^{n_s} \right]$$

becomes:

$$I = k_e + k_a L_a + \sum_j \frac{(\mathbf{L}_j \cdot \mathbf{S}_j)^{e_j}}{a + b d_j + c d_j^2} L_j \left[ k_a L_{a_j} + k_d L_{d_j} (\mathbf{N} \cdot \mathbf{L}_j)_+ + k_s L_{s_j} (\mathbf{V} \cdot \mathbf{R}_j)_+^{n_s} \right]$$

where you can have a global ambient light with intensity  $L_a$  in addition to have an ambient light intensity  $L_{a_j}$  associated with each individual light.

26

## Shading in OpenGL, cont'd

In OpenGL this equation, for one light source (the 0<sup>th</sup>) is specified something like:

```
GLfloat La[] = { 0.2, 0.2, 0.2, 1.0 };
GLfloat La0[] = { 0.1, 0.1, 0.1, 1.0 };
GLfloat Ld0[] = { 1.0, 1.0, 1.0, 1.0 };
GLfloat Ls0[] = { 1.0, 1.0, 1.0, 1.0 };
GLfloat pos0[] = { 1.0, 1.0, 1.0, 0.0 };
GLfloat a0[] = { 1.0 };
GLfloat b0[] = { 0.5 };
GLfloat c0[] = { 0.25 };
GLfloat S0[] = { -1.0, -1.0, 0.0 };
GLfloat beta0[] = { 45 };
GLfloat e0[] = { 2 };

glLightModelfv(GL_LIGHT_MODEL_AMBIENT, La);
glLightfv(GL_LIGHT0, GL_AMBIENT, La0);
glLightfv(GL_LIGHT0, GL_DIFFUSE, Ld0);
glLightfv(GL_LIGHT0, GL_SPECULAR, Ls0);
glLightfv(GL_LIGHT0, GL_POSITION, pos0);
glLightfv(GL_LIGHT0, GL_CONSTANT_ATTENUATION, a0);
glLightfv(GL_LIGHT0, GL_LINEAR_ATTENUATION, b0);
glLightfv(GL_LIGHT0, GL_QUADRATIC_ATTENUATION, c0);
glLightfv(GL_LIGHT0, GL_SPOT_DIRECTION, S0);
glLightf(GL_LIGHT0, GL_SPOT_CUTOFF, beta0);
glLightf(GL_LIGHT0, GL_SPOT_EXPONENT, e0);
```

27

## Shading in OpenGL, cont'd

Notes:

You can have as many as `GL_MAX_LIGHTS` lights in a scene. This number is system-dependent.

For directional lights, you specify a light direction, not position, and the attenuation and spotlight terms are ignored.

The directions of directional lights and spotlights are specified in the coordinate systems *of the lights*, not the surface points as we've been doing in lecture.

28

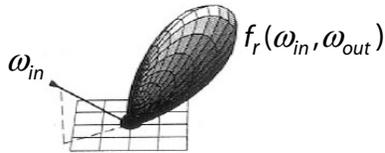
## BRDF

The Phong illumination model is really a function that maps light from incoming (light) directions  $\omega_{in}$  to outgoing (viewing) directions  $\omega_{out}$ :

$$f_r(\omega_{in}, \omega_{out})$$

This function is called the **Bi-directional Reflectance Distribution Function (BRDF)**.

Here's a plot with  $\omega_{in}$  held constant:

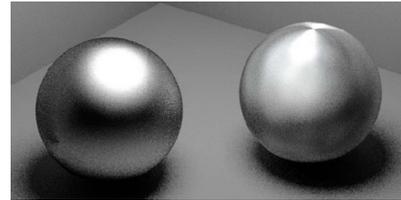
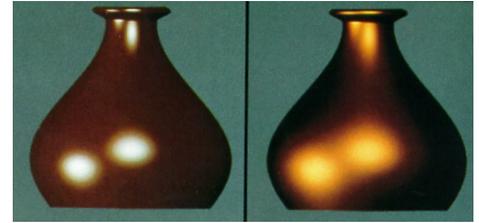


BRDF's can be quite sophisticated...

