

# Lecture 16

Object detection

# Administrative

A4 is out

- Due May 23th

A5 is out

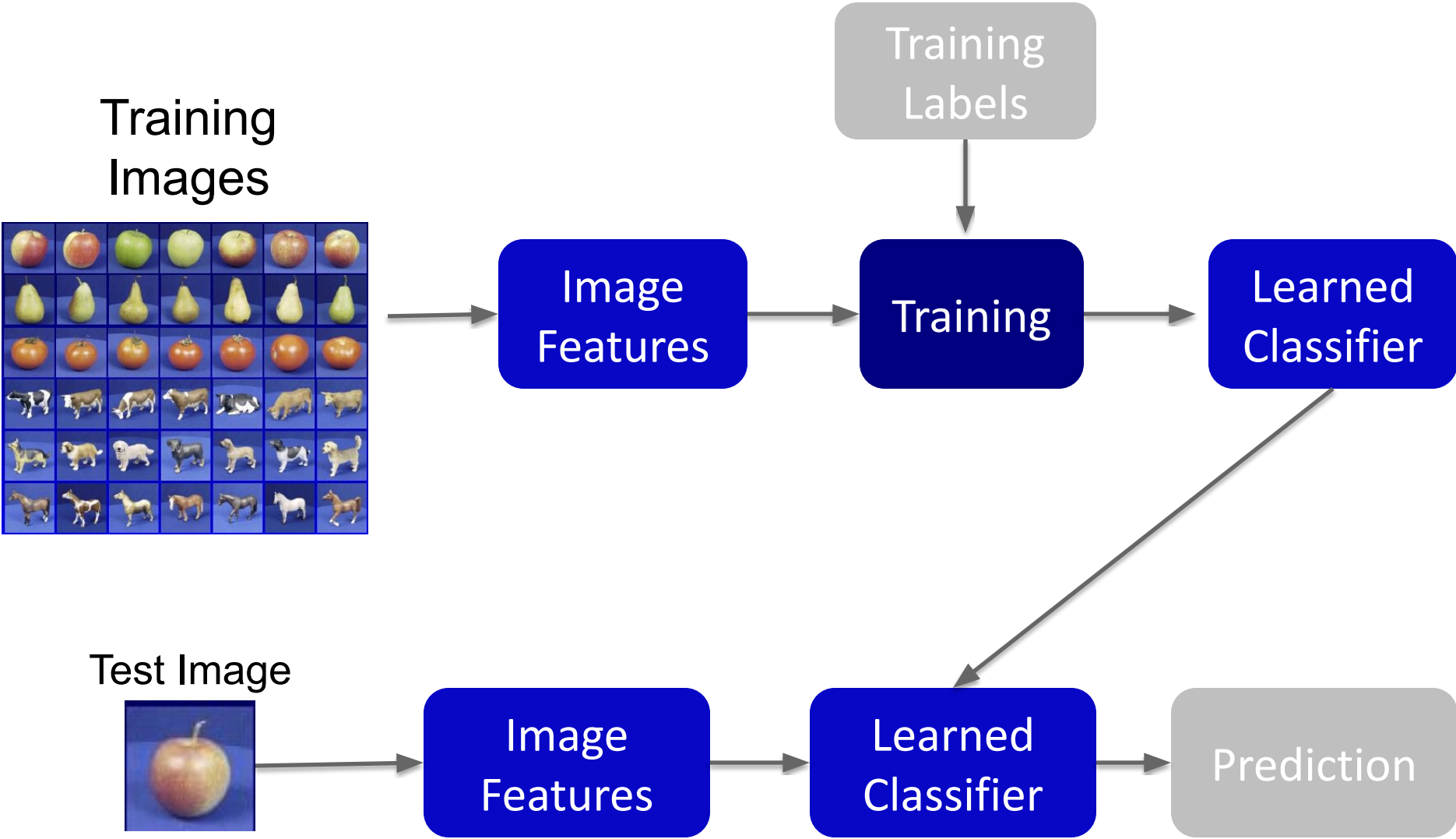
- Due May 30th

# Administrative

Recitation this friday

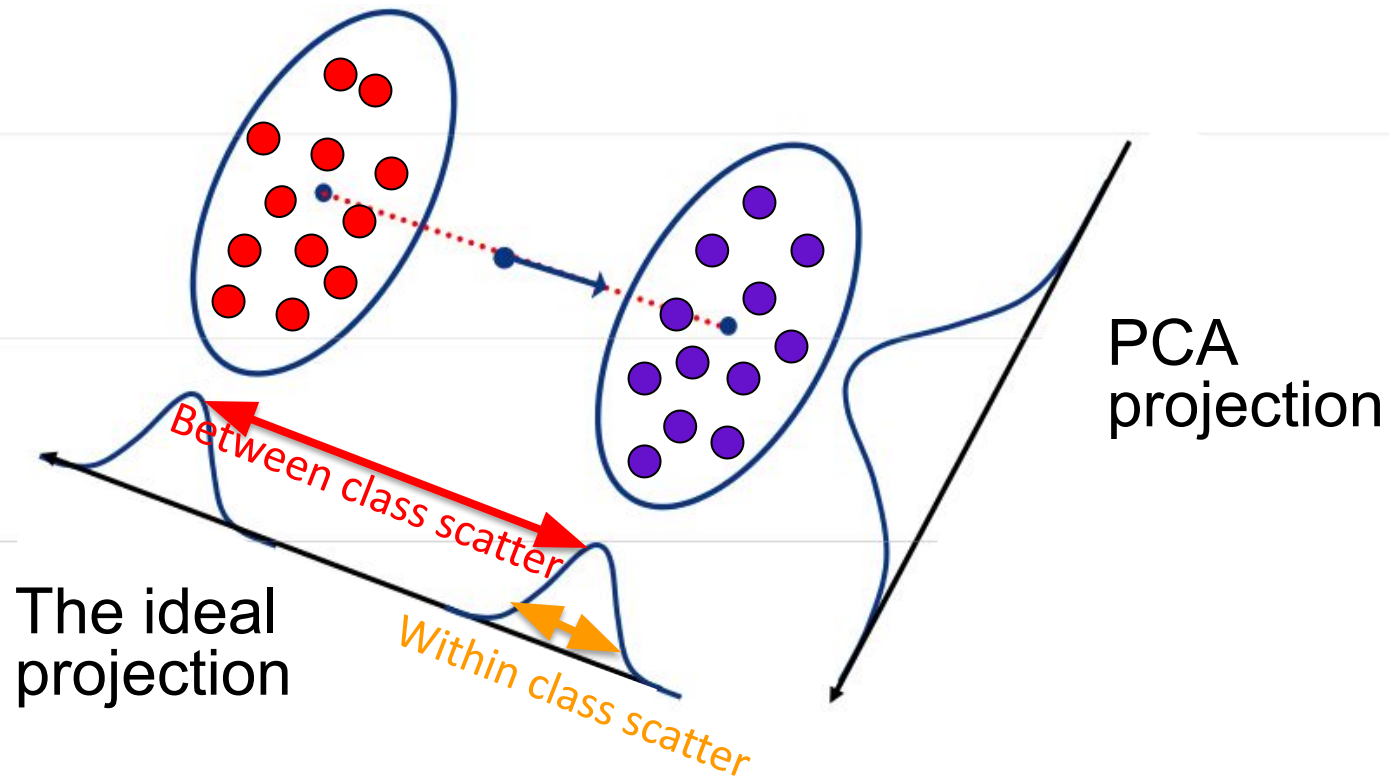
- Recognition review
- Jieyu Zhang

# So far: A simple recognition pipeline



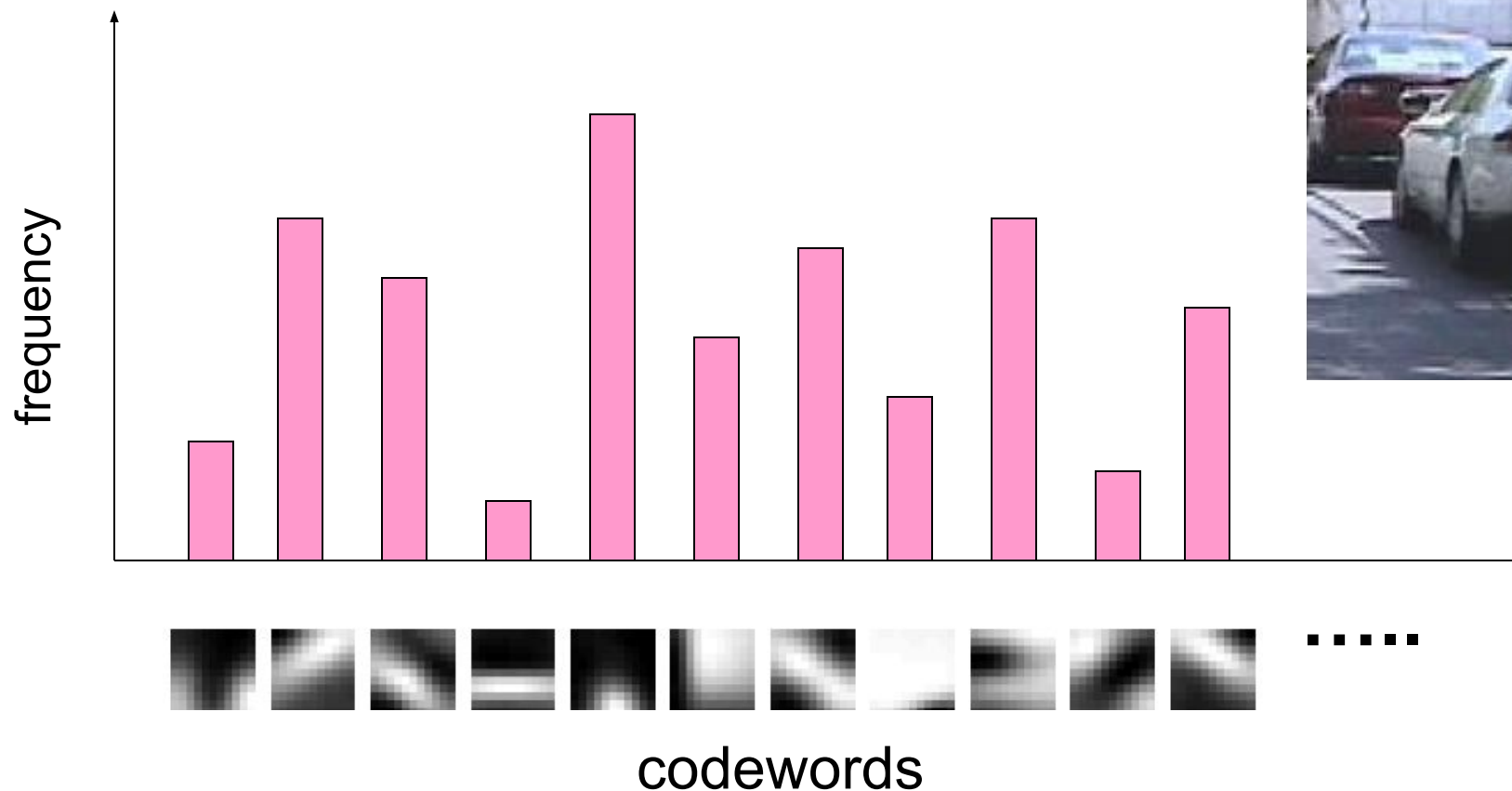
## So far: PCA versus LDA

We want a projection that maximizes:  $J(w) = \max \frac{\text{between class scatter}}{\text{within class scatter}}$

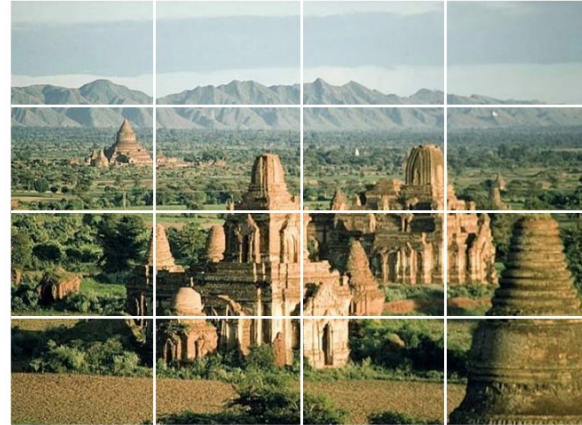


# So far: Bag of words features

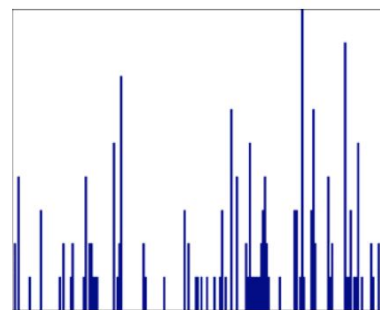
- Every image now becomes a k-dimensional histogram representation.
- We can use these features for any recognition task.



