Lecture 7 Detectors and Descriptors

Slide Credit: Ranjay Krishna

Administrative

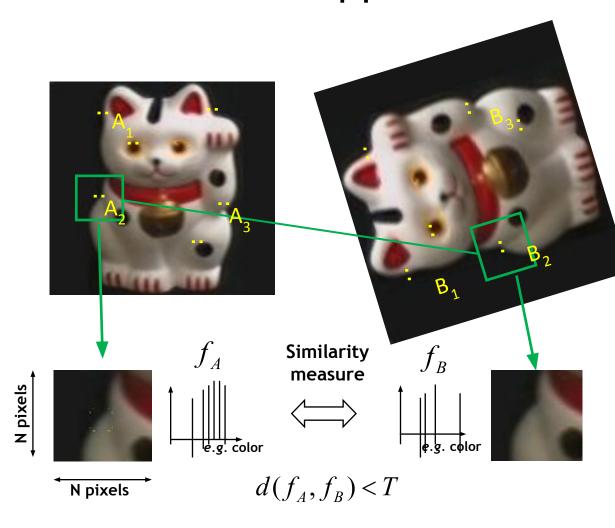
A1 was due on April 18th!!!

- You can use up to 2 late days

A2 is out

- Due May 2nd

So far: General approach for search



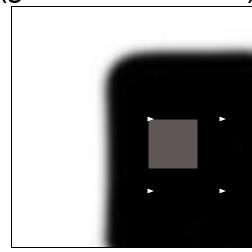
- 1. Find a set of distinctive key-points
- 2. Define a region/patch around each keypoint
- 3. Normalize the region content
- 4. Compute a local descriptor from the normalized region
- 5. Match local descriptors

So far: Corners as key-points

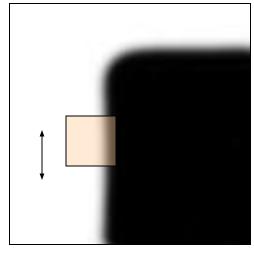
 We should easily recognize the corner point by looking through a small window (locality)

- Shifting the window in any direction should give a large change in intensity

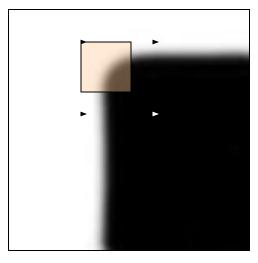
(good localization)



"flat" region: no change in all directions



"edge":
no change along
the edge direction



"corner": significant change in all directions

So far: Harris Corner Detector [Harris88]

 Compute second moment matrix (autocorrelation matrix)

$$M(\sigma_I, \sigma_D) = g(\sigma_I) * \begin{bmatrix} I_x^2(\sigma_D) & I_x I_y(\sigma_D) \\ I_x I_y(\sigma_D) & I_y^2(\sigma_D) \end{bmatrix}$$

 σ_D : for Gaussian in the derivative calculation σ_I : for Gaussian in the windowing function

1. Image derivatives

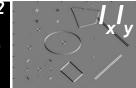












3. Gaussian filter $g(\sigma_i)$







4. Cornerness function - two strong eigenvalues

$$\theta = \det[M(\sigma_{I}, \sigma_{D})] - \alpha[\operatorname{trace}(M(\sigma_{I}, \sigma_{D}))]^{2}$$

$$= g(I_{x}^{2})g(I_{y}^{2}) - [g(I_{x}I_{y})]^{2} - \alpha[g(I_{x}^{2}) + g(I_{y}^{2})]^{2}$$

5. Perform non-maximum suppression

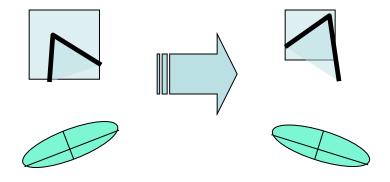


So far: Harris Detector Properties

Translation invariance?

So far: Harris Detector Properties

- Translation invariance
- Rotation invariance?

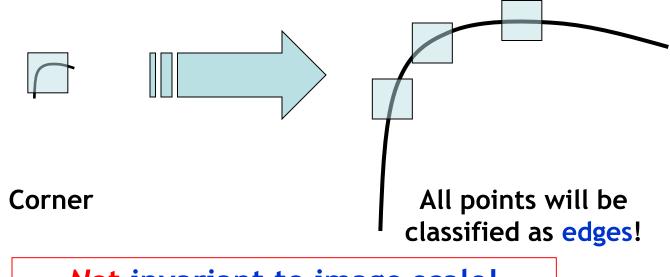


Ellipse rotates but its shape (i.e. eigenvalues) remains the same

Corner response θ is invariant to image rotation

So far: Harris Detector Properties

- Translation invariance
- Rotation invariance
- Scale invariance?



Not invariant to image scale!

Today's agenda

- Scale invariant keypoint detection
- Local detectors (SIFT)
- Local descriptors (SIFT)
- Global descriptors (HoG)

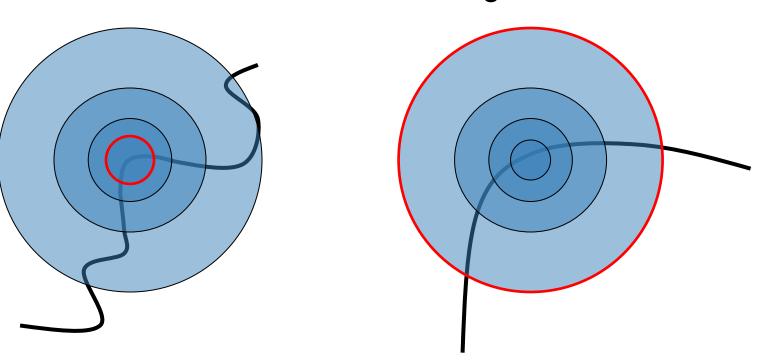
What will we learn today?

- Scale invariant keypoint detection
- Local detectors (SIFT)
- Local descriptors (SIFT)
- Global descriptors (HoG)

• Consider regions (e.g. circles) of different sizes around a point

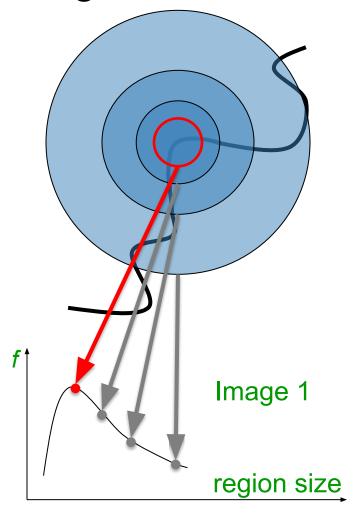
What region size do we choose, so that the regions look the same in both

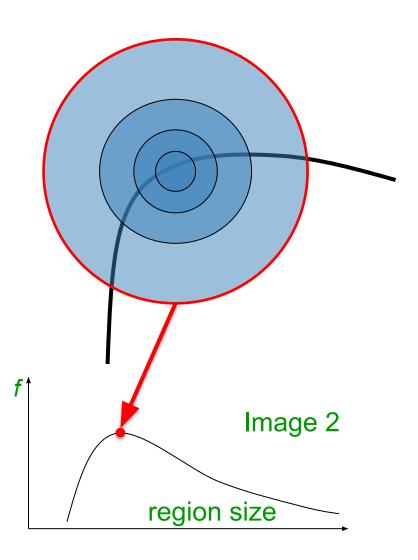
images?



Problem: How do we choose region sizes independently

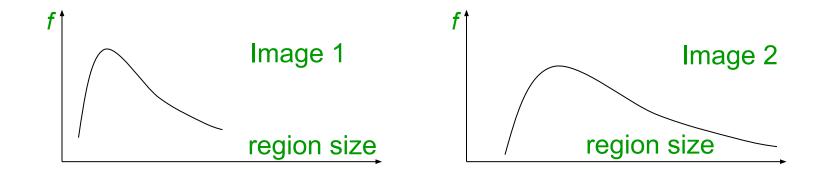
in each image?



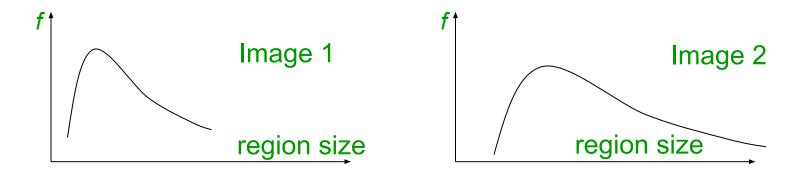


Solution: design a "scale-invariant" detector

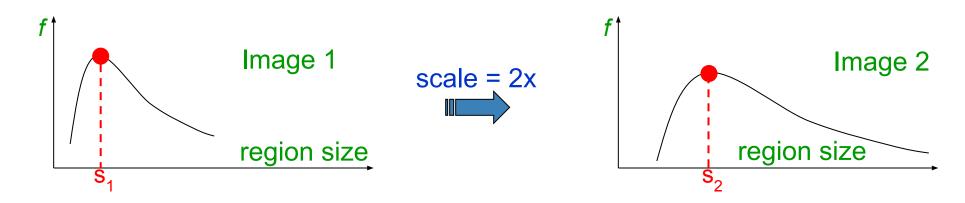
- Assume that the detector is made up of a series of functions,
 - each function depends on the pixel values and the region's size
- The function on the region should have the same value even if the keypoints are at different scales



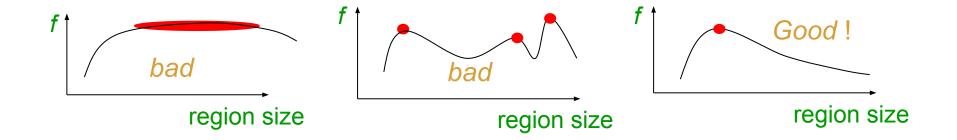
- Common approach to choose scale:
 - Take a local maximum of this function
- **Important**: this scale invariant region size is found in each image for each corner!
- **Observation**: the region size at the maximum should be *correlated* to the keypoint's scale. In other words, the size is correlated with the size of the corner



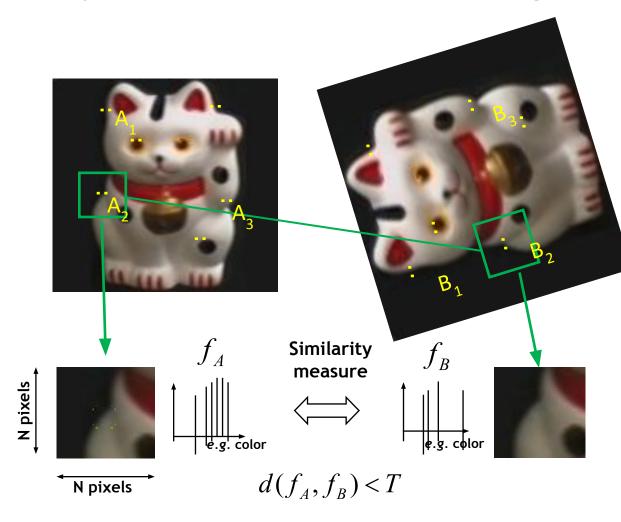
- Common approach to choose scale:
 - Take a local maximum of this function
- Important: this scale invariant region size is found in each image for each corner!
- Observation: the region size at the maximum should be correlated to the keypoint's scale. In other words, the size is correlated with the size of the corner



• A "good" function for scale selection has one stable sharp peak



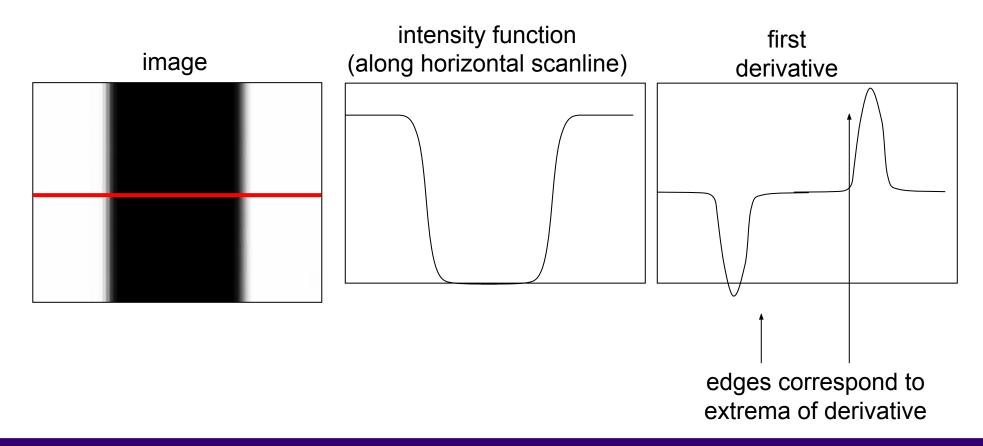
 For usual images: a good function would be one which responds to contrast (sharp local intensity change) Why we care about knowing the keypoint patch size??