29

## More sophisticated BRDF's

Cook and Torrance, 1982



Westin, Arvo, Torrance 1992



30

## Gouraud vs. Phong interpolation

Now we know how to compute the color at a point on a surface using the Phong lighting model.

Does graphics hardware do this calculation at every point? Typically not (although this is changing)...

Smooth surfaces are often approximated by polygonal facets, because:

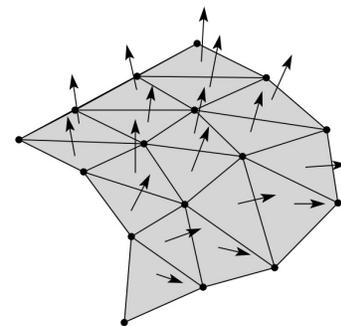
- ♦ Graphics hardware generally wants polygons (esp. triangles).
- ♦ Sometimes it easier to write ray-surface intersection algorithms for polygonal models.

How do we compute the shading for such a surface?

31

## Faceted shading

Assume each face has a constant normal:

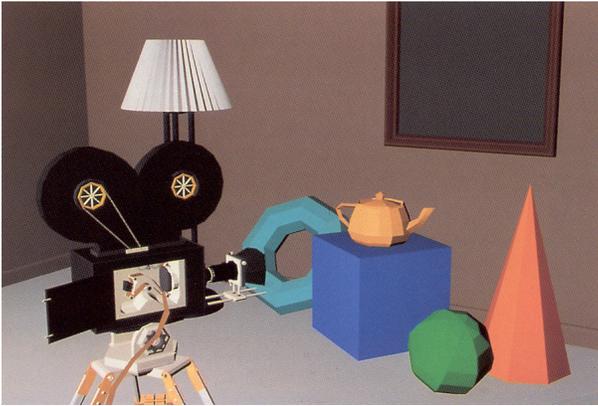


For a distant viewer and a distant light source, how will the color of each triangle vary?

Result: faceted, not smooth, appearance.

32

## Faceted shading (cont'd)



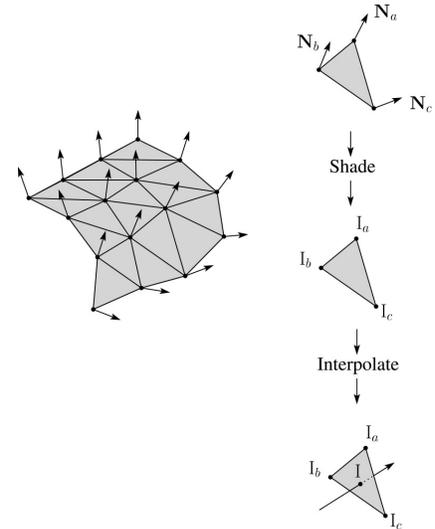
33

## Gouraud interpolation

To get a smoother result that is easily performed in hardware, we can do **Gouraud interpolation**.

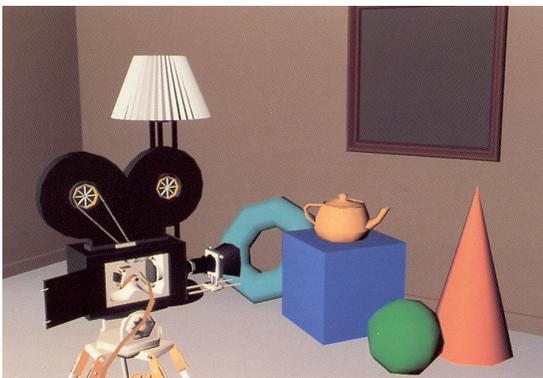
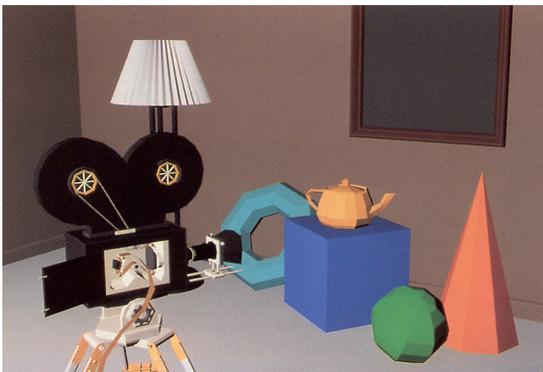
Here's how it works:

