#### **Image Processing**

CSE 457, Autumn 2003 Graphics

http://www.cs.washington.edu/education/courses/457/03au/

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Reading

5.4. in *Machine Vision*, Jain, Kasturi, Schunck.

• Sections 4.2-4.4, 4.5(intro), 4.5.5, 4.5.6, 5.1-

» on reserve in Engineering Library

#### \_

#### What is an image?

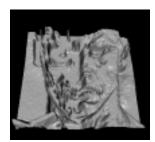
- We can think of an **image** as a function, f, from R<sup>2</sup> to R:
  - » f(x, y) gives the intensity of a channel at position (x, y)
  - » Realistically, we expect the image only to be defined over a rectangle, with a finite range:
    - $f: [a,b] \times [c,d] \rightarrow [0,1.0]$
- A color image is just three functions pasted together. We can write this as a "vector-valued" function:

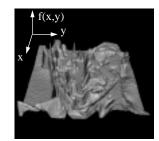
$$\vec{f}(x, y) = \begin{bmatrix} r(x, y) \\ g(x, y) \\ b(x, y) \end{bmatrix}$$

Images as functions









#### What is a digital image?

- In computer graphics, we usually operate on **digital** (**discrete**) images:
  - » Sample the space on a regular grid
  - » Quantize each sample (round to nearest integer)

If our samples are  $\Delta$  apart, we can write this as:





 $f[i,j] = \text{Quantize}\{f(i \Delta, j \Delta)\}$ 





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#### Image processing

- An **image processing** operation typically defines a new image *g* in terms of an existing image *f*.
- The simplest operations are those that transform each pixel in isolation. These pixel-to-pixel operations can be written as g(x,y)=t(f(x,y))
- Examples:
  - » threshold: emphasize a particular transition level
  - » RGB  $\rightarrow$  grayscale: extract the luminance for the pixel

A typical choice for mapping to grayscale is to apply the YIQ television matrix and keep the Y.

$$\begin{bmatrix} Y \\ I \\ Q \end{bmatrix} = \begin{bmatrix} 0.299 & 0.587 & 0.114 \\ 0.596 & -0.275 & -0.321 \\ 0.212 & -0.523 & 0.311 \end{bmatrix} * \begin{bmatrix} R \\ G \\ B \end{bmatrix}$$

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### single pixel changes



to grayscale









threshold at 128

#### Pixel movement

• Some operations preserve intensities, but move pixels around in the image  $g(x, y) = f(\tilde{x}(x, y), \tilde{y}(x, y))$ 



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example: image registration

#### more pixel movement effects



ripple



image transitions



reflection in ripples

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#### Noise

- Image processing is also useful for noise reduction
- Common types of noise:
  - » Salt and pepper noise: contains random occurrences of black and white pixels
  - » Impulse noise: contains random occurrences of white pixels
  - » Gaussian noise: variations in intensity drawn from a Gaussian normal distribution







Salt and pepper noise



Impulse noise



Gaussian noise

#### Ideal noise reduction



image 1



image 2



average



image 2



image 3





#### Practical noise reduction

• How can we "smooth" away noise in a single image?

• Is there a more abstract way to represent this sort of operation? Of course there is!

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#### Convolution

- One of the most common methods for filtering an image is called **convolution**.
- In 1D, convolution is defined as:

$$g(x) = f(x) * h(x)$$

$$= \int_{-\infty}^{\infty} f(x')h(x-x')dx'$$

$$= \int_{-\infty}^{\infty} f(x')\tilde{h}(x'-x)dx' \qquad \text{where } \tilde{h}(x) = h(-x)$$

g(x) is "f convolved with h":

evaluate the integral of  $f \cdot h$  with h flipped around the y-axis and centered at x

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#### Discrete convolution

• For a digital signal, we define **discrete convolution** as:

$$\begin{split} g[i] &= f[i] * h[i] \\ &= \sum_{j} f[j] h[i-j] \\ &= \sum_{j} f[j] \widetilde{h}[j-i] \end{split} \qquad \text{where } \widetilde{h}[i] = h[-i] \end{split}$$

g[i] is "f convolved with h":

evaluate the sum of  $f \cdot h$  with h flipped around the y-axis and centered at i cse457-04-image-processing © 2003 University of Washington