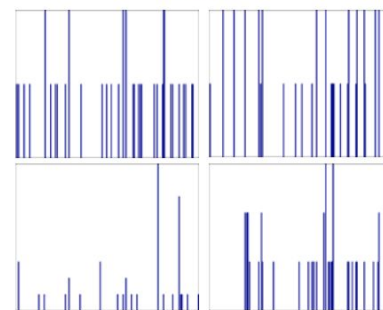
# So far: Bag of words + pyramids



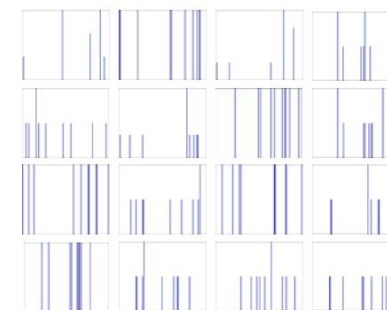
Locally orderless  
representation at  
several levels of  
spatial resolution



level 0



level 1



level 2

# Today's agenda

- Object detection
  - Task and evaluation
- A simple detector
- Deformable parts model



# Today's agenda

- Object detection
  - Task and evaluation
- A simple detector
- Deformable parts model

# Object Detection

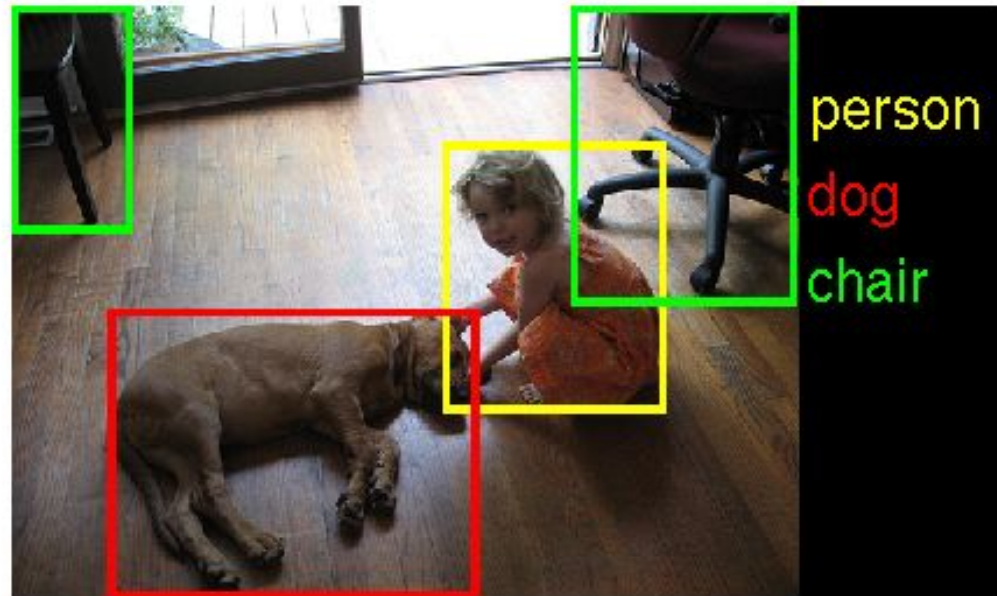


Credit: Flickr user [neilalderney123](#)

- What do you see in the image?

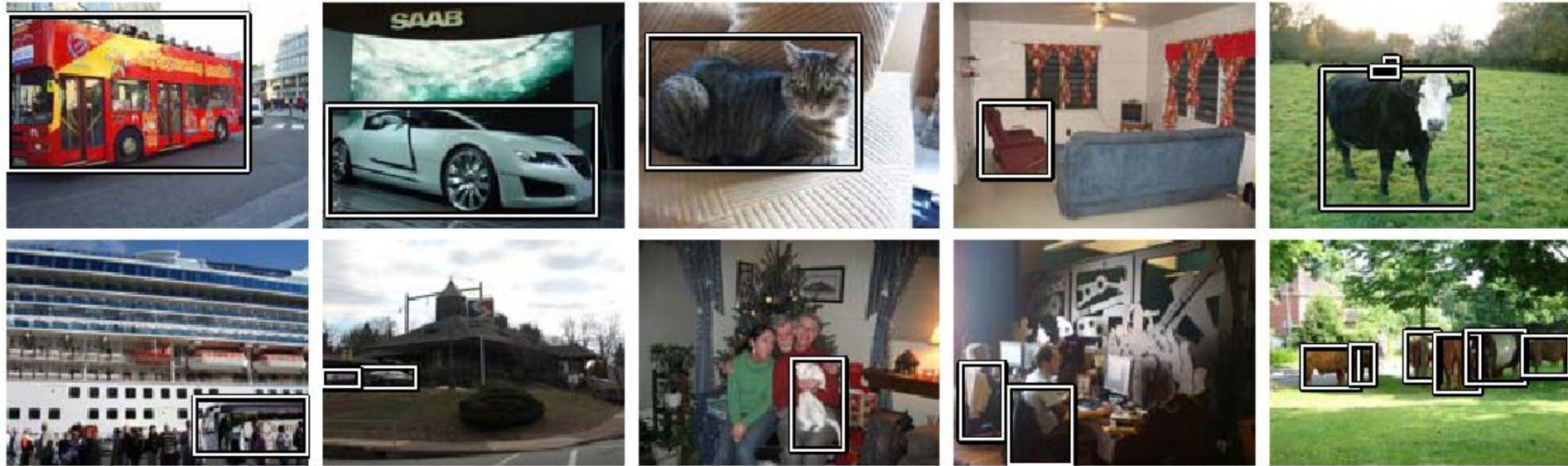
# Object Detection

- **Problem:** Detecting and localizing generic objects from various categories, such as cars, people, etc.
- **Challenges:**
  - Illumination,
  - viewpoint,
  - deformations,
  - Intra-class variability



# Object Detection Benchmarks

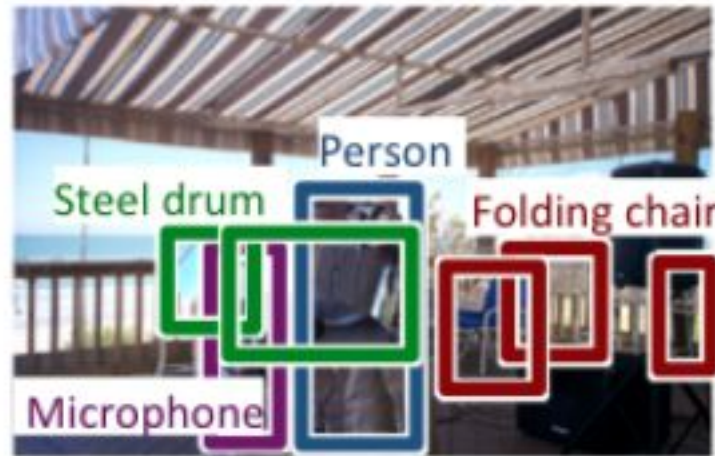
- PASCAL VOC Challenge



- 20 categories
- Annual classification, detection, segmentation, ... challenges

# Object Detection Benchmarks

- PASCAL VOC Challenge
- ImageNet Large Scale Visual Recognition Challenge (ILSVRC)
  - 200 Categories for detection



# Object Detection Benchmarks

- PASCAL VOC Challenge
- ImageNet Large Scale Visual Recognition Challenge (ILSVR)
- Common Objects in Context (COCO)
  - 80 Object categories



# How do we evaluate object detection?



— predictions  
— ground truth

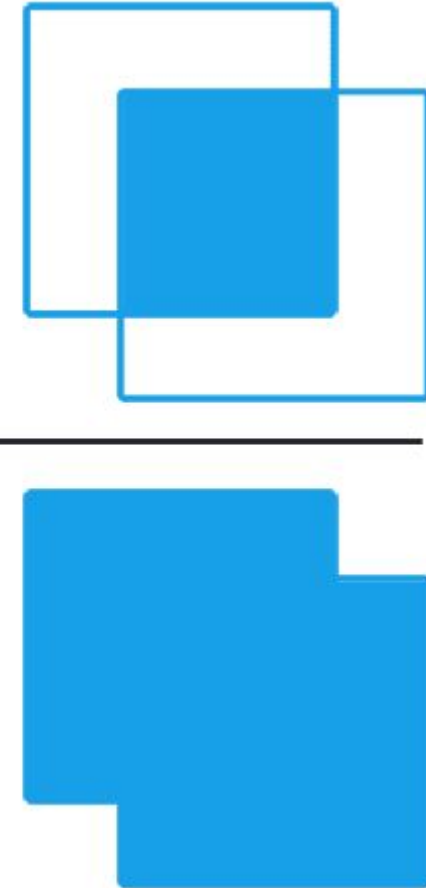
# Defining what is a good versus bad detection

IoU is a metric used to decide good from bad predictions.

Given a predicted box and ground truth box:

IoU = **intersection** between the two boxes **over** (divided by) the **union** of the two

$$\text{IoU} = \frac{\text{Area of Overlap}}{\text{Area of Union}}$$

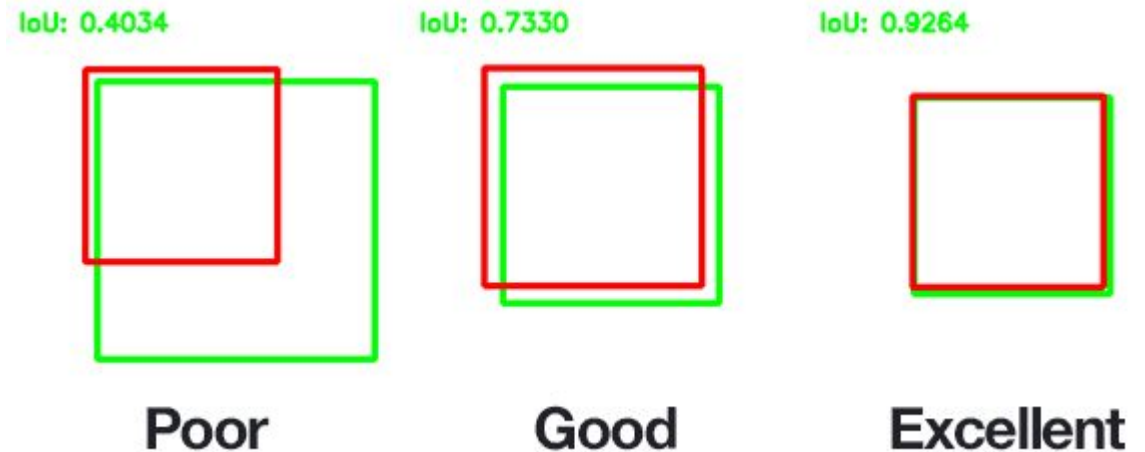




# Defining what is a good versus bad detection

We say a prediction was good if it has  $\text{IoU} > 0.5$  with any of the ground truth boxes

0.5 is a threshold that is generally accepted as a good heuristic.