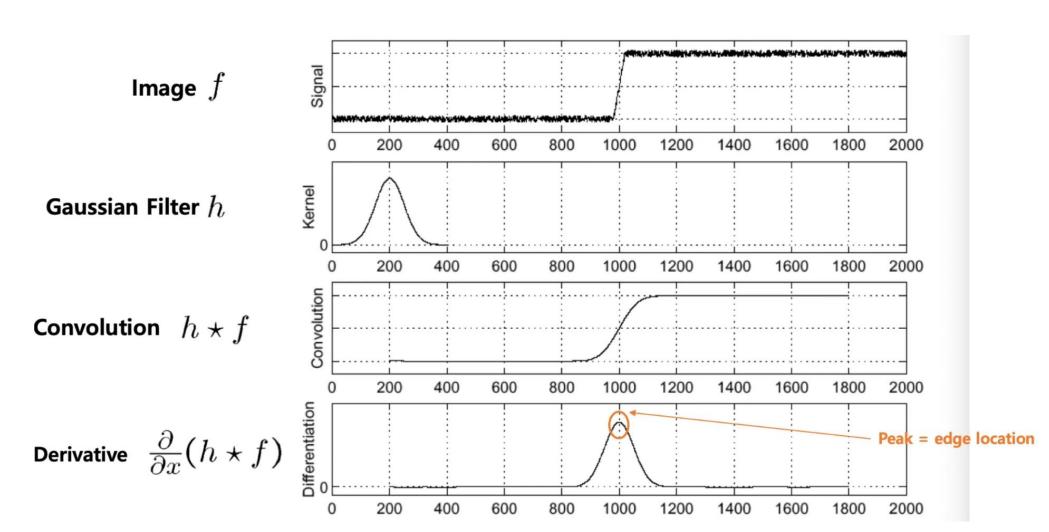
- 1. Find a set of distinctive key-points
- 2. Define a region/patch around each keypoint
- 3. Normalize the region content
- 4. Compute a local descriptor from the normalized region
- 5. Match local descriptors

Before we design this function, let's review: Characterizing edges

An edge is a place of rapid change in the image intensity function



Review: detecting edges



Review: Because convolutions are linear:

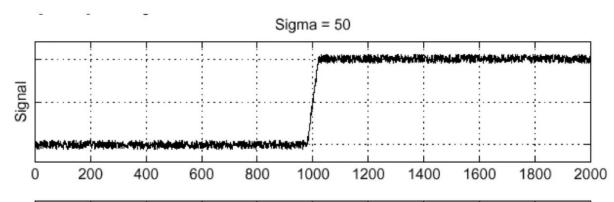
$$\frac{\partial}{\partial x}(h \star f) = (\frac{\partial}{\partial x}h) \star f$$

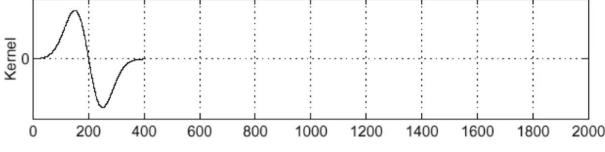
f

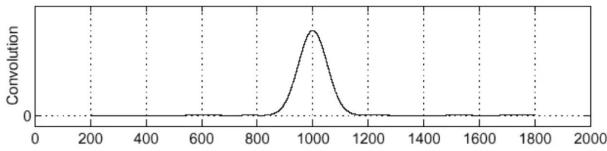


$$(\frac{\partial}{\partial x}h)\star f$$

 $\frac{\partial}{\partial x}h$





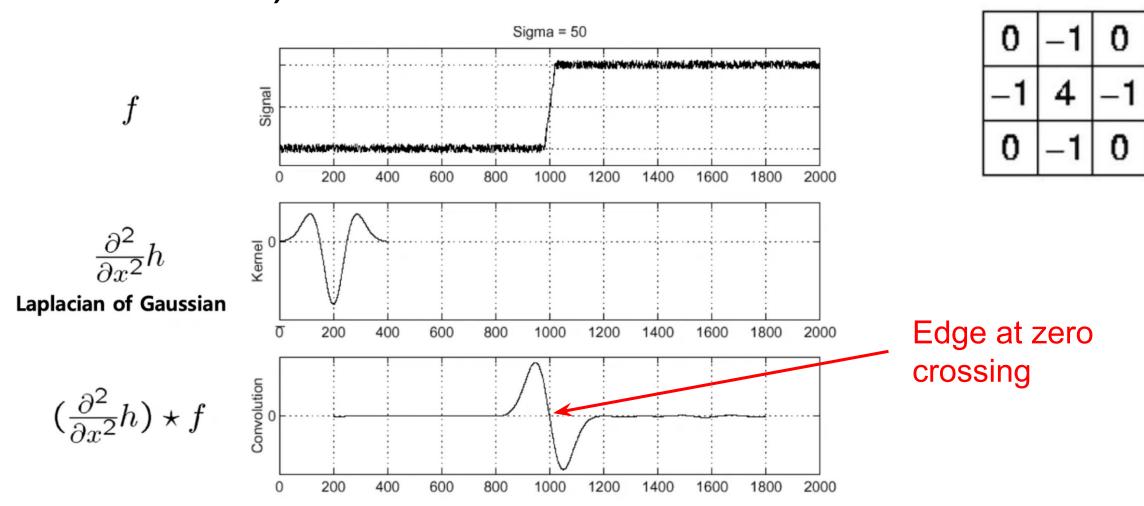


Another similar filter: The Laplacian

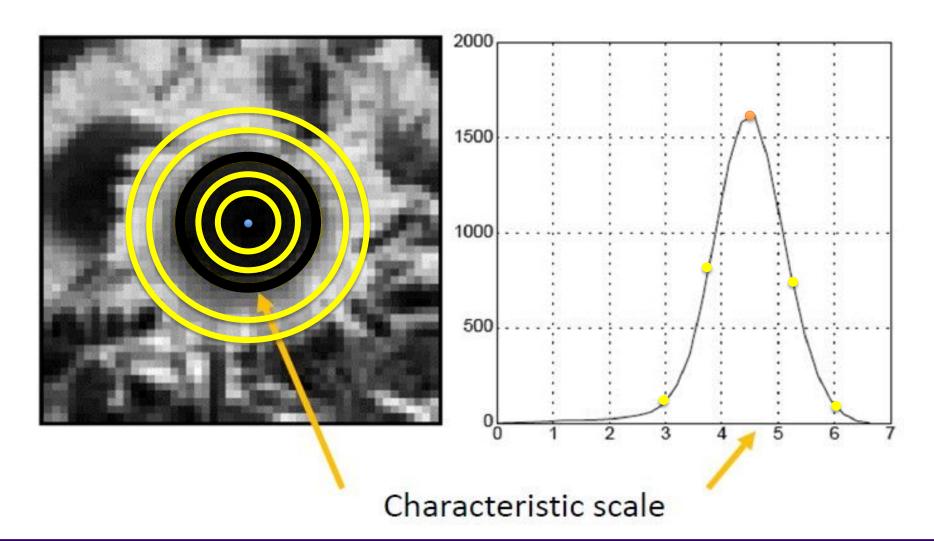
$$Laplacian \ \nabla^2 f = \frac{\partial^2 f}{\partial^2 x} + \frac{\partial^2 f}{\partial^2 y}$$

0	-1	0
-1	4	-1
0	-1	0

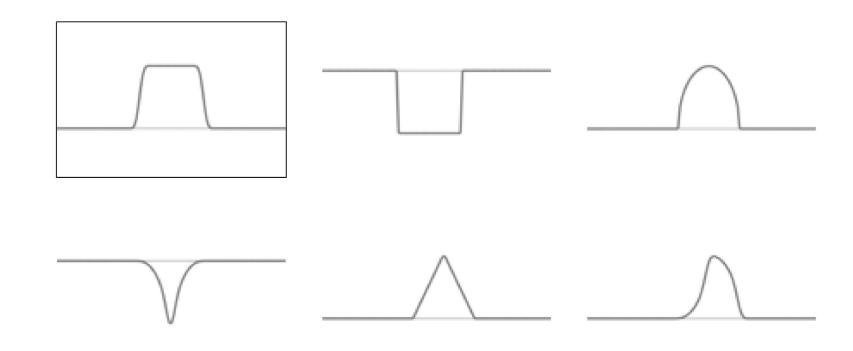
Another similar filter: The Laplacian (second derivative) of a Gaussian



