

Pixel anti-aliasing

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Surface reflection equation

To compute the reflection from a real surface, we would actually need to solve the surface reflection equation:

$$I(\omega_{out}) = \int_{H} I(\omega_{in}) f_r(\omega_{in}, \omega_{out}) d\omega_{in}$$

For a directional light with intensity L_1 coming from direction direction, ω_1 , we can view the remaining directions as contributing zero, giving: $I(\omega_{out}) = L_1 f_r(\omega_1, \omega_{out})$

We can plot the reflected light as a function of viewing angle for multiple light source contributions:



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Reflection anti-aliasing



Simulating gloss and translucency

The mirror-like form of reflection, when used to approximate glossy surfaces, introduces a kind of aliasing, because we are undersampling reflection (and refraction). R

For example:



Distributing rays over reflection directions gives:



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Full anti-aliasing



Full anti-aliasing...lots of nested integrals!

Computing these integrals is prohibitively expensive, especially after following the rays recursively.

We'll look at ways to approximate highdimensional integrals...

Summing over ray paths

We can think of this problem in terms of enumerated rays:



The intensity at a pixel is the sum over the primary rays: 1^{n}

$$I_{pixel} = \frac{1}{n} \sum_{i}^{n} I(r_i)$$

For a given primary ray, its intensity depends on secondary rays:

$$I(r_i) = \sum_j I(r_{ij}) f_r(r_{ij} \to r_i)$$

Substituting back in:

$$I_{pixel} = \frac{1}{n} \sum_{i} \sum_{j} I(r_{ij}) f_r(r_{ij} \rightarrow r_i)$$

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Whitted integration

An anti-aliased Whitted ray tracer chooses very specific paths, i.e., paths starting on a regular subpixel grid with only perfect reflections (and refractions) that terminate at the light source.



One problem with this approach is that it doesn't account for non-mirror reflection at surfaces.

Summing over ray paths



We can incorporate tertiary rays next:

$$I_{pixel} = \frac{1}{n} \sum_{i} \sum_{j} \sum_{k} I(r_{ijk}) f_r(r_{ijk} \rightarrow r_{ij}) f_r(r_{ij} \rightarrow r_i)$$

Each triple i,j,k corresponds to a ray path:

$$r_{ijk} \rightarrow r_{ij} \rightarrow r_{ij}$$

So, we can see that ray tracing is a way to approximate a complex, nested light transport integral with a summation over ray paths (of arbitrary length!).

Problem: too expensive to sum over all paths.

Solution: choose a small number of "good" paths.

Monte Carlo path tracing

Instead, we could choose paths starting from random sub-pixel locations with completely random decisions about reflection (and refraction). This approach is called **Monte Carlo path tracing** [Kajiya86].



The advantage of this approach is that the answer is known to be unbiased and will converge to the right answer.

Importance sampling

The disadvantage of the completely random generation of rays is the fact that it samples unimportant paths and neglects important ones.

This means that you need a lot of rays to converge to a good answer.

The solution is to re-inject Whitted-like ideas: spawn rays to the light, and spawn rays that **favor** the specular direction.



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Distribution ray tracing

These ideas can be combined to give a particular method called **distribution ray tracing** [Cook84]:

- uses non-uniform (jittered) samples.
- replaces aliasing artifacts with noise.
- provides additional effects by distributing rays to sample:
 - Reflections and refractions
 - · Light source area
 - · Camera lens area
 - Time

[Originally called "distributed ray tracing," but we will call it distribution ray tracing so as not to confuse with parallel computing.]

Stratified sampling

Another method that gives faster convergence is **stratified sampling**.

E.g., for sub-pixel samples:



We call this a **jittered** sampling pattern.

One interesting side effect of these stochastic sampling patterns is that they actually injects noise into the solution (slightly grainier images). This noise tends to be less objectionable than aliasing artifacts.

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DRT pseudocode

TraceImage() looks basically the same, except now each pixel records the average color of jittered sub-pixel rays.

function traceImage (scene):

for each pixel (i, j) in image do

 $I(i, j) \leftarrow 0$

for each sub-pixel id in (i,j) do

 $\mathbf{s} \leftarrow pixelToWorld(jitter(i, j, id))$

 $\mathbf{p} \leftarrow \mathbf{COP}$

 $\mathbf{d} \leftarrow (\mathbf{s} - \mathbf{p}).normalize()$

 $I(i, j) \leftarrow I(i, j) + traceRay(scene, p, d, id)$

end for

 $I(i, j) \leftarrow I(i, j)/numSubPixels$

end for

end function

A typical choice is numSubPixels = 5*5.

DRT pseudocode (cont'd)

Now consider traceRay(), modified to handle opaque glossy surfaces:

function traceRay(scene, p, d, id):

- $(\mathbf{q}, \mathbf{N}, \text{material}) \leftarrow intersect (\text{scene}, \mathbf{p}, \mathbf{d})$ $I \leftarrow shade(...)$ **R** ← *jitteredReflectDirection*(material, **N**, -**d**, id) $I \leftarrow I + material.k_r * traceRay(scene, q, R, id)$
- return I

end function



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Soft shadows



Distributing rays over light source area gives:



Pre-sampling glossy reflections



The pinhole camera, revisited

Recall the pinhole camera:







Lenses

Pinhole cameras in the real world require small apertures to keep the image in focus.

Lenses focus a bundle of rays to one point => can have larger aperture.



For a "thin" lens, we can approximately calculate where an object point will be in focus using the the Gaussian lens formula:

$$\frac{1}{d_i} + \frac{1}{d_o} = \frac{1}{f}$$

where f is the focal length of the lens.

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Depth of field

Lenses do have some limitations.

The most noticeable is the fact that points that are not in the object plane will appear out of focus.

The depth of field is a measure of how far from the object plane points can be before appearing "too blurry."



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Simulating depth of field



Image plane

Plane in focus

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Distributing rays over a finite aperture gives:



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Chaining the ray id's

In general, you can trace rays through a scene and keep track of their id's to handle all of these effects:



DRT to simulate

Distributing rays over time gives:



Summary

What to take home from this lecture:

- The limitations of Whitted ray tracing.
- How distribution ray tracing works and what effects it can simulate.

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