#### Convolution in 2D

In two dimensions, convolution becomes:

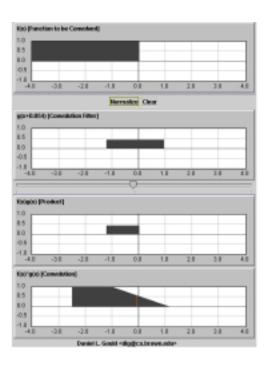
$$g(x,y) = f(x,y) * h(x,y)$$

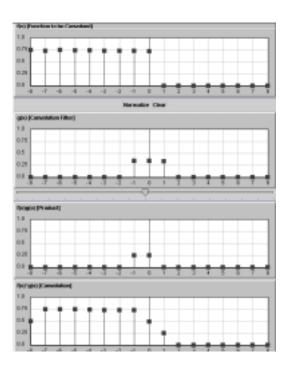
$$= \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} f(x',y')h(x-x',y-y')dx'dy'$$

$$= \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} f(x',y')\tilde{h}(x'-x,y'-y)dx'dy' \qquad \text{where } \tilde{h}(x,y) = h(-x,-y)$$

Similarly, discrete convolution in 2D becomes:

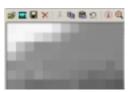
$$\begin{split} g[i,j] &= f[i,j] * h[i,j] \\ &= \sum_{k} \sum_{l} f[k,l] h[i-k,j-l] \\ &= \sum_{k} \sum_{l} f[k,l] \widetilde{h}[k-i,l-j] \\ \end{split} \quad \text{where } \widetilde{h}[i,j] = h[-i,-j]$$

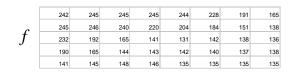


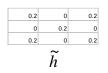


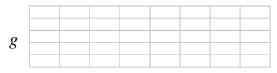
#### Convolution representation

• Since f, g, and  $\tilde{h}$  are defined over finite regions, we can write them out in two-dimensional arrays:









Note: This is not matrix multiplication!

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#### Mean filters

• How can we represent our noise-reducing averaging filter as a convolution diagram?

# Gaussian noise Salt and pepper noise 3x3

Effect of mean filters



5x5







#### Gaussian filters

Gaussian filters weigh pixels based on their distance from the center of the convolution filter. In particular:

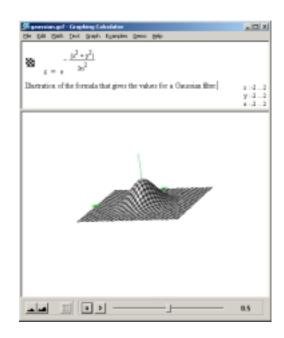
 $h[i, j] = \frac{e^{-(i^2 + j^2)/(2\sigma^2)}}{C}$ 

- This does a decent job of blurring noise while preserving features of the image.
- What parameter controls the width of the Gaussian?
- What happens to the image as the Gaussian filter kernel gets wider?
- What is the constant C? What should we set it to?

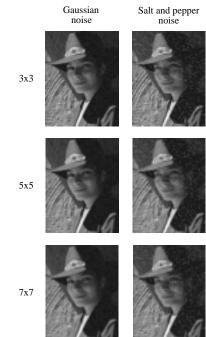
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Effect of Gaussian filters 5x5



#### Median filters

- A **Median Filter** operates over an *m*x*m* region by selecting the median intensity in the region.
- What advantage does a median filter have over a mean filter?
- Is a median filter a kind of convolution?

Effect of median filters



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Comparison:
Gaussian noise

7x7

Mean

Gaussian

Median

Comparison: salt and pepper noise

7x7

#### Edge detection

- One of the most important uses of image processing is **edge detection:** 
  - » Really easy for humans
  - » Really difficult for computers
  - » Fundamental in computer vision
  - » Important in many graphics applications

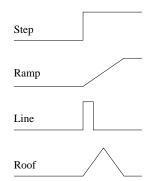
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#### What is an edge?