Laplacian of a Gaussian

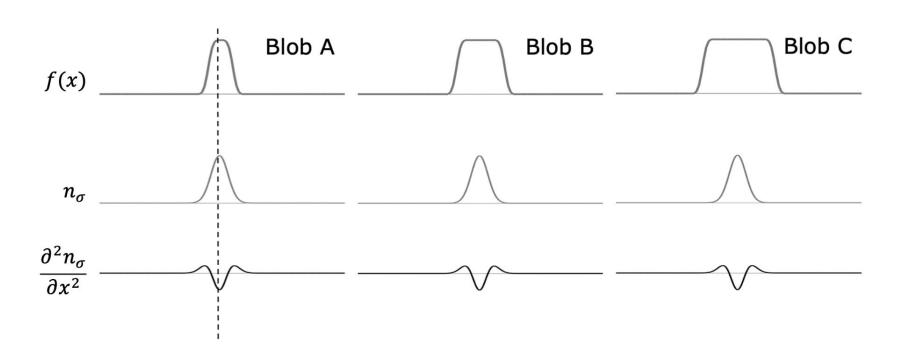


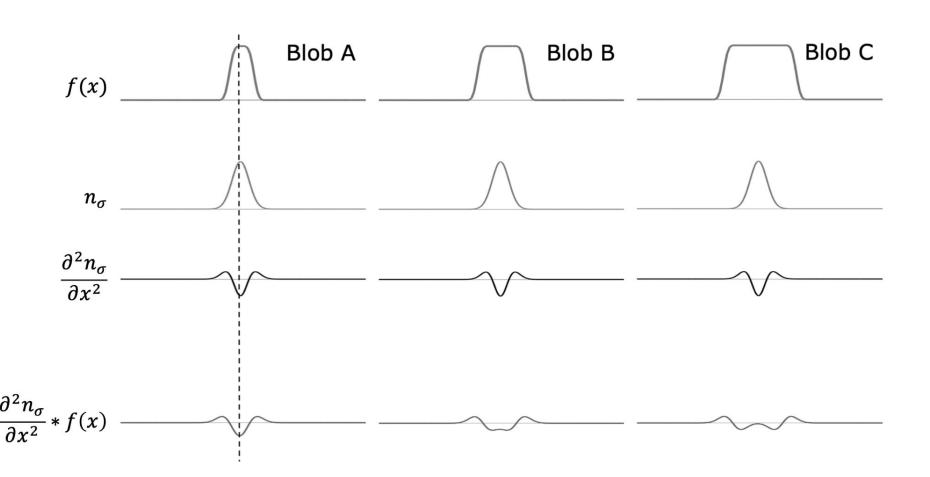
LoG is very good to detecting not just edges or corners but any "blob"

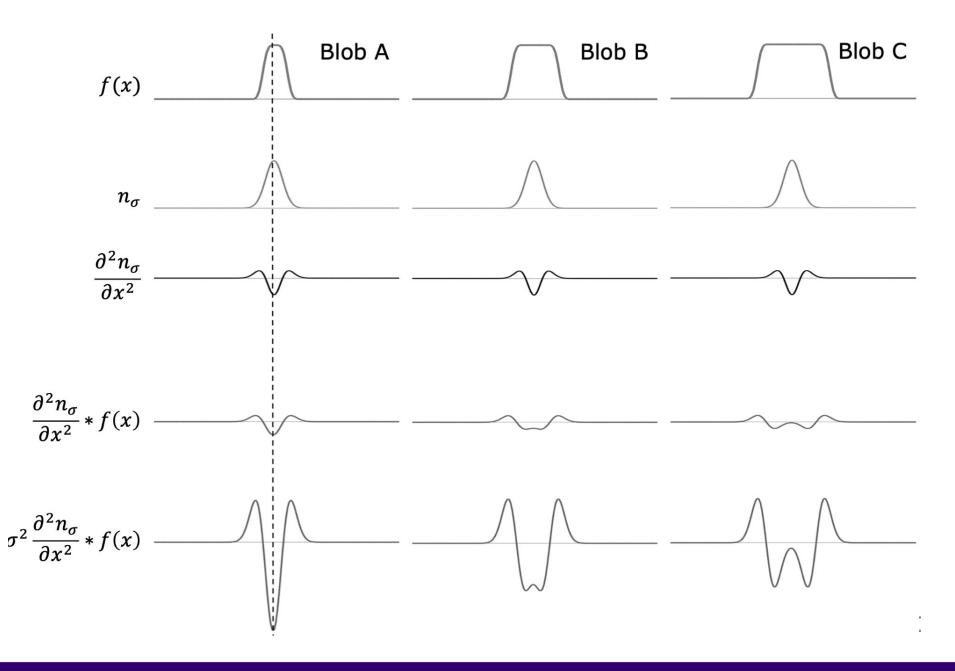




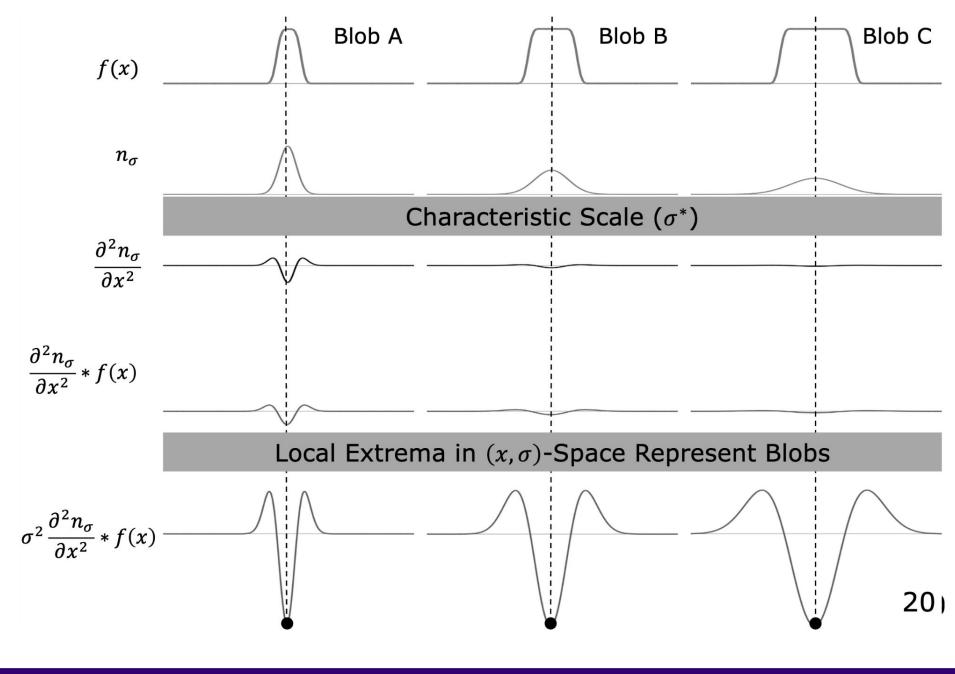
Blob B is 2x as wide as blob A Blob C is 3x as wide as blob B







increasing sigma, we can detect blobs of different sizes



Given: 1D signal f(x)

Compute: $\sigma^2 \frac{\partial^2 n_{\sigma}}{\partial x^2} * f(x)$ at many scales $(\sigma_0, \sigma_1, \sigma_2, ..., \sigma_k)$.

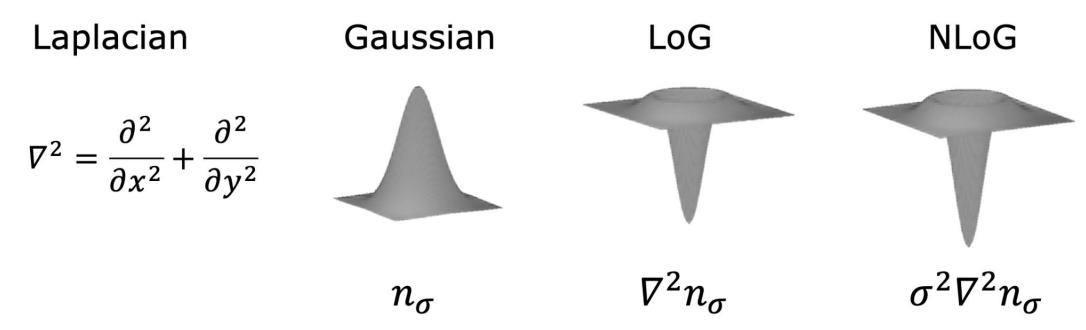
Find:
$$(x^*, \sigma^*) = \underset{(x,\sigma)}{\operatorname{arg max}} \left| \sigma^2 \frac{\partial^2 n_{\sigma}}{\partial x^2} * f(x) \right|$$

 x^* : Blob Position

 σ^* : Characteristic Scale (Blob Size)

Example in 2D

Normalized LoG (NLoG) is used to find blobs in images



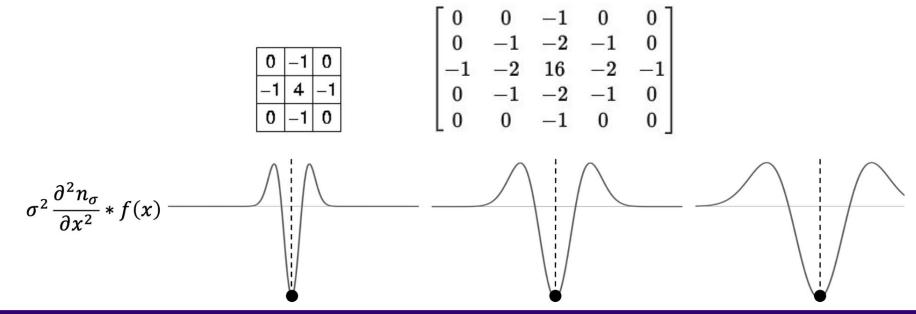
Location of Blobs identified by Local maxima after applying NLoG at many scales.

What do laplacian filters look like?

The size of the filter increases with increasing sigma.

Meaning that larger blobs require a larger filter.

Q. Why is this a problem?



This is a very expensive algorithm!

Given an image I(x,y)

Convolve the image using NLoG at many scales σ

Find:

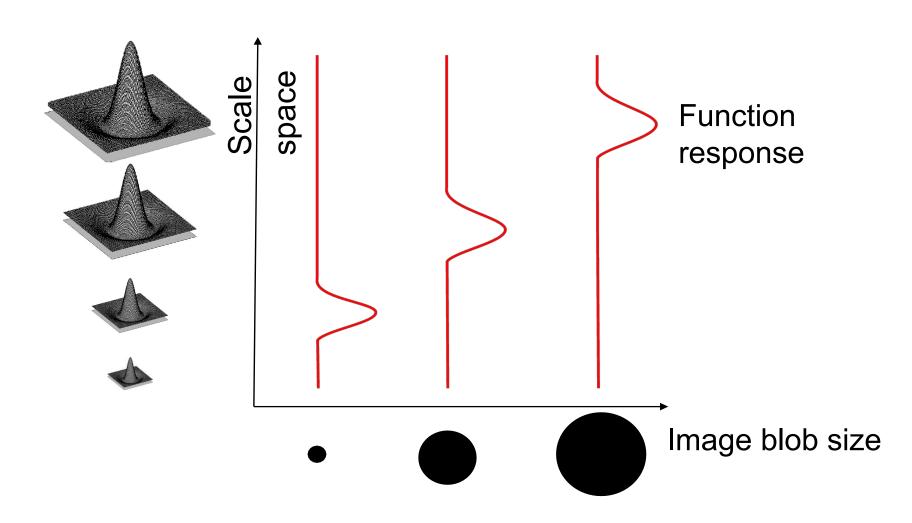
$$(x^*, y^*, \sigma^*) = \underset{(x,y,\sigma)}{\operatorname{arg max}} |\sigma^2 \nabla^2 n_{\sigma} * I(x,y)|$$

 (x^*, y^*) : Position of the blob

 σ^* : Size of the blob

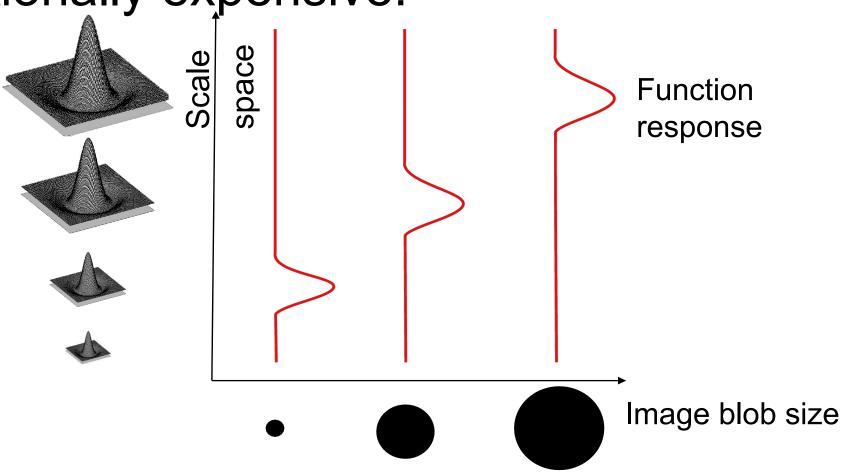
Laplacian of a Gaussian

Laplacian (2nd derivative) of Gaussian (LoG)



Problem: We have to convolve multiple filters of different sized laplacians to find all blobs. This is computationally expensive!