# How do we evaluate object detection?



— predictions  
— ground truth

## True positive:

- The overlap of the prediction with the ground truth is **MORE than 0.5**

# How do we evaluate object detection?



— predictions  
— ground truth

**True positive:**

**False positive:**

- The overlap of the prediction with the ground truth is **LESS than 0.5**

# How do we evaluate object detection?



— predictions  
— ground truth

**True positive:**

**False positive:**

**False negative:**

- The objects that our model doesn't find

# How do we evaluate object detection?



— predictions

— ground truth

**True positive:**

**False positive:**

**False negative:**

- The objects that our model doesn't find

What is a **True Negative**?

|               | <u>Predicted 1</u> | <u>Predicted 0</u> |
|---------------|--------------------|--------------------|
| <u>True 1</u> | true<br>positive   | false<br>negative  |
| <u>True 0</u> | false<br>positive  | true<br>negative   |

$$precision = \frac{TP}{TP + FP}$$

$$recall = \frac{TP}{TP + FN}$$

# How do we evaluate object detection?



— predictions  
— ground truth

**True positive: 1**

**False positive: 2**

**False negative: 1**

**Q. What is the precision?**

# How do we evaluate object detection?



— predictions  
— ground truth

**True positive: 1**

**False positive: 2**

**False negative: 1**

Q. What is the precision?

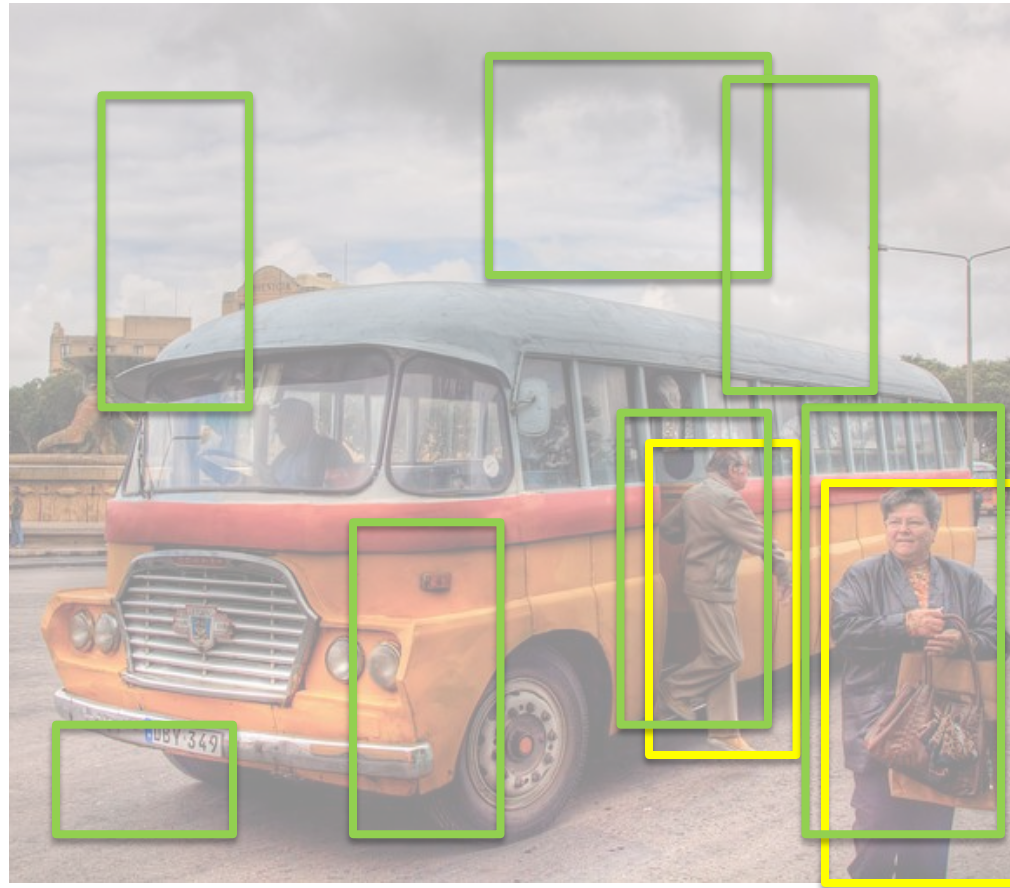
Q. What is the recall?



# How to intuitively understand precision versus recall

- Precision:
  - how many of the **predicted detections** are correct?
- Recall:
  - how many of the **ground truth objects** are detected?

In reality, our model makes a lot of predictions with varying scores between 0 and 1



— predictions  
— ground truth

Here are all the boxes that are predicted with **score > 0**.

From this, we see that:

- Recall is perfect!
- But our precision is BAD!