1. Compute normals at the vertices.
2. Shade only the vertices.
3. Interpolate the resulting vertex colors.



34

## Faced shading vs. Gouraud interpolation

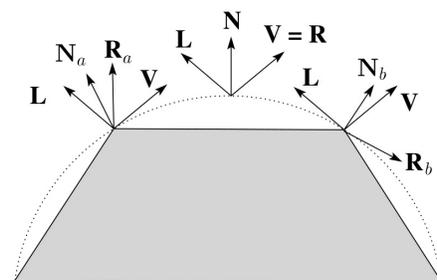


35

## Gouraud interpolation artifacts

Gouraud interpolation has significant limitations.

1. If the polygonal approximation is too coarse, we can miss specular highlights.



2. We will encounter **Mach banding** (derivative discontinuity enhanced by human eye).

Alas, this is usually what graphics hardware supports.

Maybe someday soon all graphics hardware will do...

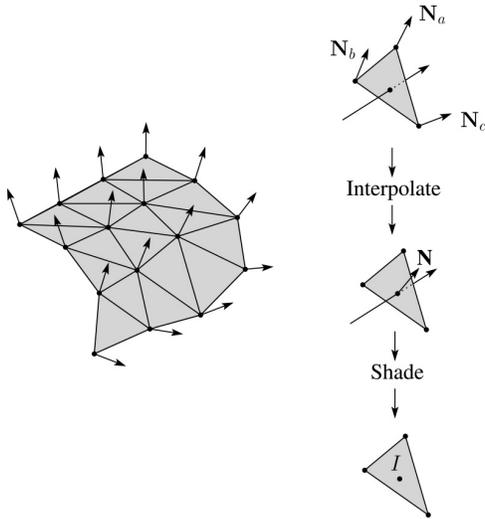
36

## Phong interpolation

To get an even smoother result with fewer artifacts, we can perform **Phong interpolation**.

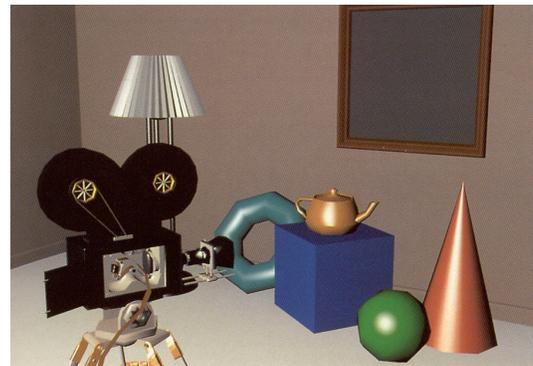
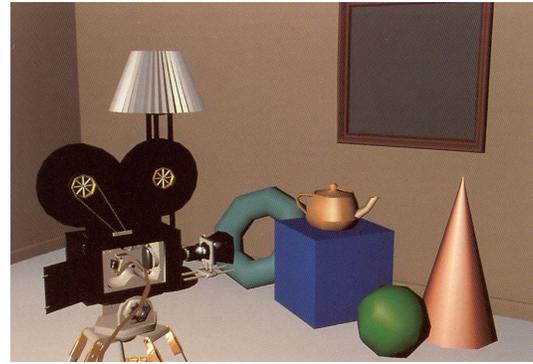
Here's how it works:

1. Compute normals at the vertices.
2. Interpolate normals and normalize.
3. Shade using the interpolated normals.



37

## Gouraud vs. Phong interpolation



38

## Summary

The most important thing to take away from this lecture is the equation for the Phong lighting model described in the "Iteration Four" slide.

- ♦ What is the physical meaning of each variable?
- ♦ How are the terms computed?
- ♦ What effect does each term contribute to the image?
- ♦ What does varying the parameters do?

You should also understand the differences between faceted, Gouraud, and Phong interpolated shading.

39