Laplacian (2nd derivative) of Gaussian (LoG)

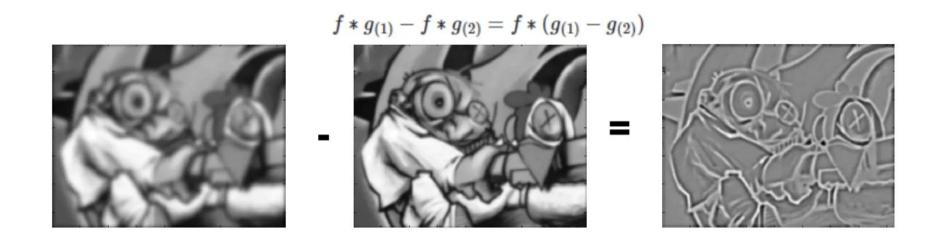


Today's agenda

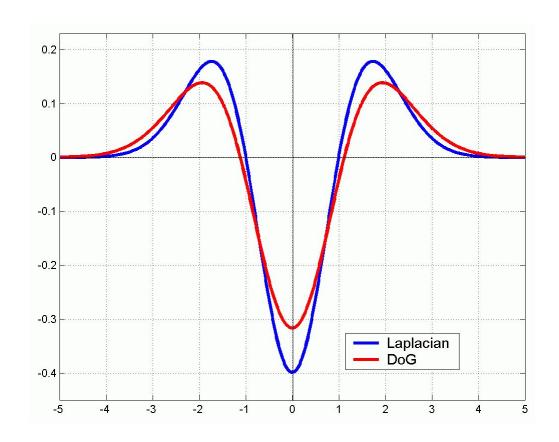
- Scale invariant keypoint detection
- Local detectors (SIFT)
- Local descriptors (SIFT)
- Global descriptors (HoG)

The LoG is very similar to the difference of Gaussians (DoG)





LoG and DoG are very similar



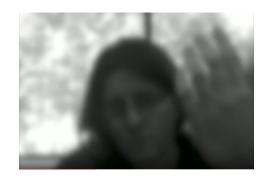
Note: both filters are invariant to

scale and rotation

Why does this approximation matter?



Original video



Blurred with a Gaussian kernel



Blurred with a different Gaussian kernel

Q. What happens if you subtract one blurred image from another?

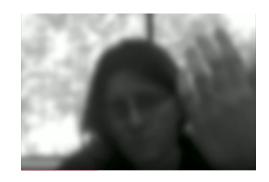
Difference of Gaussians (DoG) example



Original video



DoG: $k_1 - k_2$



Blurred with a Gaussian kernel: k₁



DoG: $k_1 - k_3$

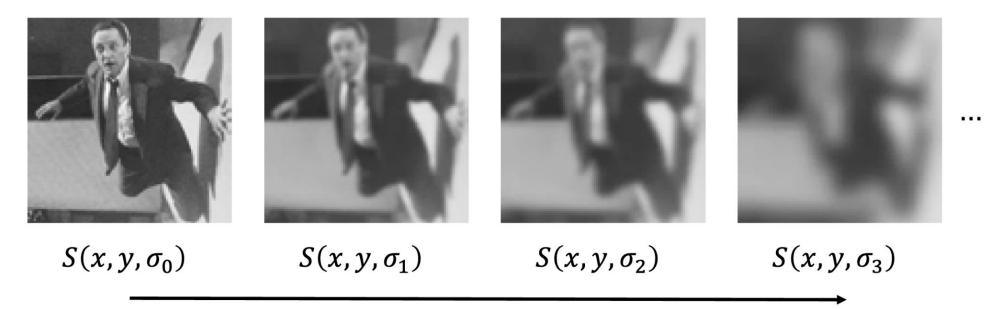


Blurred with a different Gaussian kernel: k₂



DoG: $k_1 - k_4$

Example in 2D



Increasing σ , Higher Scale, Lower Resolution

Scale Space: Stack of images created by filtering an image with Gaussians of different sigma values

$$S(x, y, \sigma) = n(x, y, \sigma) * I(x, y)$$

Example in 2D









 $S(x, y, \sigma_0)$

 $S(x, y, \sigma_1)$

 $S(x, y, \sigma_2)$

 $S(x, y, \sigma_3)$

Increasing σ , Higher Scale, Lower Resolution

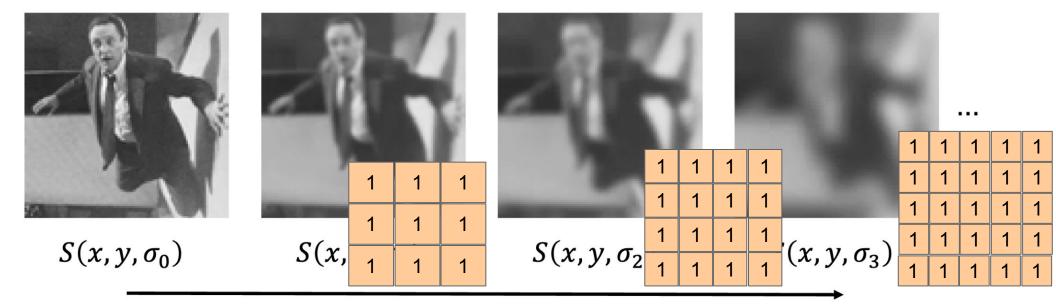
Selecting sigmas to generate the scale-space:

$$\sigma_k = \sigma_0 s^k \qquad k = 0,1,2,3,...$$

s: Constant multiplier

 σ_0 : Initial Scale

sigma represents size of a filter



Increasing σ , Higher Scale, Lower Resolution

Selecting sigmas to generate the scale-space:

$$\sigma_k = \sigma_0 s^k \qquad k = 0,1,2,3,...$$

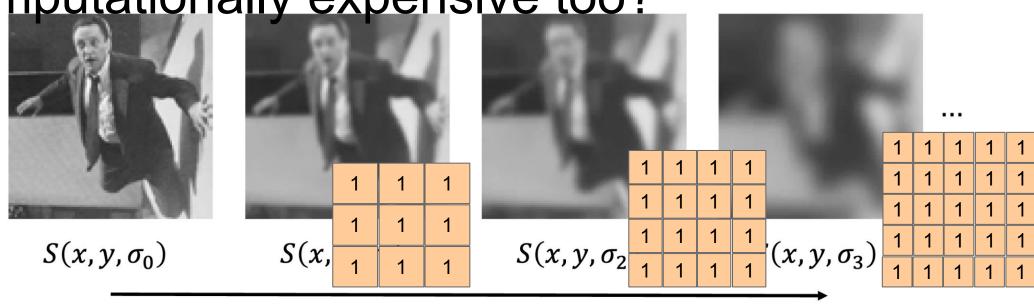
s: Constant multiplier

 σ_0 : Initial Scale

But wait, aren't we again using larger filter?

Doesn't this mean that using Gaussian filters is

computationally expensive too?



Increasing σ , Higher Scale, Lower Resolution

Selecting sigmas to generate the scale-space:

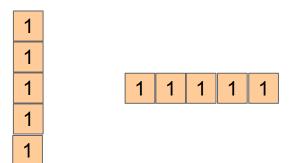
$$\sigma_k = \sigma_0 s^k \qquad k = 0,1,2,3,...$$

s: Constant multiplier

 σ_0 : Initial Scale

Remember from A1: Gaussian kernels are separable

Convolving with two 1D convolution filters = convolving with a large 2D filter



1	1	1	1	1
1	1	1	1	1
1	1	1	1	1
1	1	1	1	1
1	1	1	1	1

What do laplacian filters look like?

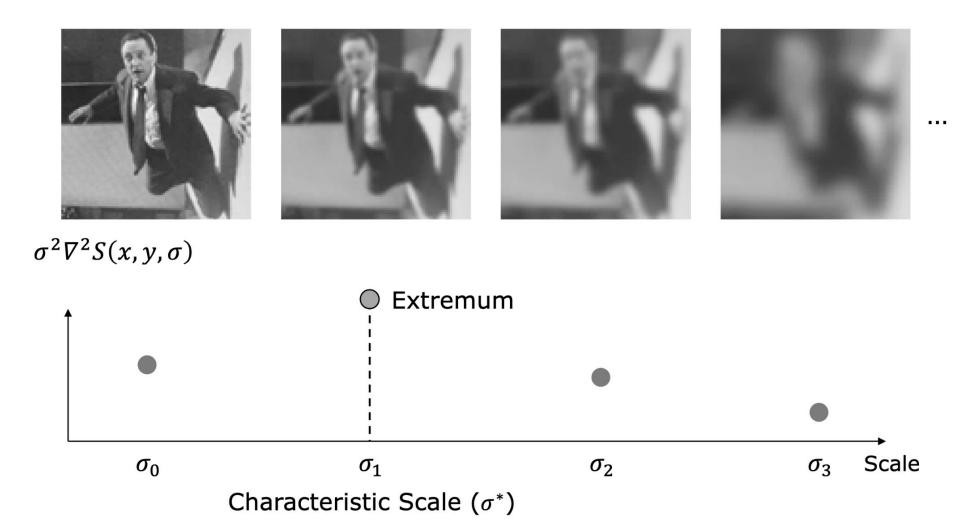
Laplacian

$$\begin{bmatrix} 0 & -1 & 0 \\ -1 & 4 & -1 \\ 0 & -1 & 0 \end{bmatrix} \qquad \begin{bmatrix} 0 & 0 & -1 & 0 & 0 \\ 0 & -1 & -2 & -1 & 0 \\ -1 & -2 & 16 & -2 & -1 \\ 0 & -1 & -2 & -1 & 0 \\ 0 & 0 & -1 & 0 & 0 \end{bmatrix}$$