# How do we evaluate object detection?



— predictions  
— ground truth

Here are all the boxes that are predicted with **score > 0.5**

We are using a **threshold of 0.5**

**Q. What happens to precision if threshold is high?**

# How do we evaluate object detection?



— predictions

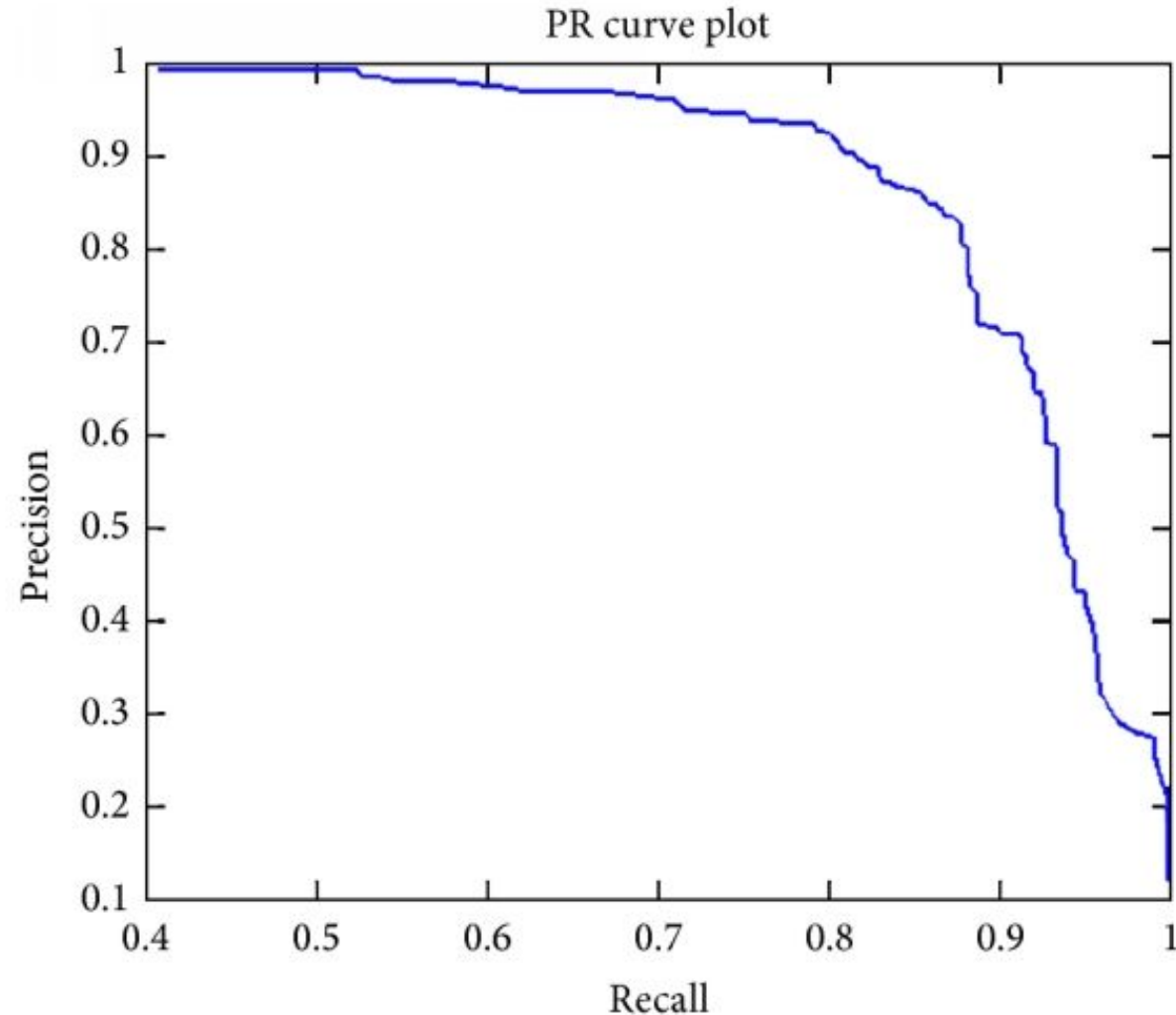
— ground truth

Here are all the boxes that are predicted with **score > 0.5**

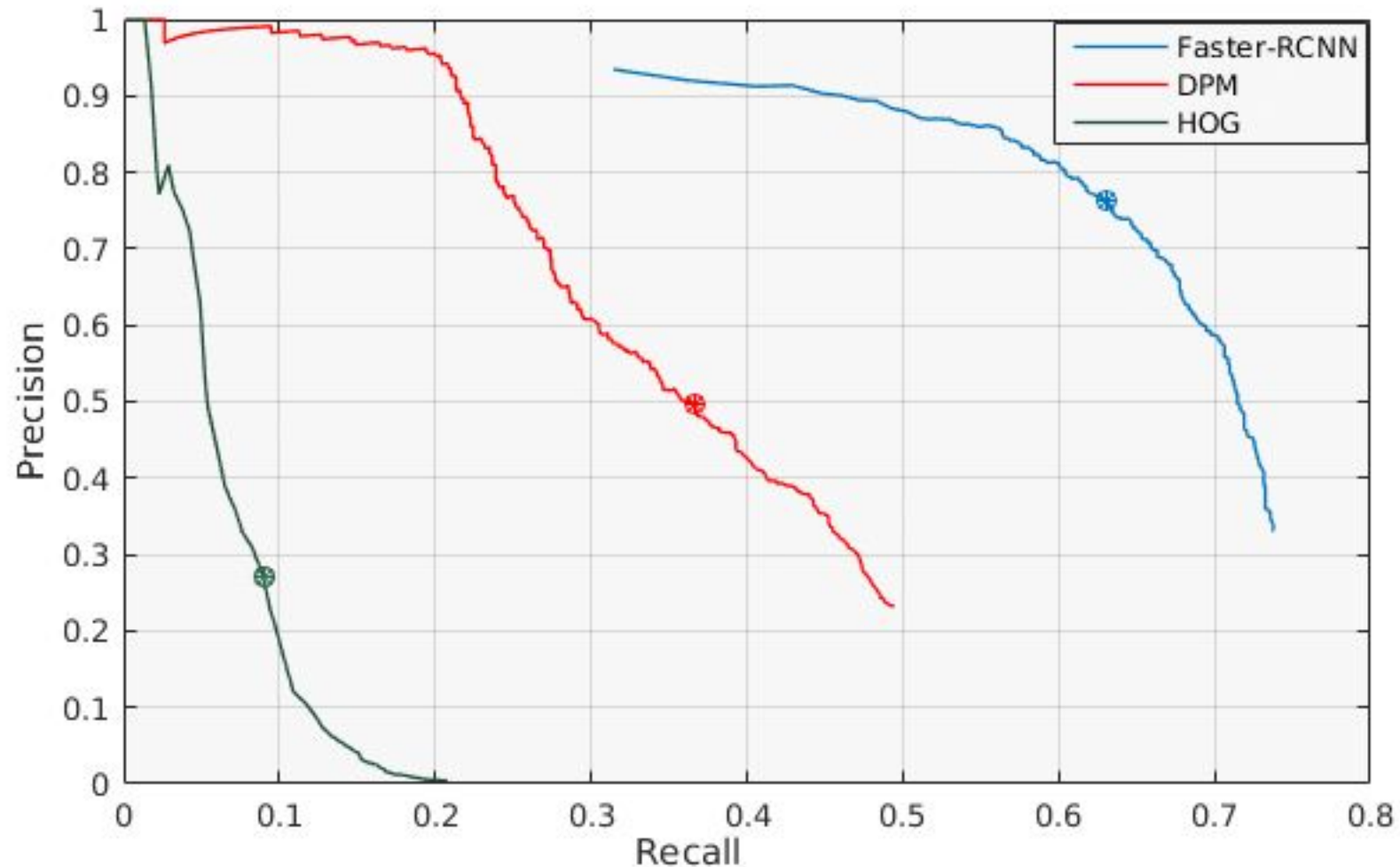
We are using a **threshold of 0.5**

**Q.** What happens to **recall** if threshold is high?

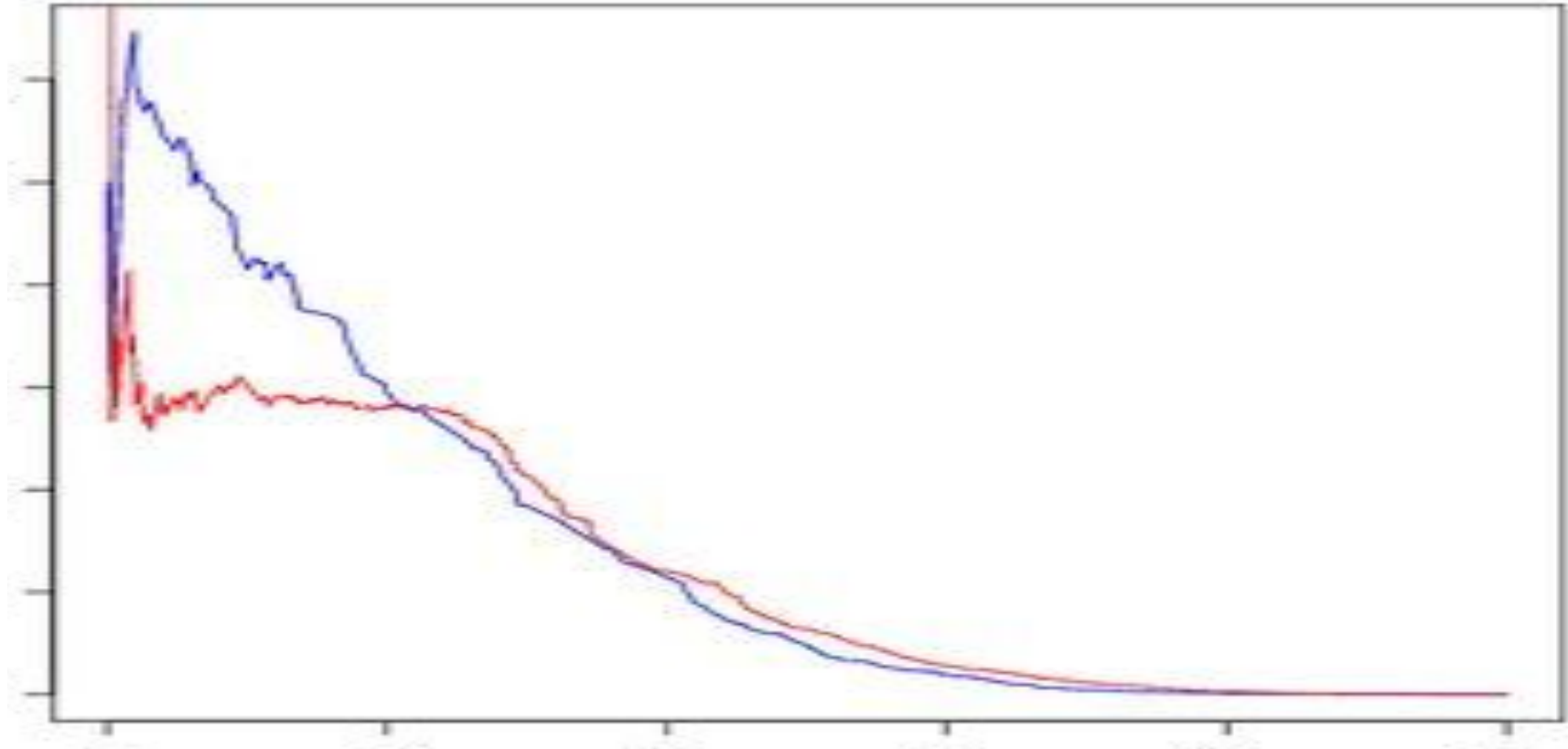
# Precision – recall curve (PR curve)



# Which model is the best?



# Which model is the best?



# True positives - detecting **person**

UoCTTI\_L SVM-MDPM



MIZZOU\_DEF-HOG-LBP



NECUIUC\_CLS-DTCT



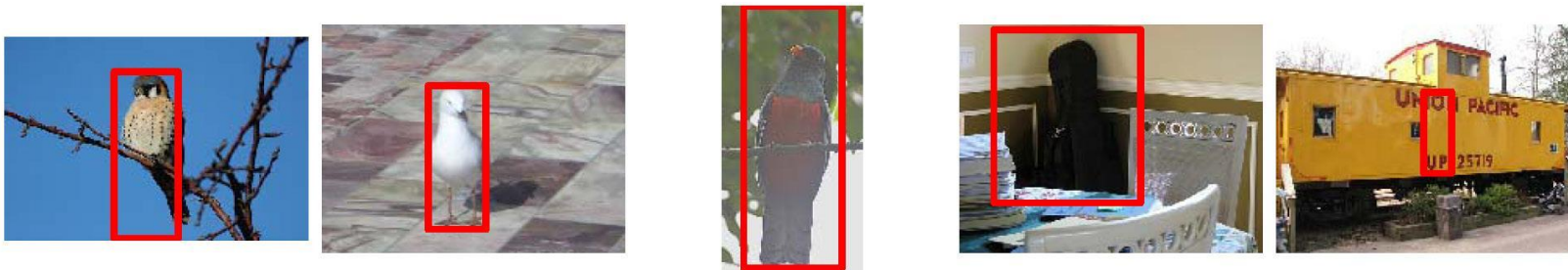


# False positives - detecting person

UoCTTI\_LSVM-MDPM



MIZZOU\_DEF-HOG-LBP



NECUIUC\_CLS-DTCT



# Near misses: IoU falls short of 0.5

UoCTTI\_LSYM-MDPM



MIZZOU\_DEF-HOG-LBP



NECUIUC\_CLS-DTCT



# True positives - detecting **bicycle**

UoCTTI\_LSVM-MDPM



OXFORD\_MKL



NECUIUC\_CLS-DTCT



# False positives - detecting **bicycle**

UoCTTI\_LSVM-MDPM



OXFORD\_MKL



NECUIUC\_CLS-DTCT



# Today's agenda

- Object detection
  - Task and evaluation
- **A simple detector**
- Deformable parts model

# Dalal-Triggs method



sliding window

# At every patch as the window slides

1. Convert the image patch into your favorite feature representation
  - a. For example:
    - i. HoG,
    - ii. HoG with PCA,
    - iii. RGB with LDA,
    - iv. Bag of words on RGB
    - v. etc.
2. Use a trained classifier to determine if it is a specific class
  - a. e.g. kNN classifier
3. Accumulate the predictions over all the patches

# Sliding window + hog features



- Slide through the image and check if there is an object at every location

No person here



# Sliding window + hog features



- Slide through the image and check if there is an object at every location

YES!! Person match found

# Sliding window + hog features



- But what if we were looking for buses?

No bus found

# Sliding window + hog features



- But what if we were looking for buses?

No bus found

# Sliding window + hog features



- We will never find the object if we don't choose our window size wisely!

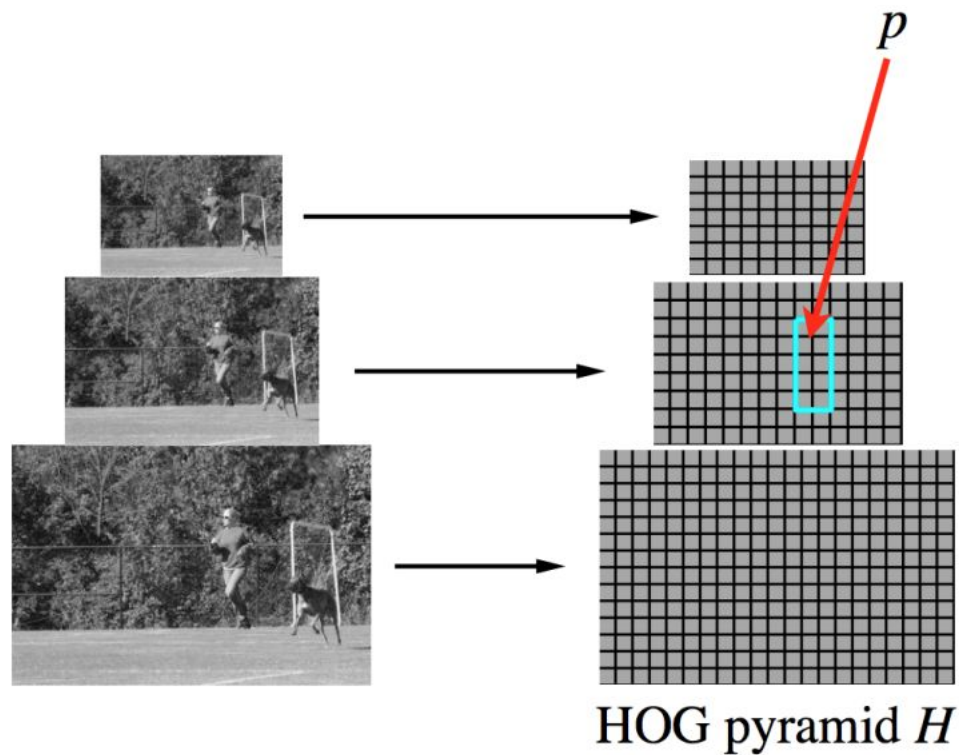
No bus found

# Sliding window + hog features



- We need to do **multi-scale** sliding windows with pyramids

Computationally, we first resize the image to different sizes and then extract features at each size.



# Today's agenda

- Object detection
  - Task and evaluation
- A simple detector
- Deformable parts model

## Recap – bag of words

- We can present images as a set of “words”
  - Where each word represents a **part** of the image.

Bag of ‘words’

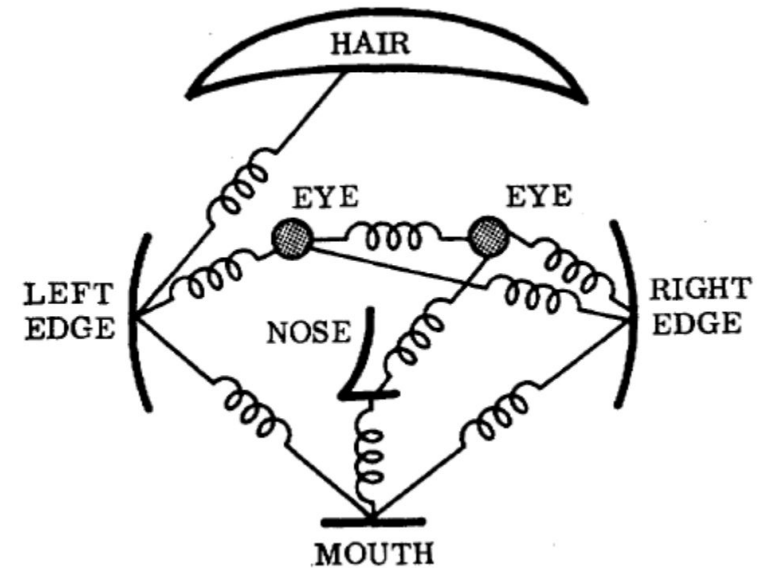


- Can we use the location of these patches to find objects within those images?



# Deformable Parts Model

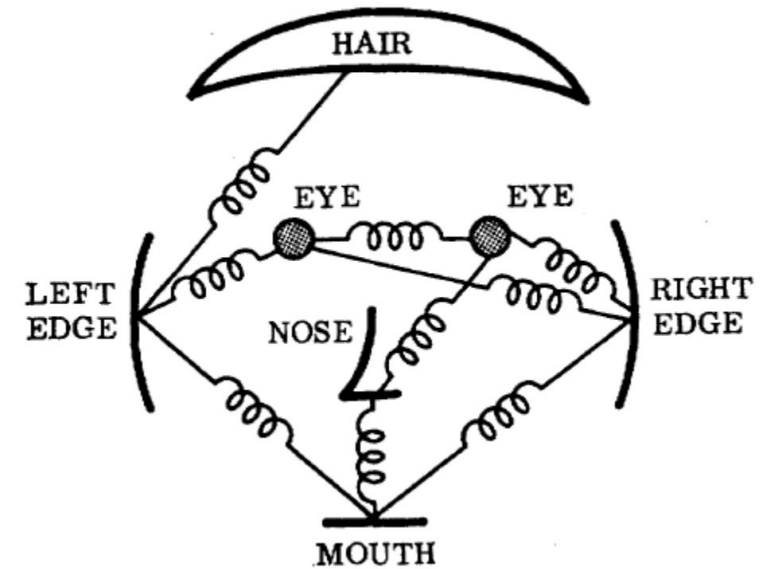
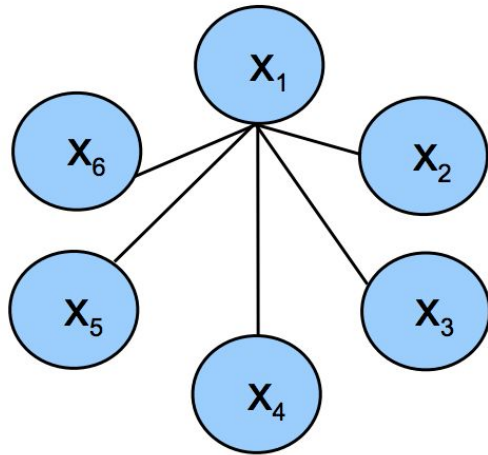
- Represents an object as a “collection of parts” arranged in a “deformable configuration”
- Each part represents local appearances
- Spring-like connections between certain pairs of parts



Fischler and Elschlager, Pictoral Structures, 1973

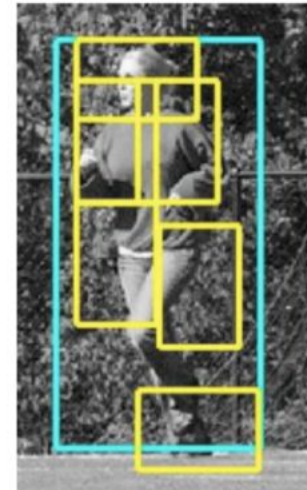
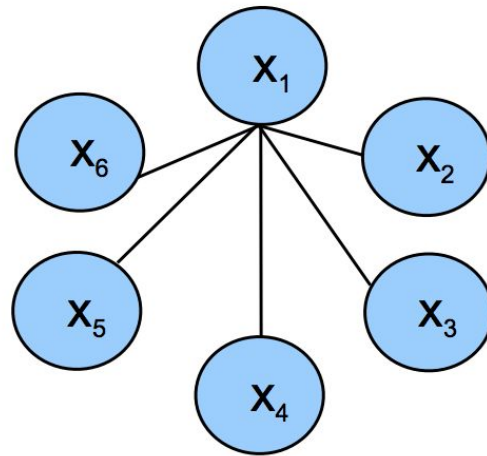
# Deformable parts model

- The parts of an object form pairwise relationships.
- We can model this using a “star model”
  - where every part is defined relative to a root.