• **Q**: How might you detect an edge in 1D?

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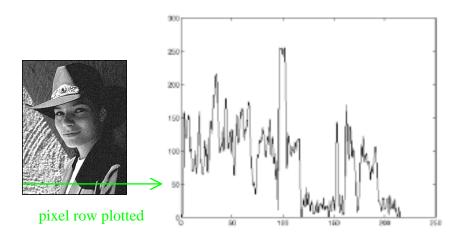
#### Gradients

• The **gradient** is the 2D equivalent of the derivative:

$$\nabla f(x, y) = \left(\frac{\partial f}{\partial x}, \frac{\partial f}{\partial y}\right)$$

- Properties of the gradient
  - » It's a vector
  - » Points in the direction of maximum increase of f
  - » Magnitude is rate of increase
- How can we approximate the gradient in a discrete image?

#### Less than ideal edges



#### Steps in edge detection

- Edge detection algorithms typically proceed in three or four steps:
  - » Filtering: cut down on noise
  - » Enhancement: amplify the difference between edges and non-edges
  - » **Detection**: use a threshold operation
  - » **Localization** (optional): estimate geometry of edges beyond pixels

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#### Edge enhancement

• A popular gradient magnitude computation is the **Sobel** operator:

$$S_x = \begin{bmatrix} -1 & 0 & 1 \\ -2 & 0 & 2 \\ -1 & 0 & 1 \end{bmatrix}$$

$$S_{x} = \begin{bmatrix} -1 & 0 & 1 \\ -2 & 0 & 2 \\ -1 & 0 & 1 \end{bmatrix} \qquad S_{y} = \begin{bmatrix} 1 & 2 & 1 \\ 0 & 0 & 0 \\ -1 & -2 & -1 \end{bmatrix}$$

• We can then compute the magnitude of the vector  $(s_r, s_v)$ .

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#### Results of Sobel edge detection







Magnitude

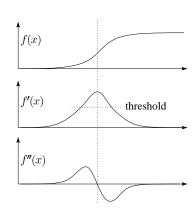




#### Second derivative operators

• The Sobel operator can produce thick edges. Ideally, we're looking for infinitely thin boundaries.

An alternative approach is to look for local extrema in the first derivative: places where the change in the gradient is highest.



**Q**: A peak in the first derivative corresponds to what in the second derivative?

#### Localization with the Laplacian

- An equivalent measure of the second derivative in 2D is the **Laplacian**:  $\nabla^2 f(x, y) = \frac{\partial^2 f}{\partial x^2} + \frac{\partial^2 f}{\partial y^2}$
- Using discrete difference equations, the Laplacian filter can be shown to be:

$$\Delta^2 = \begin{bmatrix} 0 & 1 & 0 \\ 1 & -4 & 1 \\ 0 & 1 & 0 \end{bmatrix}$$

Zero crossings of this filter correspond to positions of maximum gradient. These zero crossings can be used to localize edges.

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#### Localization with the Laplacian







Smoothed



Laplacian (+128)

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## Sharpening with the Laplacian



Original



Laplacian (+128)

Why does the sign make a difference?

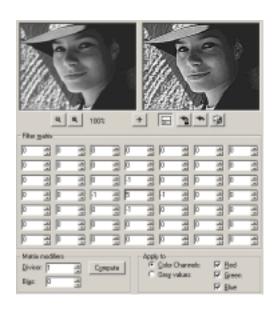
How can you write a filter that makes the bottom image?



Original + Laplacian



Original - Laplacian



#### **Summary**

- What you should take away from this lecture:
  - » The meanings of all the boldfaced terms.
  - » A richer understanding of the terms "image" and "image processing"
  - » How noise reduction is done
  - » How convolution filtering works
  - » The effect of mean, Gaussian, and median filters
  - » What an image gradient is and how it can be computed
  - » How edge detection is done
  - » What the Laplacian image is and how it is used in either edge detection or image sharpening

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