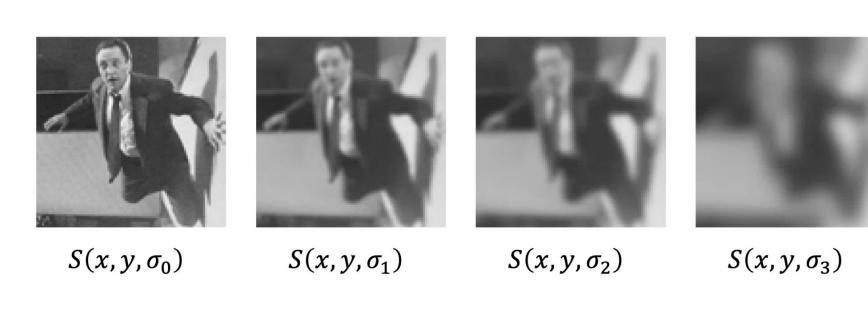
Gaussian

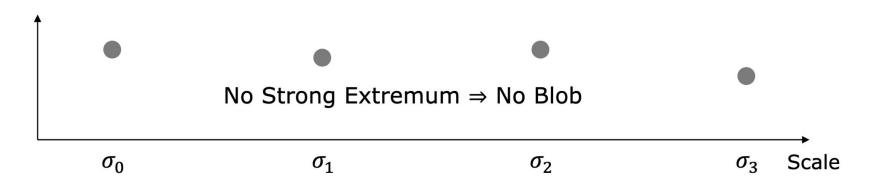
$$\frac{1}{256} \cdot \begin{bmatrix} 1 & 4 & 6 & 4 & 1 \\ 4 & 16 & 24 & 16 & 4 \\ 6 & 24 & 36 & 24 & 6 \\ 4 & 16 & 24 & 16 & 4 \\ 1 & 4 & 6 & 4 & 1 \end{bmatrix}$$

Example in 2D

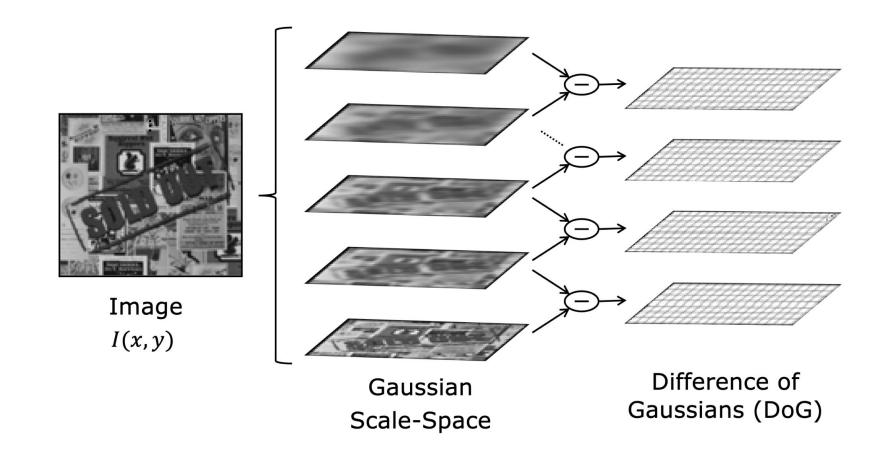


Example in 2D



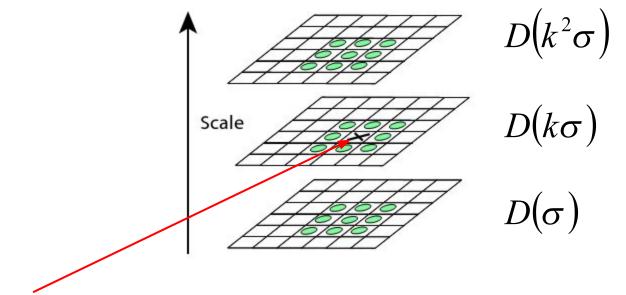


Overall SIFT detector algorithm



Extracting SIFT keypoints and scales

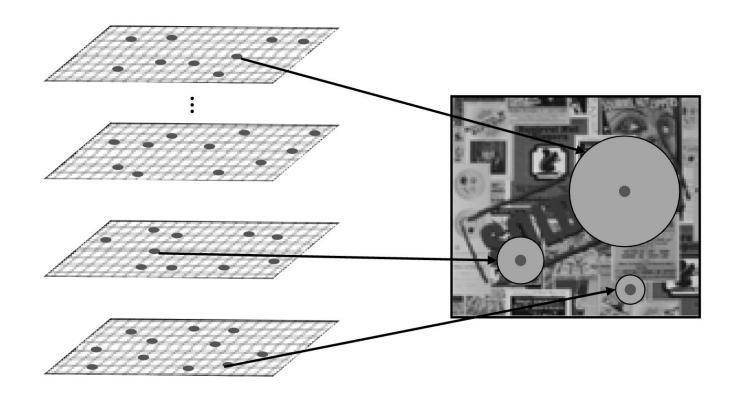
Choose the maxima within 3x3x3 neighborhood.



X is selected if it is larger or smaller than all 26 neighbors

Extracting SIFT keypoints and scales

Sigma value tells you how big the blog is



Difference-of-Gaussians

$$G(k^2\sigma)*I$$

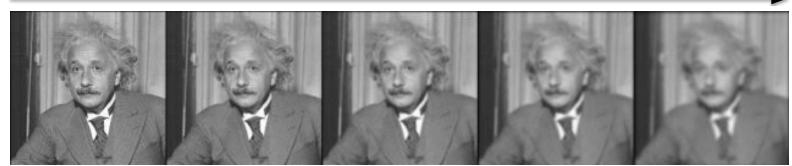
 $G(k\sigma)*I$

 $G(\sigma)*I$

$$D(\sigma) = (G(k\sigma) - G(\sigma)) * I$$

Scale, σ

Gaussian:



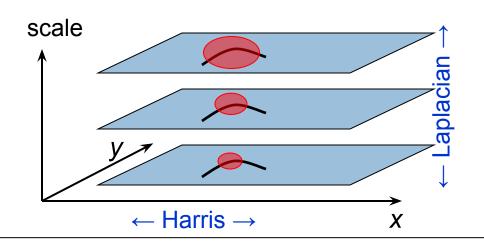
DoG:

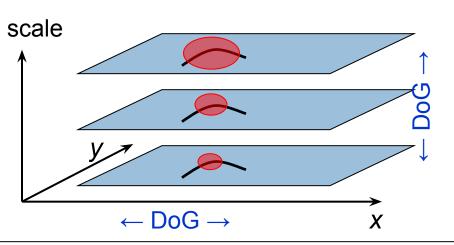
Scale Invariant Detectors

- Harris-Laplacian¹
 Find local maximum of:
 - Harris corner detector in space (image coordinates)
 - Laplacian in scale



Difference of Gaussians in space and scale





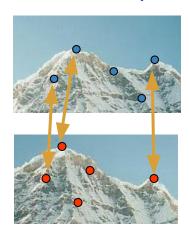
Scale Invariant Detectors

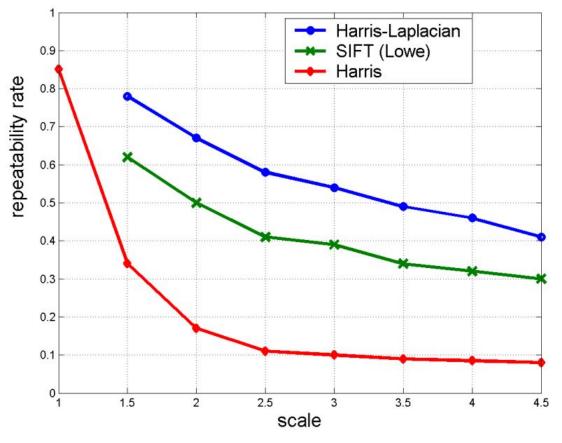
Experimental evaluation of detectors

w.r.t. scale change

Repeatability rate:

correspondences # possible correspondences





Scale Invariant Detection: Summary

- Given: two images of the same scene with a large scale difference between them
- Goal: find the same interest points independently in each image
- Solution: search for maxima of suitable functions in scale (DoG with different size) and in space (convolution over the image)

Methods:

- Harris-Laplacian [Mikolajczyk, Schmid]: maximize Laplacian over scale, Harris' measure of corner response over the image
- 2. SIFT [Lowe]: maximize Difference of Gaussians over scale and space

Today's agenda

- Scale invariant keypoint detection
- Local detectors (SIFT)
- Local descriptors (SIFT)
- Global descriptors (HoG)

What's next?

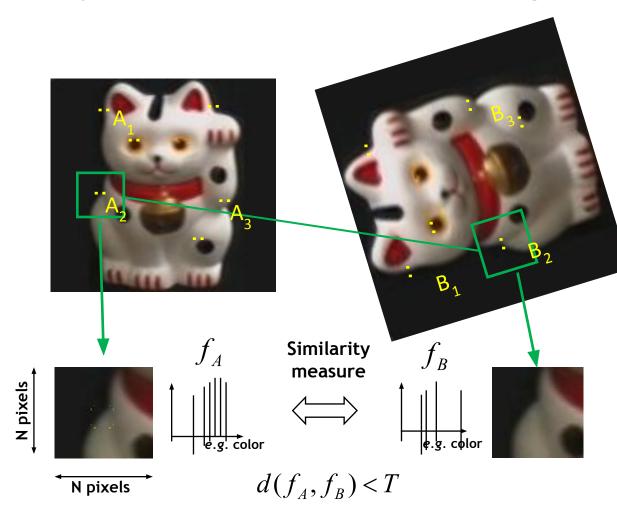
We now can detect keypoints at varying scales. But what can we do with those keypoints?

Things we would like to do:

- Search:
 - We would need to find similar key points in other images
- Panorama stitching
 - Match keypoints from one image to another.
- Etc...

For all such applications, we need a way of 'describing' the keypoints.

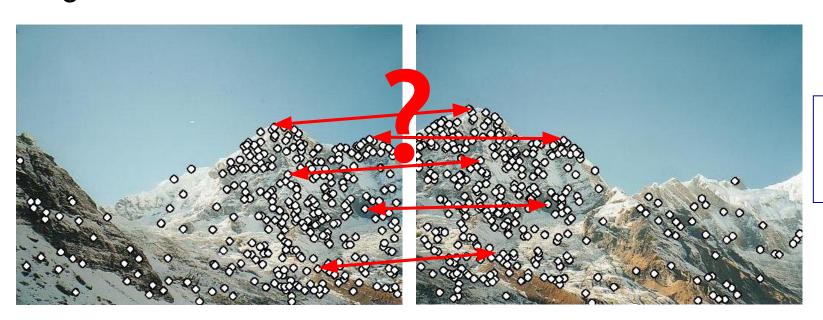
Why we care about knowing the keypoint patch size??



- 1. Find a set of distinctive key-points
- 2. Define a region/patch around each keypoint
- 3. Normalize the region content
- 4. Compute a local descriptor from the normalized region
- 5. Match local descriptors

Local Descriptors are vectors

- We know how to detect points
- Next question: How to describe them for matching?
- Descriptor: Vector that summarizes the content of the keypoint neighborhood.