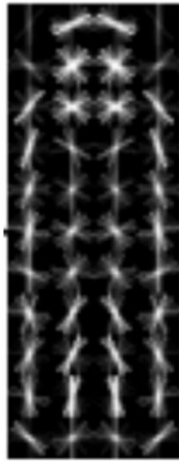
# Detecting a person with their parts

- For example, a person can be modelled as having a head, left arm, right arm, etc.
- All parts can be modelled relative to the global person detector, which acts as the root.

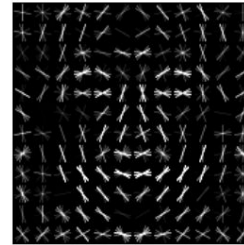


# Deformable parts model

- Each model will have a **global** filter. And a set of **part** filters. Here is an example of a global person filter with it's 'head' part filter:

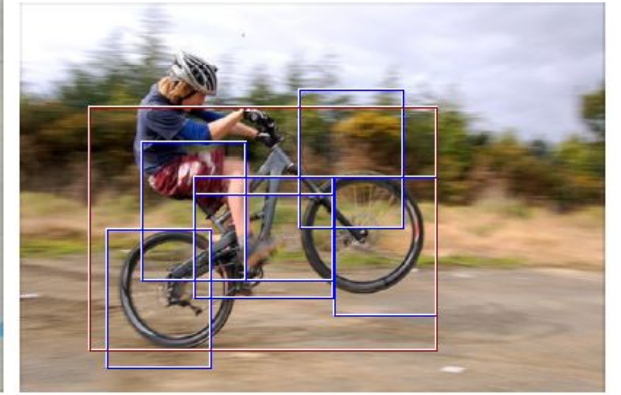
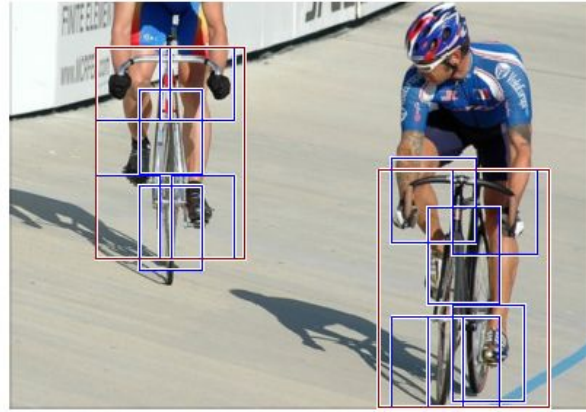


Global/root  
filter



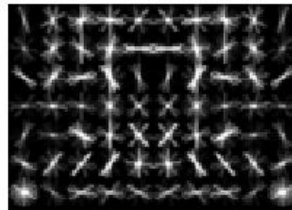
Part filter

# 5-part bicycle model

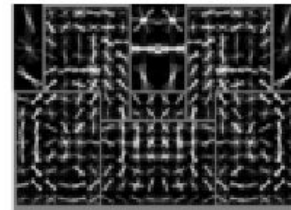


“side view” bike  
model component

Root filter

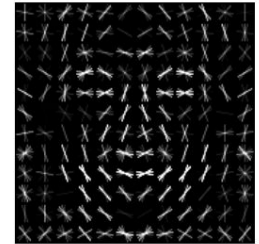
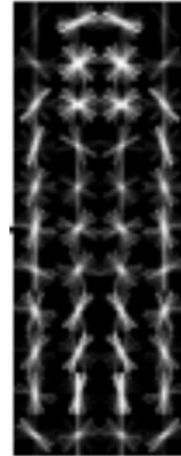


Part filters

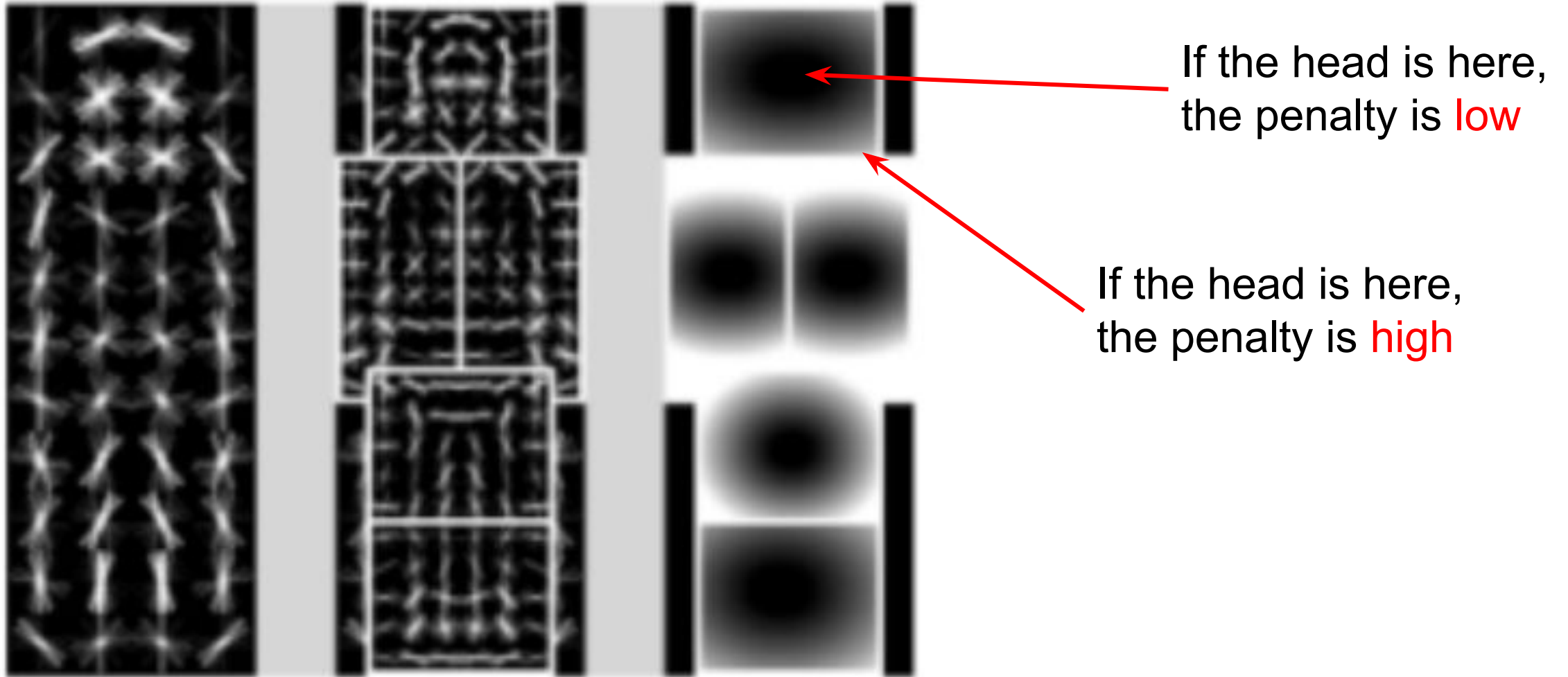


# Deformable parts model

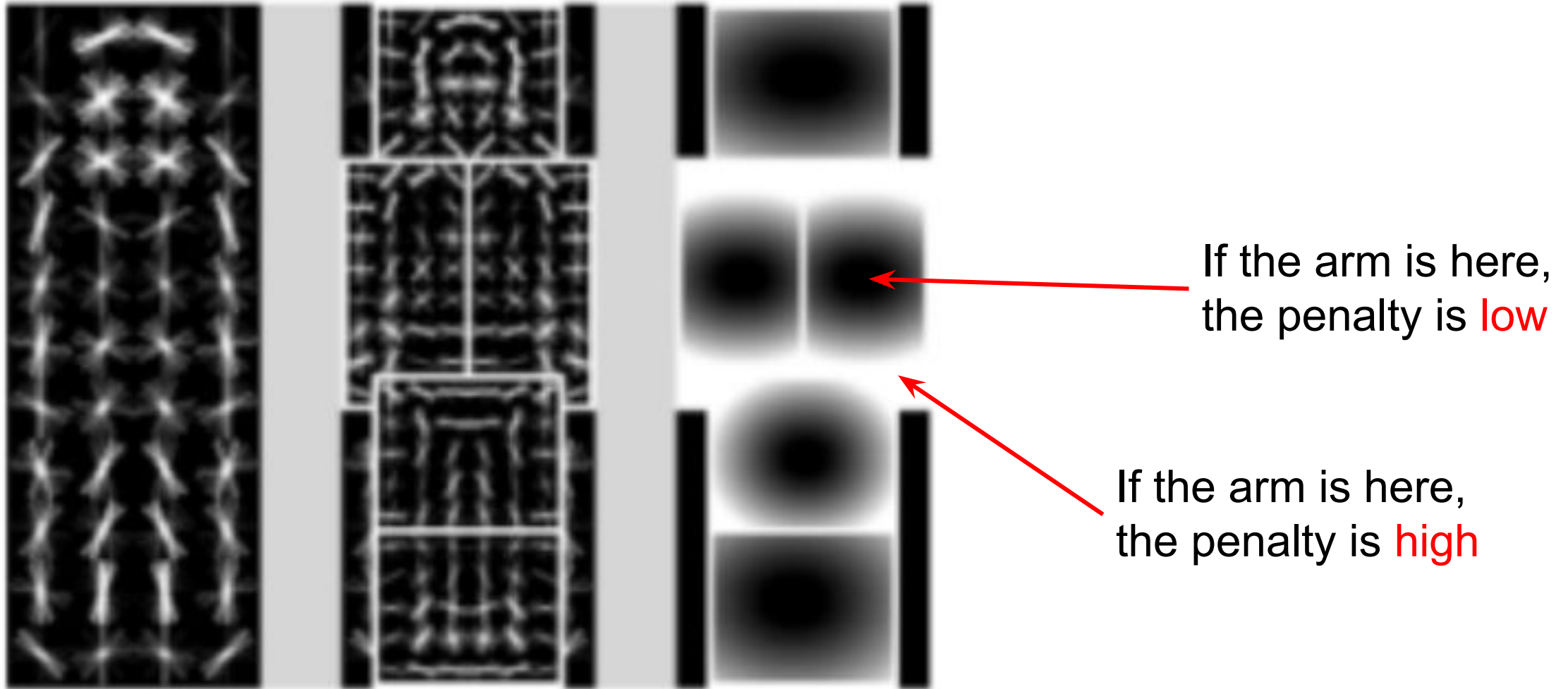
- Mixture of deformable part models
- Each component has global component + deformable parts
- Part filters have finer details