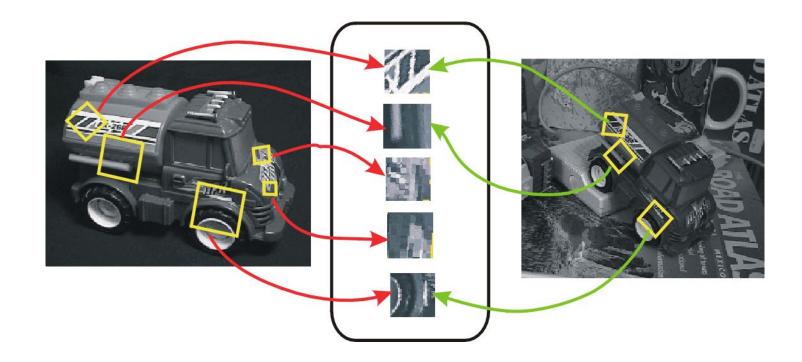


Point descriptor should be:

- 1. Invariant
- 2. Distinctive

Invariant Local Descriptors

Image content is transformed into local feature coordinates that are **invariant** to translation, rotation, scale, and other imaging parameters

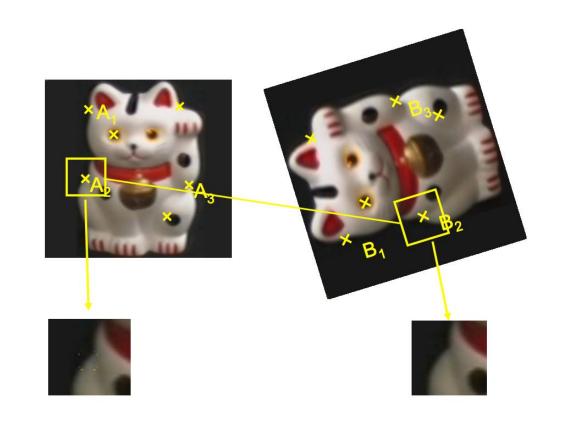


Rotation invariant descriptors

So far, we have figured out the scale of the keypoints.

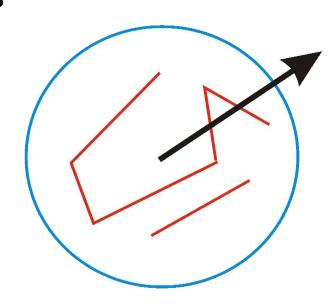
- So we can normalize them to be the same size.

Q. How do we re-orient the patches so that they are rotation invariant?



Constructing a rotation invariant descriptor

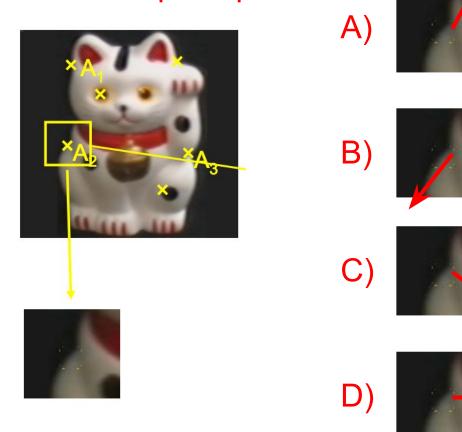
- We are given a keypoint and its scale from DoG
- We will select the direction of maximum gradient as the orientation for the keypoint
- We will describe all features *relative* to this orientation

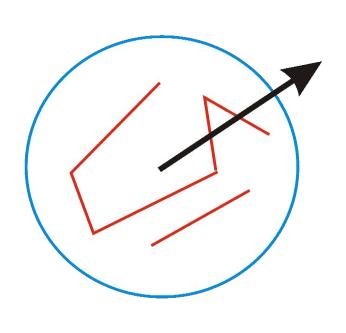


Visualizing what that looks like

Q. Which one is the direction of the maximum gradient

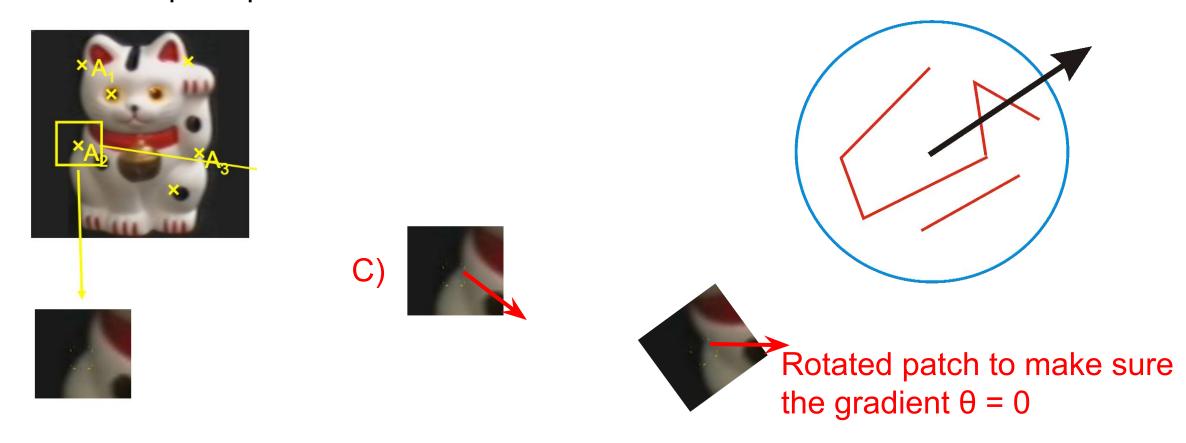
for this ketpoint patch?





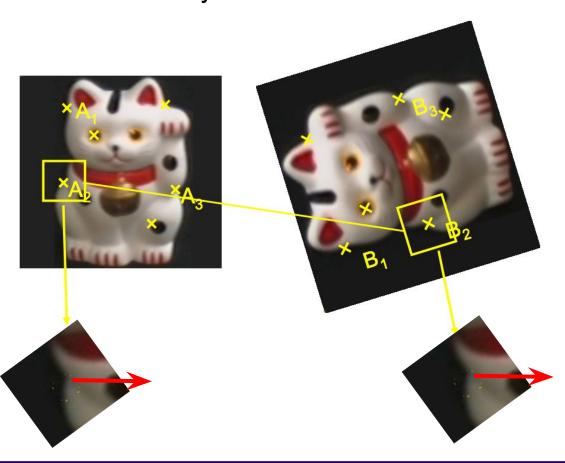
Visualizing what that looks like

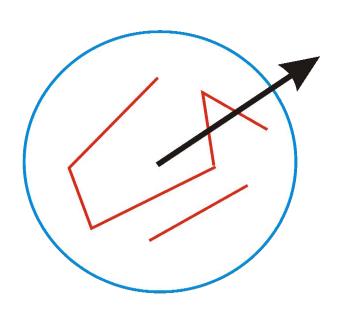
Q. Which one is the direction of the maximum gradient for this ketpoint patch?



Feature descriptors become rotation invariant

 If the keypoint appears rotated in another image, the features will be the same, because they're relative to the characteristic orientation

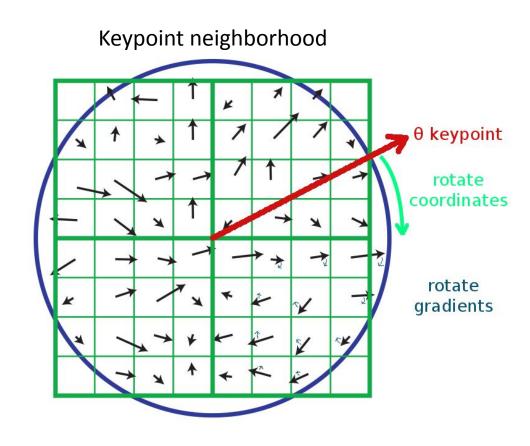




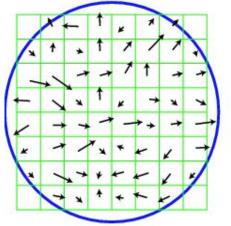
SIFT descriptor (Scale-Invariant Feature Transform)

Gradient-based descriptor to capture texture in the keypoint neighborhood

- 1. Blur the keypoint's image patch to remove noise
- 2. Calculate image **gradients** over the neighborhood patch.
- 3. To become rotation invariant, rotate the gradients by $-\theta$ (- maximum direction)
 - Now we've cancelled out rotation and have gradients expressed at locations relative to maximum direction θ
- 4. Generate a descriptor

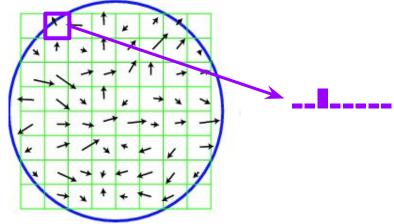


Keypoint neighborhood



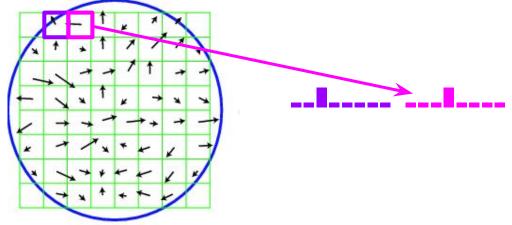
Q. How do we turn this into a vector?





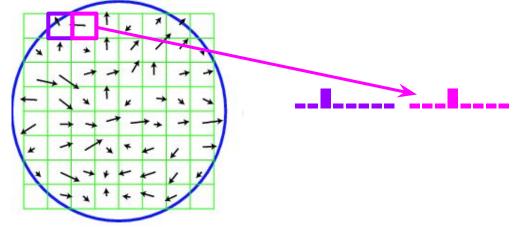
- We can turn every pixel into a histogram
- Histogram contains 8 buckets, all of them zero except for one.
- Make the bucket of the direction of the gradient equal to 1





- Do this for every single pixel
- Q. What would the size of the keypoint vector be?

Keypoint neighborhood

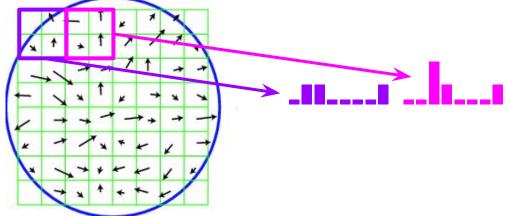


• Do this for every single pixel

Q. Why might this be a bad strategy? What could go wrong?

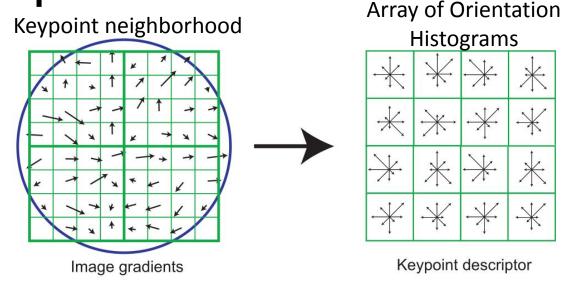
Hint: think about how matching might fail

Keypoint neighborhood



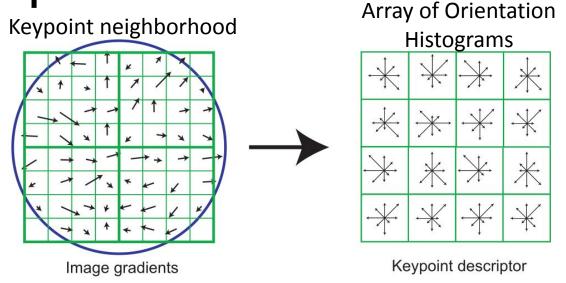
- Solution: divide keypoint up into 4x4 "cells"
- Calculate a histogram per cell and sum them together

SIFT descriptor formation



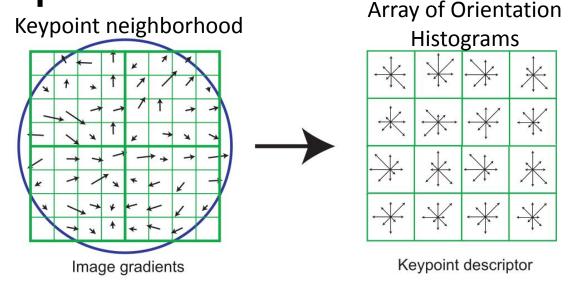
- Each cell gives us a histogram vector. We have a total of 4x4 vectors
- Calculate the overall gradients in each patch into their local orientated histograms
 - Also, scale down gradient contributions for gradients far from the center
 - Each histogram is quantized into 8 directions (each 45 degrees)

SIFT descriptor formation

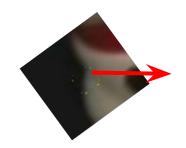


• Q. What is the size of the descriptor?