# DPM for person model with 5 parts

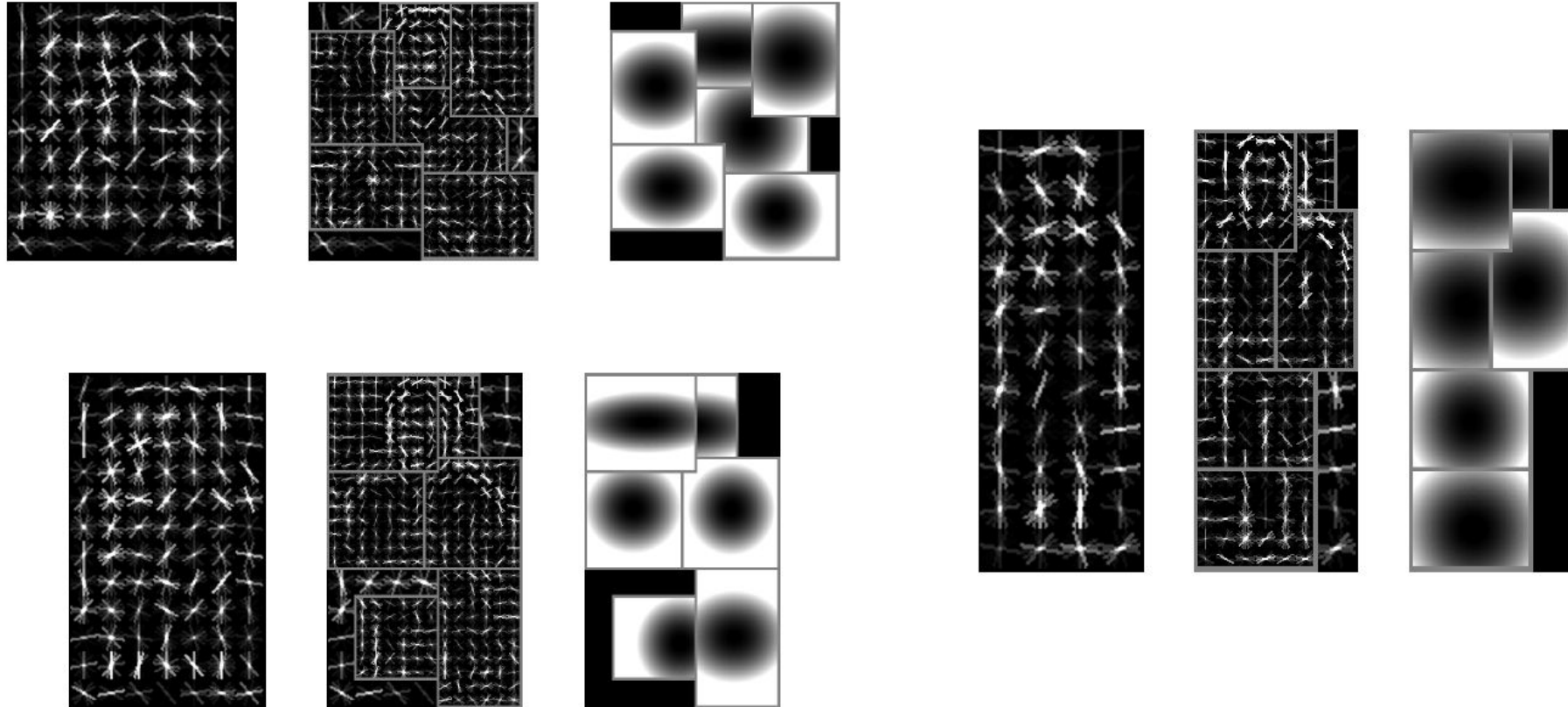


# DPM for person model with 5 parts



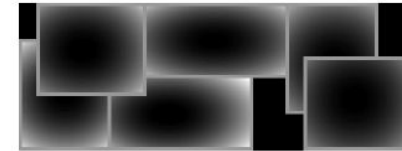
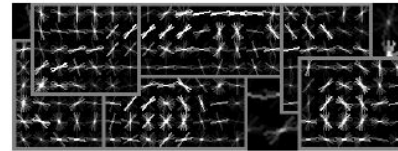
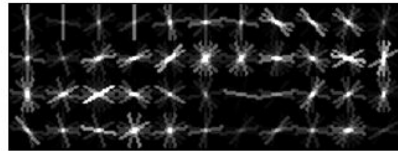
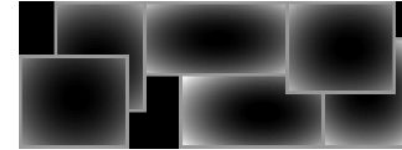
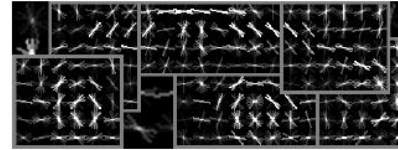
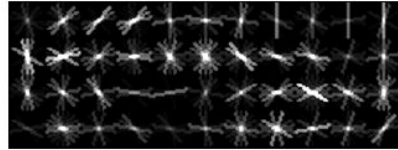


# Multiple DPM for person model with 6 parts

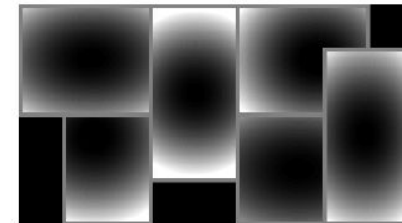
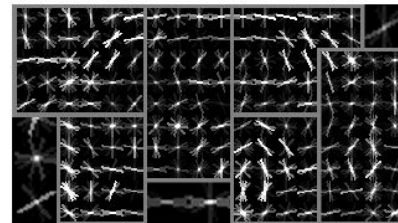
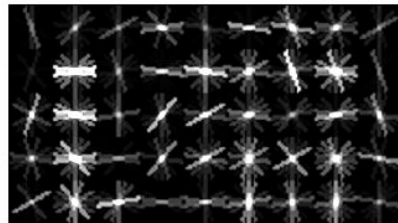
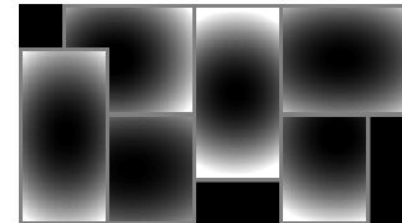
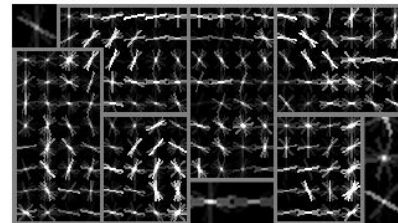
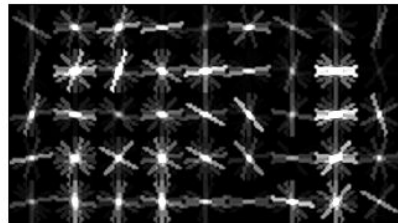


# DPM for car with 6 parts

side view



frontal view



root filters (coarse)

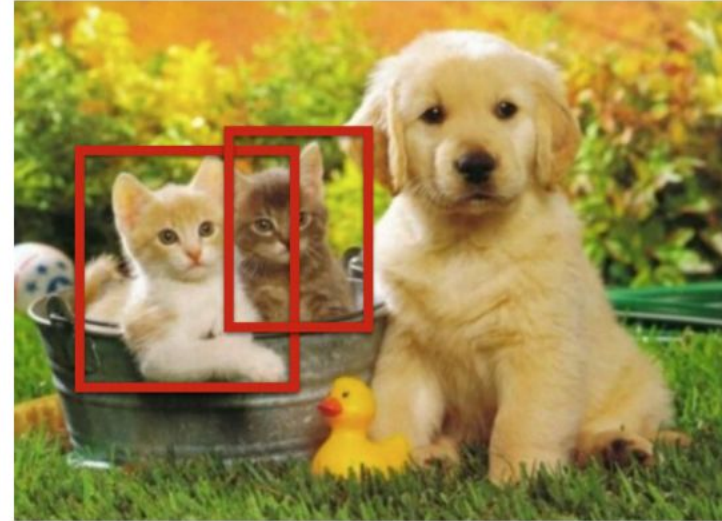
part filters (fine)

deformation models

# How do we use the parts to make a detection?

Intuition:

1. First, use the sliding windows at different pyramid scales to detect each part (and the root).
2. Each part gives you a score for where the person might be
3. Accumulate the global and part scores and penalize the deformation of the parts.

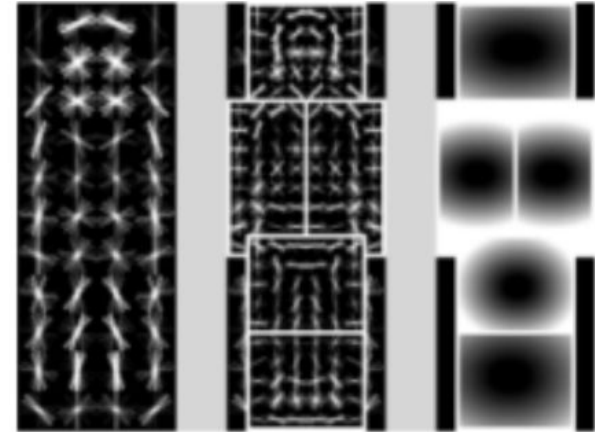


# Example for detecting people



Image input

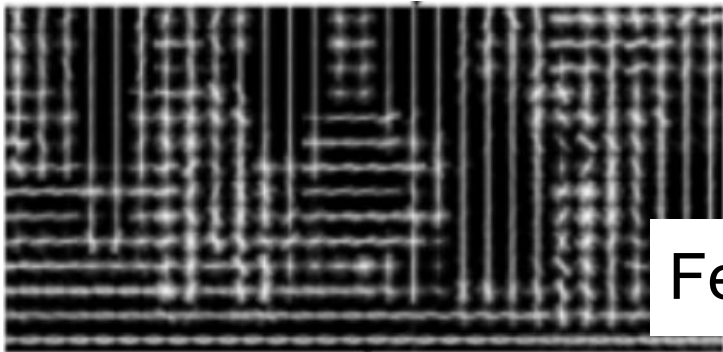
A feature  
template for  
person



# First extract features

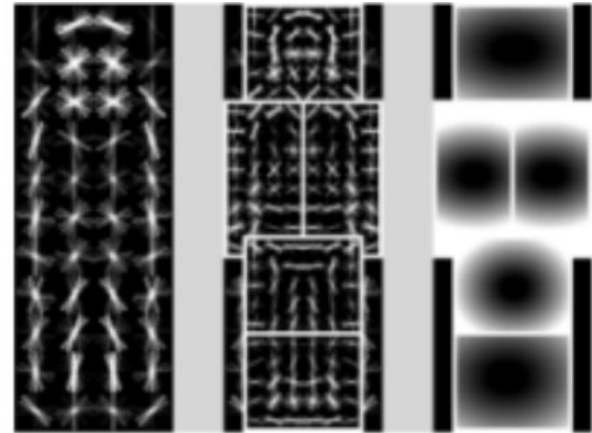


Image input



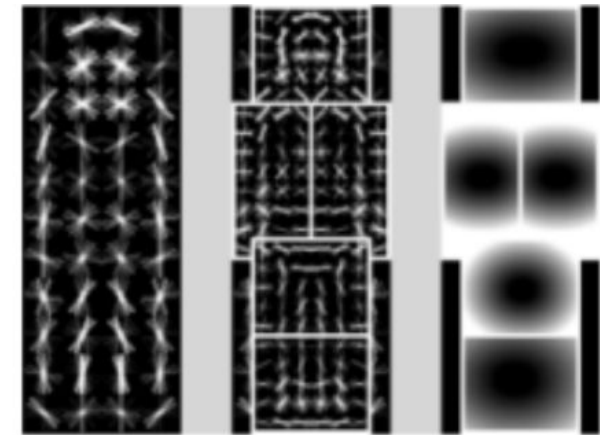
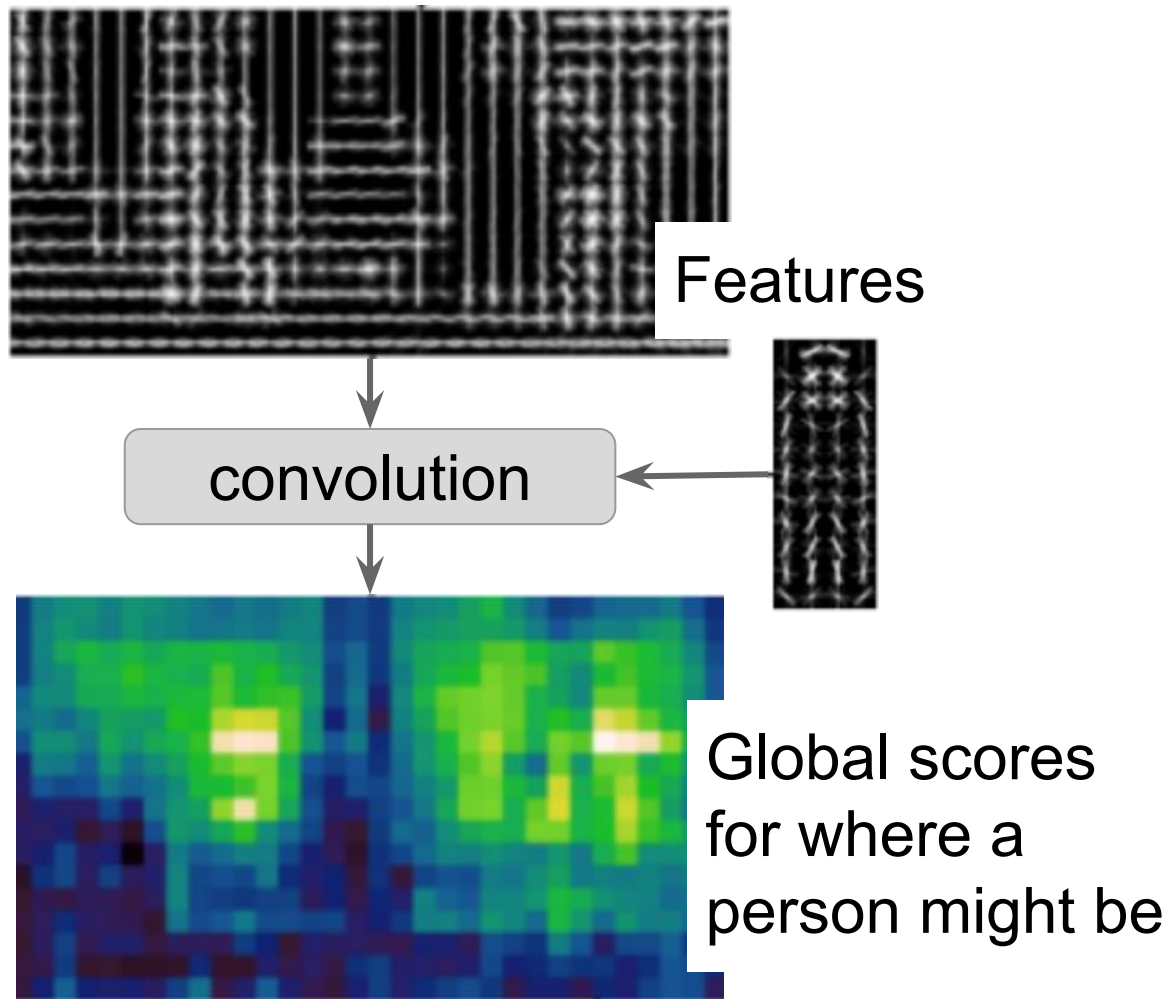
Features

A feature template for person

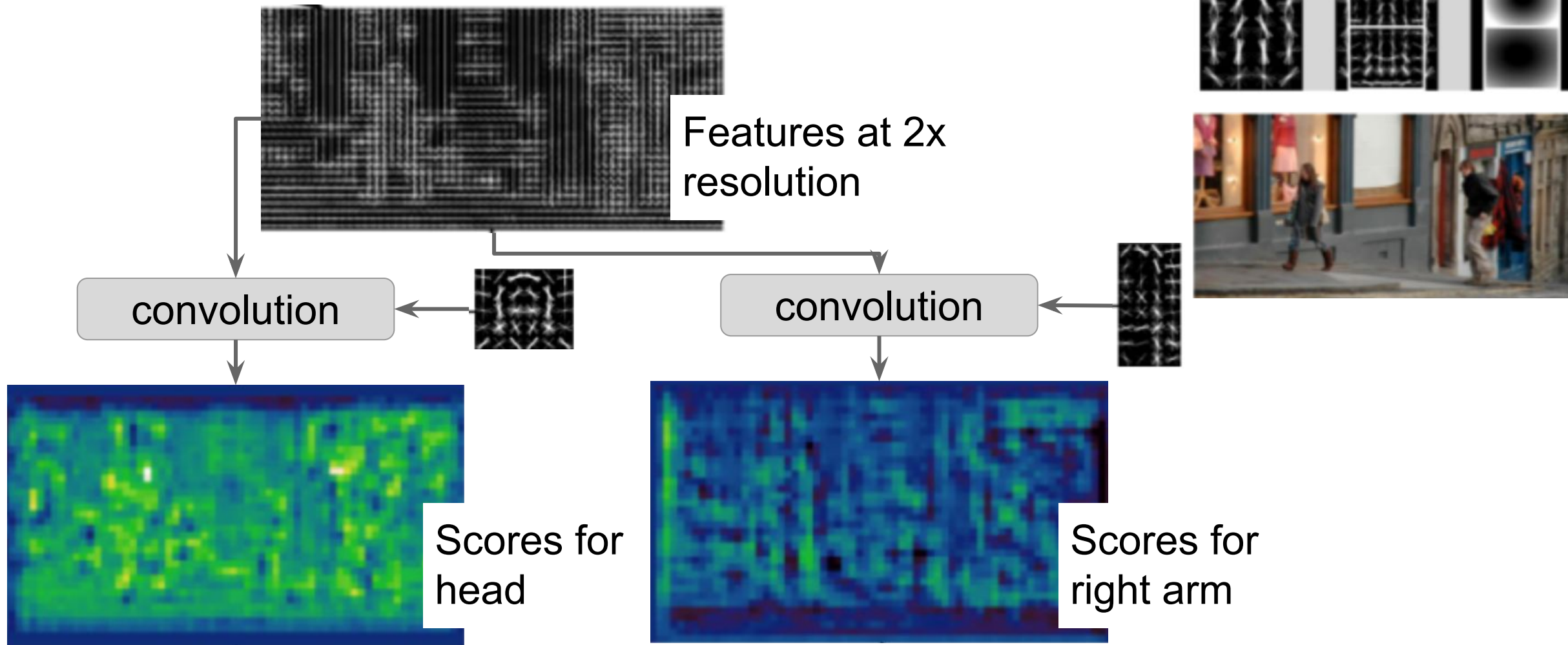


Features at 2x resolution

# Calculate scores for **part** templates

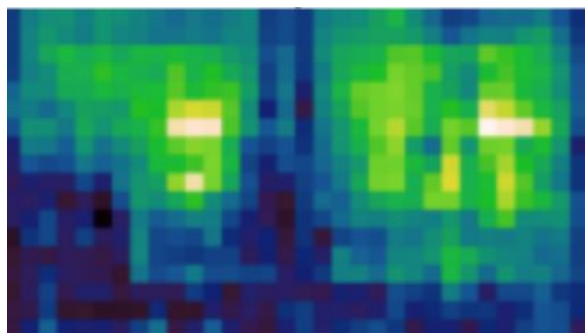


# Calculate scores for global template

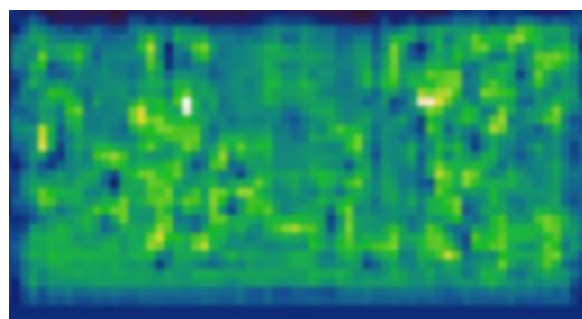


After step 1, we have scores for all parts and global template

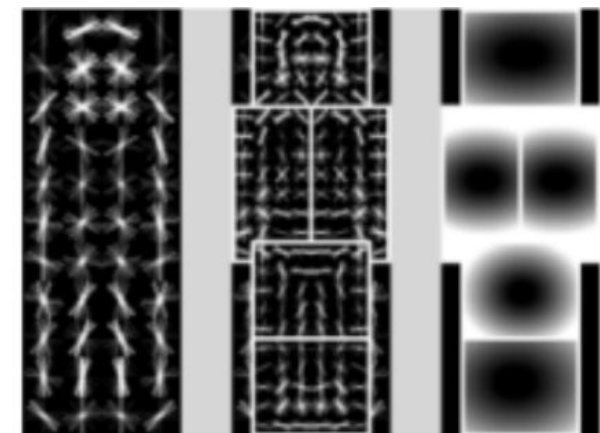
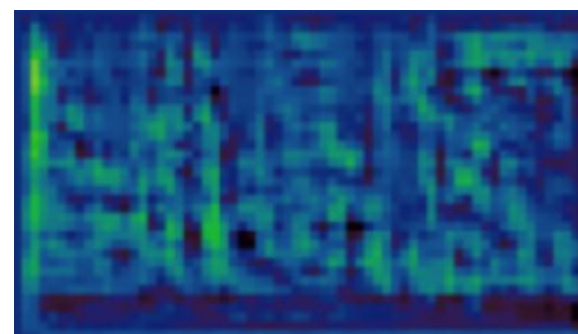
Global scores



Scores for head

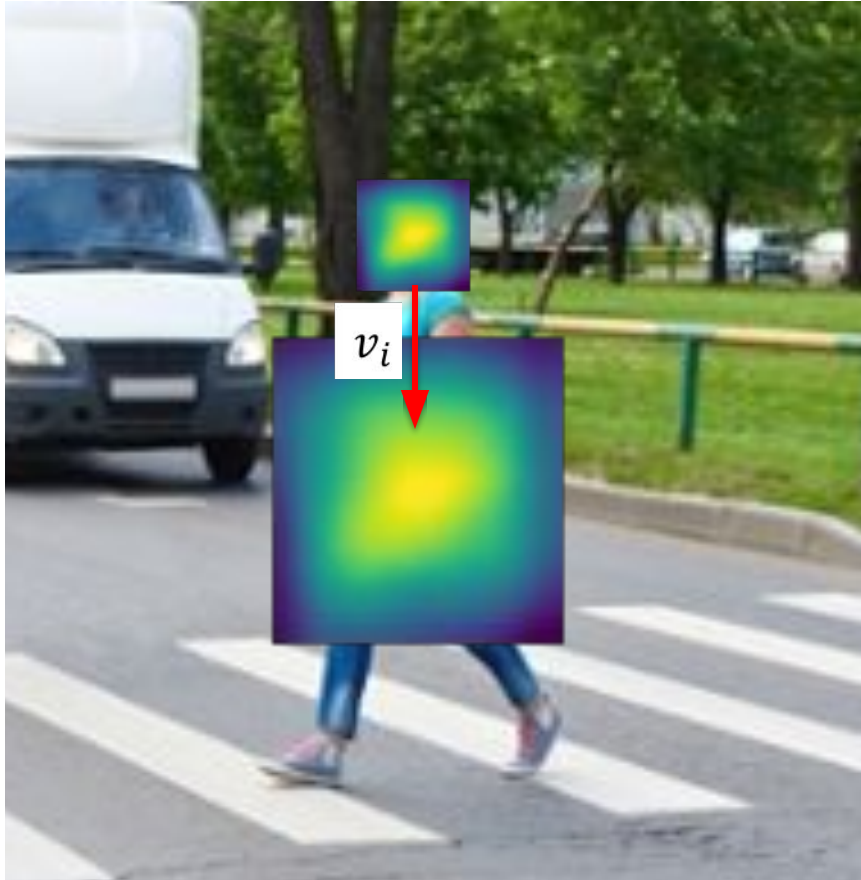


Scores for right arm





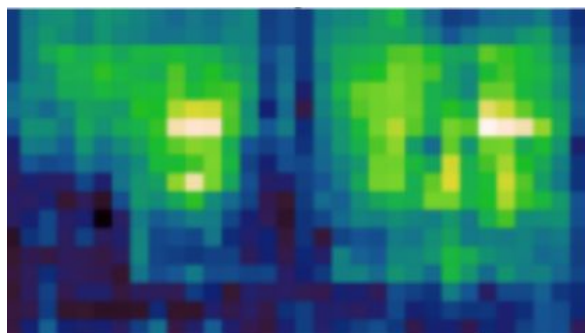
# Allowing each part to deform and guess where the entire body is.