SIFT descriptor formation

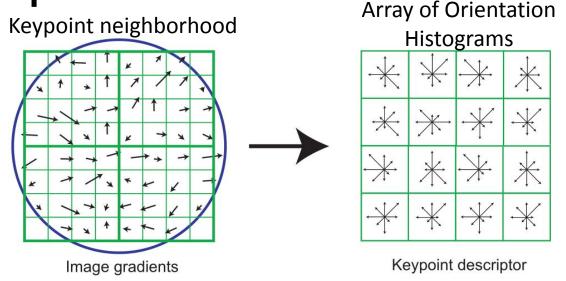


- 8 orientation bins per histogram,
- 4x4 histogram vectors,
- total is $8 \times 4 \times 4 = 128$ numbers.
- So a SIFT descriptor is a length 128 vector



$$\mathcal{H}o\mathcal{G}(k) = egin{bmatrix} g_1 \ g_2 \ \dots \ g_{128} \end{bmatrix}$$

SIFT descriptor formation



- SIFT descriptor is invariant to rotation (because we rotated the patch) and scale (because we worked with the scaled image from DoG)
- We can compare each vector from image A to each vector from image B to find matching keypoints!
 - O How do we match distances?

Making descriptors robust

Image gradients

Keypoint descriptor

- Adding robustness to illumination changes:
- Each descriptor is made of gradients (differences between pixels),
 - It's already invariant to changes in brightness
 - (e.g. adding 10 to all image pixels yields the exact same descriptor)
- A sharpening filter applied to the image will increase the magnitude of gradients linearly.
 - To correct for contrast changes, normalize the histogram (scale to magnitude=1.0)
- Very large image gradients are usually from unreliable 3D illumination effects (glare, etc).
 - To reduce their effect, clamp all values in the vector to be ≤ 0.2 (an experimentally tuned value). Then normalize the vector again.
- Result is a vector which is fairly invariant to illumination changes.

SIFT descriptor distances

Given keypoints k_1 and k_2 , we can calculate their HoG features:

 $HoG(k_1)$

 $HoG(k_2)$

We can calculate their matching score as:

$$d_{\mathcal{H}o\mathcal{G}}(k_1, k_2) = \sqrt{\sum_{i} (\mathcal{H}o\mathcal{G}(k_1)_i - \mathcal{H}o\mathcal{G}(k_2)_i)^2}$$

Find nearest neighbor for each keypoint in image A in image B

Given keypoints k_1 and k_2 , we can calculate their HoG features:

 $HoG(k_1)$

 $HoG(k_2)$

We can calculate their matching score as:

$$d_{\mathcal{H}o\mathcal{G}}(k_1, k_2) = \sqrt{\sum_{i} (\mathcal{H}o\mathcal{G}(k_1)_i - \mathcal{H}o\mathcal{G}(k_2)_i)^2}$$







Figure 12: The training images for two objects are shown on the left. These can be recognized in a cluttered image with extensive occlusion, shown in the middle. The results of recognition are shown on the right. A parallelogram is drawn around each recognized object showing the boundaries of the original training image under the affi ne transformation solved for during recognition. Smaller squares indicate the keypoints that were used for recognition.

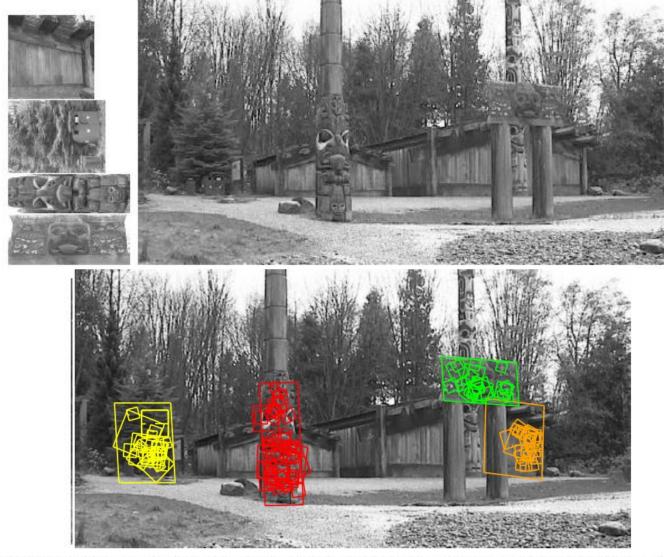


Figure 13: This example shows location recognition within a complex scene. The training images for locations are shown at the upper left and the 640x315 pixel test image taken from a different viewpoint is on the upper right. The recognized regions are shown on the lower image, with keypoints shown as squares and an outer parallelogram showing the boundaries of the training images under the affi ne transform used for recognition.

Recognition of specific objects, scenes

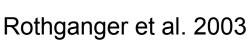


Schmid and Mohr 1997



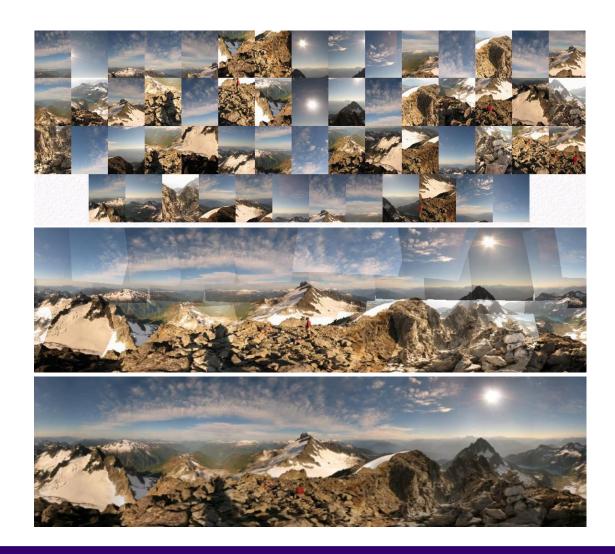
Sivic and Zisserman, 2003







Panorama stitching/Automatic image mosaic

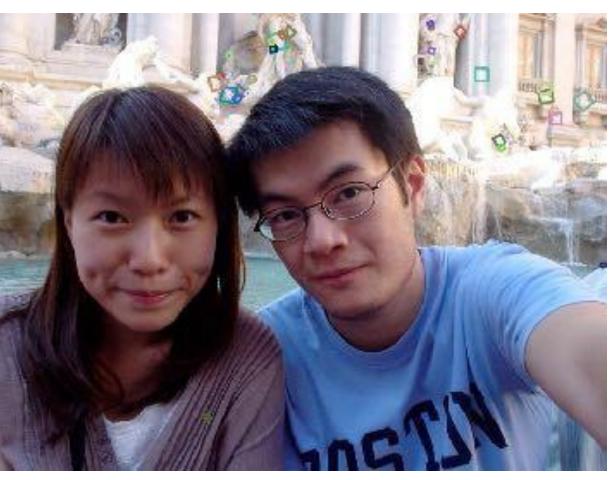


http://matthewalunbrown.com/autostitch/autostitch.html

Wide baseline stereo



Even robust to extreme occlusions





Applications of local invariant features

- Recognition
- Wide baseline stereo
- Panorama stitching
- Mobile robot navigation
- Motion tracking
- 3D reconstruction
- ...

Today's agenda

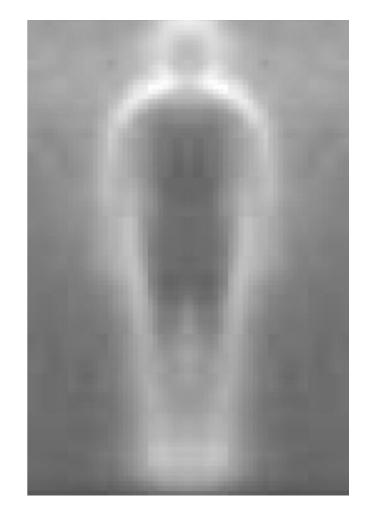
- Scale invariant keypoint detection
- Local detectors (SIFT)
- Local descriptors (SIFT)
- Global descriptors (HoG)

Global Feature descriptors

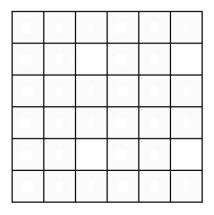
- Find robust feature set that allows object shape to be recognized.
- Challenges
 - Wide range of pose and large variations in appearances
 - Cluttered backgrounds under different illumination
 - Computation speed
- Histogram of Oriented Gradients (HoG)

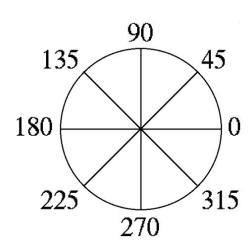
[1] N. Dalal and B. Triggs. Histograms of Oriented Gradients for Human Detection. In CVPR, pages 886-893, 2005

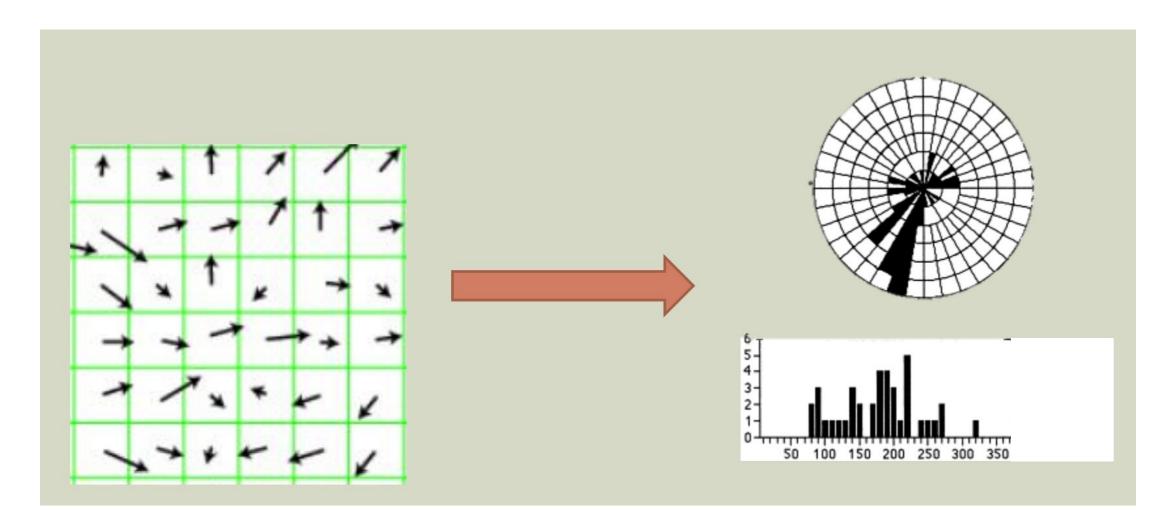
- Local object appearance and shape can often be characterized well using gradients.
- Specifically, the distribution of local intensity gradients or edge directions.

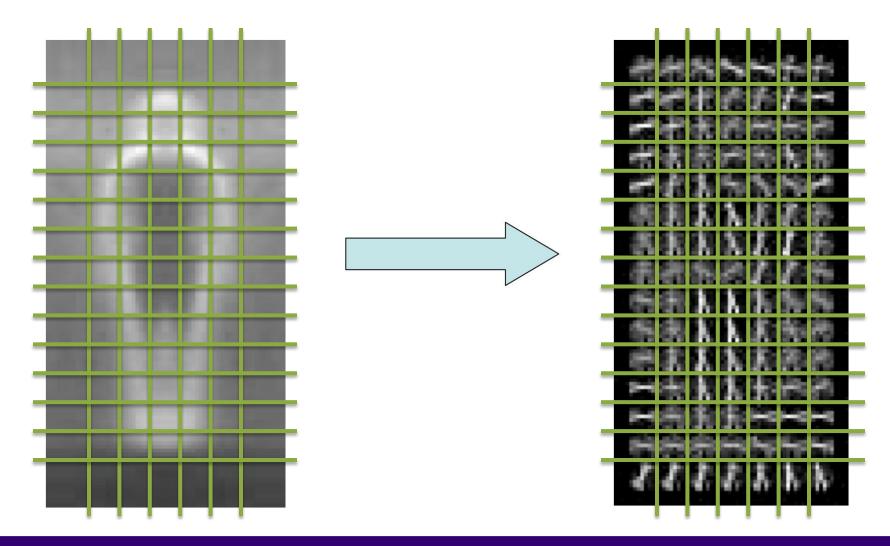


- Dividing the image window into small spatial regions (cells)
- Cells can be either rectangle or radial.
- Each window sums up local 1-D histogram of gradient directions over the pixels of the cell.



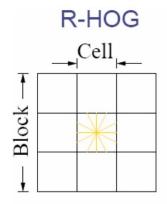


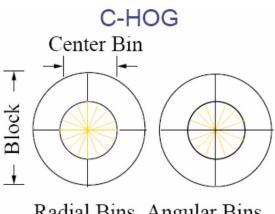




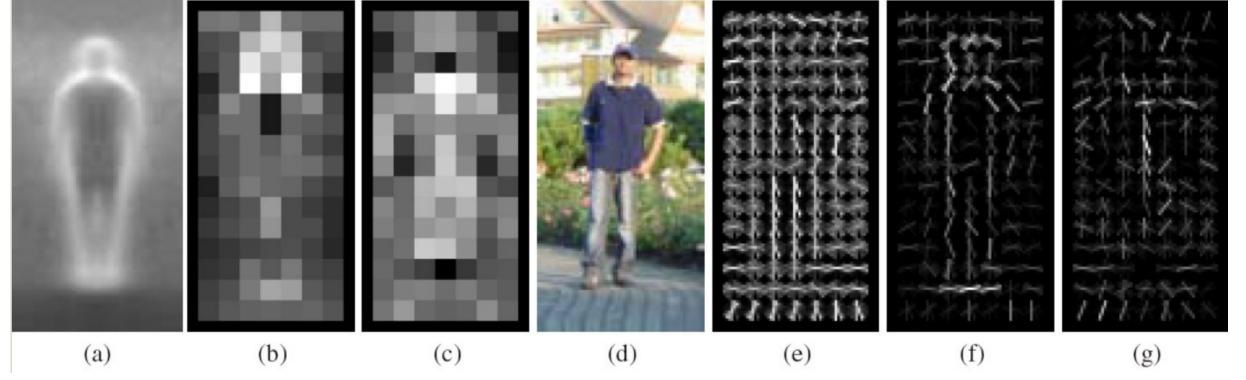
Normalization

- To make HoG invariant to illumination and shadows, it is useful to normalize the local responses
- Normalize each cell's histogram using histogram over a larger regions ("blocks").





Radial Bins, Angular Bins

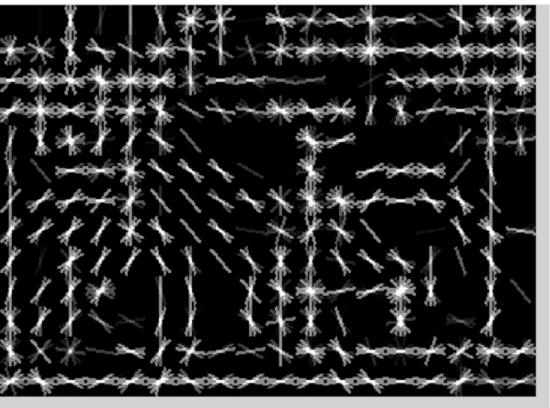


- a. Average gradient over example photo of a person
- b. "Positive" blocks that help match to other photos of people
- c. "Negative" blocks that do not match to photos of other people
- d. A test image
- e. It's HOG descriptor visualized
- f. HOG descriptor weighted by positive weights
- g. HOG descriptor weighted by negative weights

Visualizing HoG

Visualizing HoG



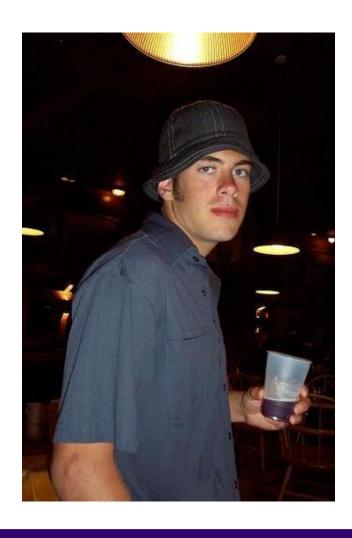


Difference between HoG and SIFT

- HoG is usually used to describe larger image regions.
- SIFT is used for key point matching

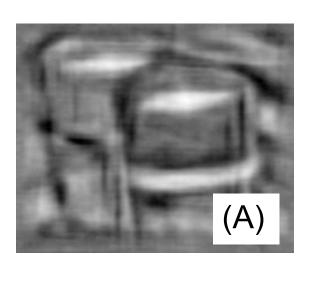
- SIFT histograms are normalized with respect to the dominant gradient.
- HoG gradients are normalized using neighborhood blocks.

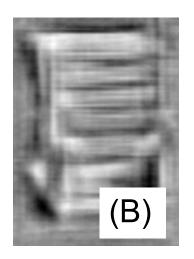
HoG features are good but gradients are insufficient sometimes

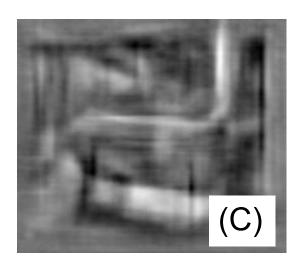


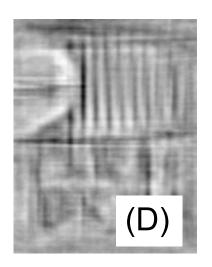


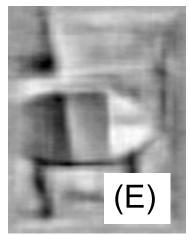
Chair Detections

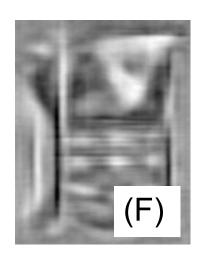


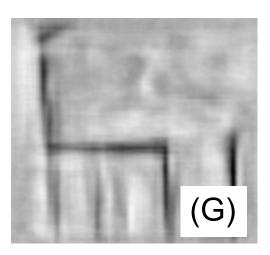












Chair Detections







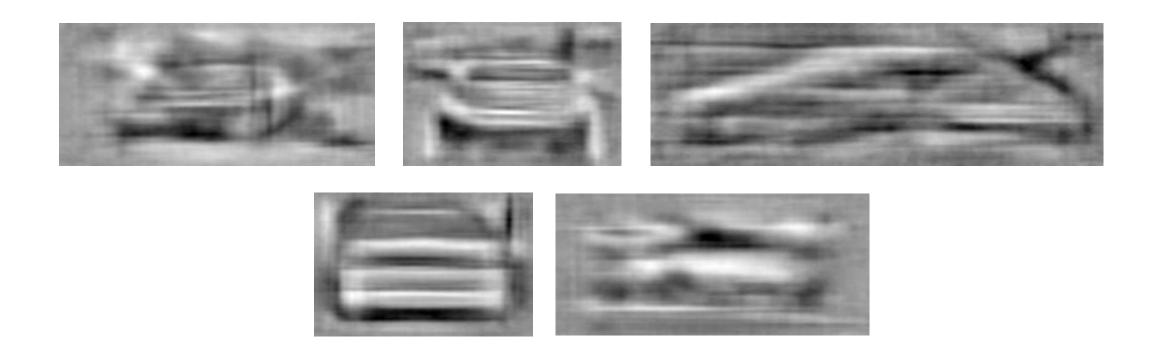








Car Detections



Car Detections











The HOGgles Challenge



Clap your hands when you see a person

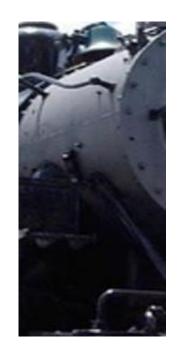






















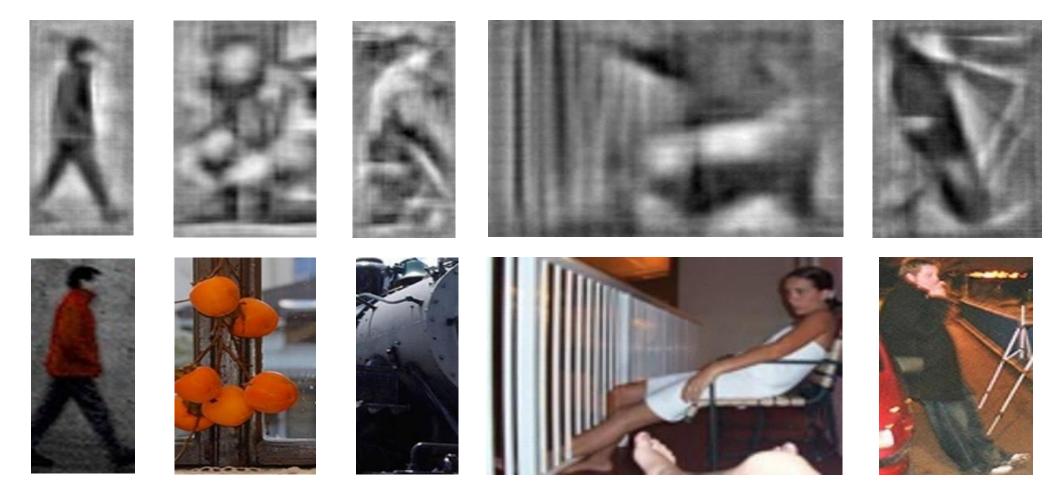








The HOGgles Challenge



Next time

Homographies