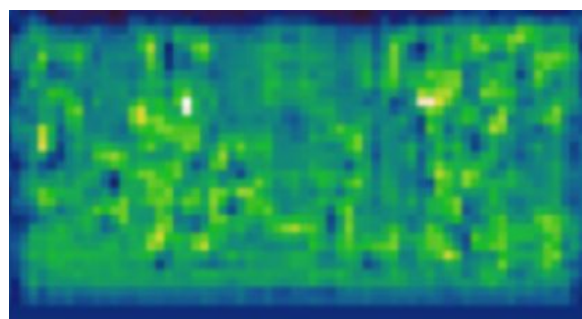
- Given the location for the detected head, we can guess where the body should be.
- The body should be in the direction ( $v_i$ ) predefined in the model
- Bodies can be of different sizes and shapes. So we allow it to deform by some variable  $d_i$
- This deformation spreads the scores to potential locations of the body

Step 2: each part gives you a score for where the person might be

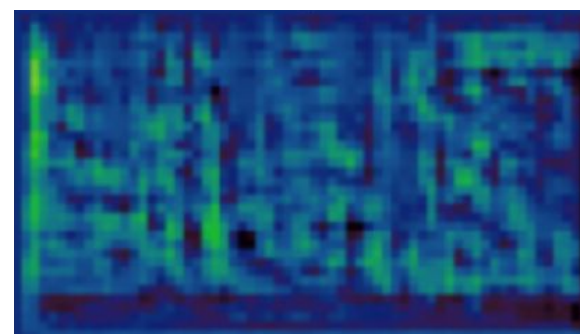
Global scores



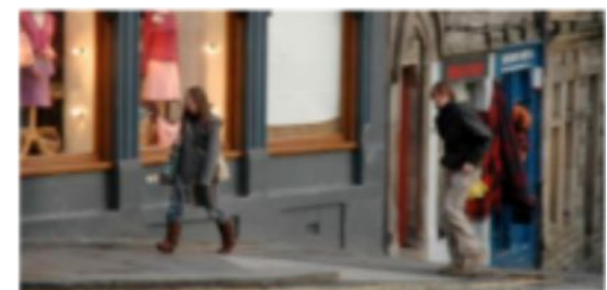
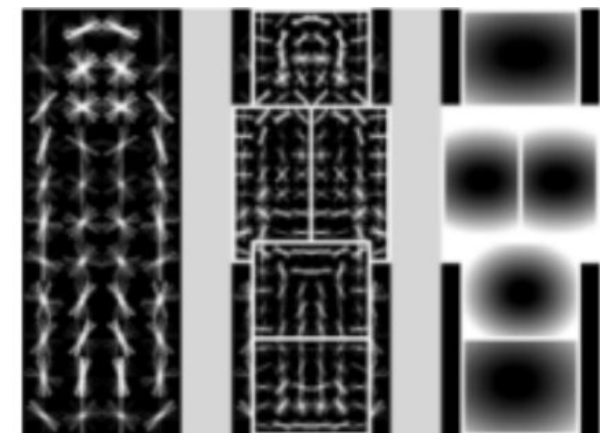
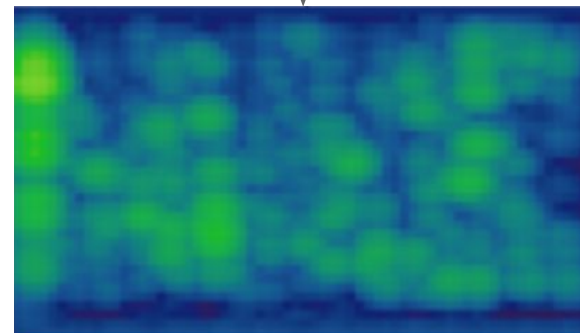
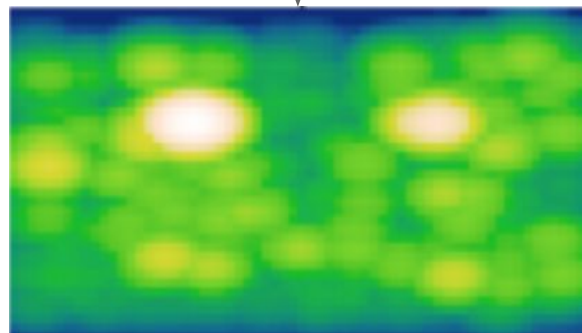
Scores for head



Scores for right arm



Each part is allowed to deform. So it deforms to where the person might be.



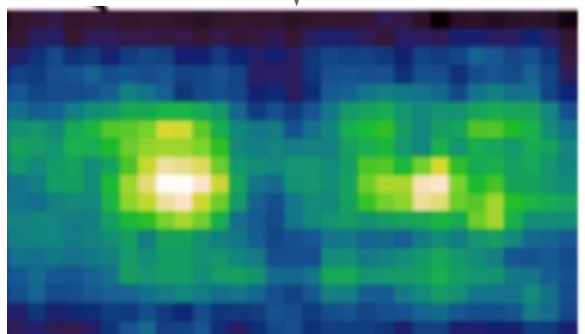
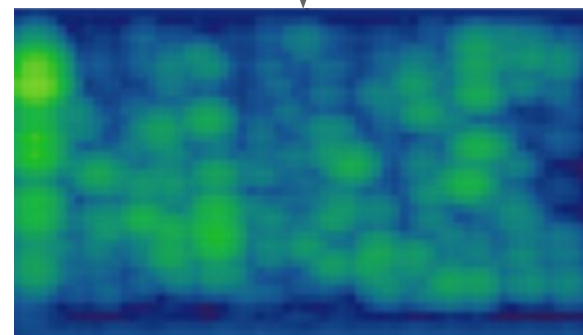
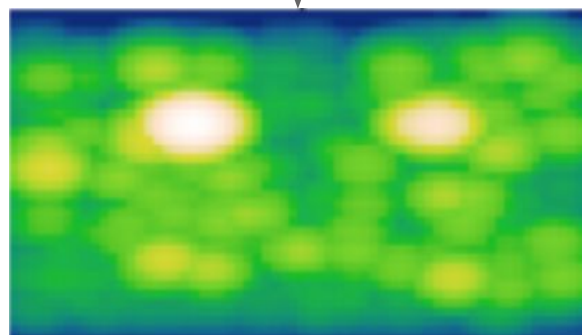
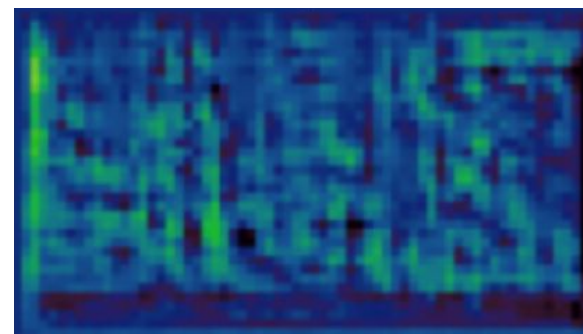
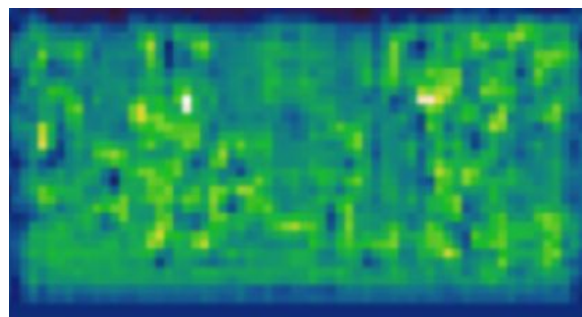
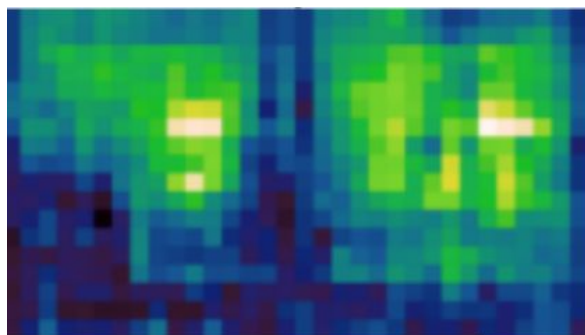
**Intuition:** If the head is here, where is the whole person likely to be?

# Step 3: Add up the scores for the final detections

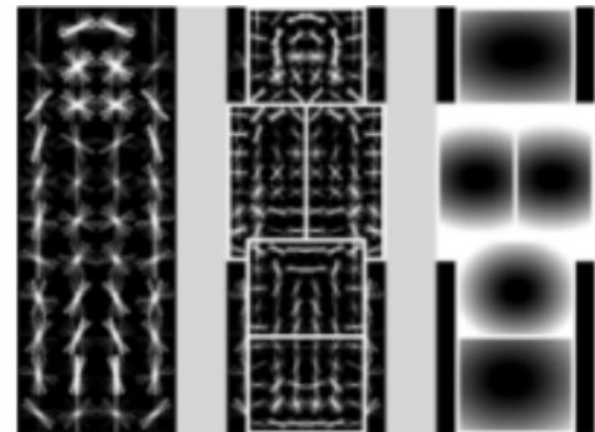
Scores for head

Scores for right arm

Global scores



Add up final scores



# Formally, DPM is defined as:

- A model for an object with  $n$  parts is a  $(n + 2)$  tuple:

$$(F_0, P_1, \dots, P_n, b)$$

Root filter      Model for 1st part      Bias term

- Each part-based model defined as:

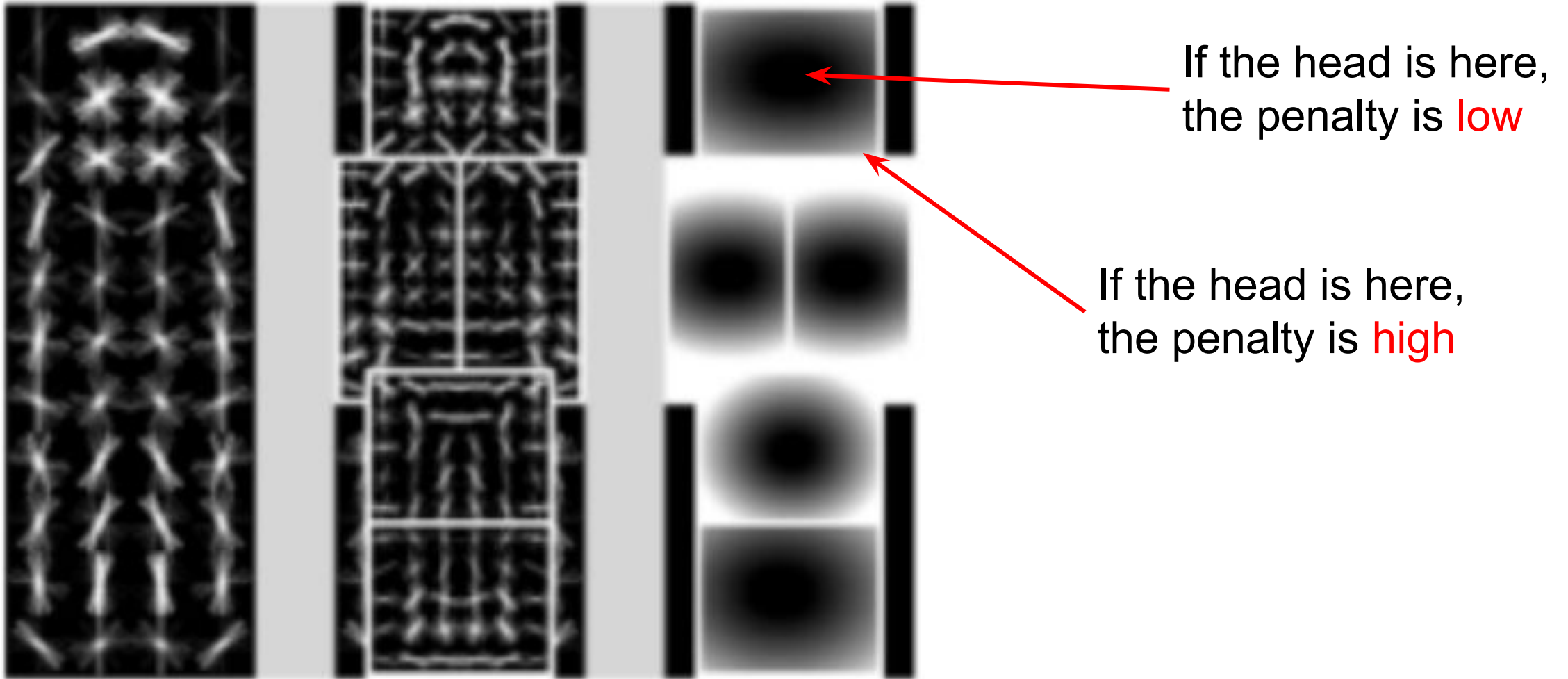
$$(F_i, v_i, d_i)$$

$F_i$  filter for the  $i$ -th part

$v_i$  “anchor” position for part  $i$  relative to the root position

$d_i$  defines a deformation cost for each possible placement of the part relative to the anchor position

$d_i$  can be defined in many ways. We will use a Gaussian filter to define it.



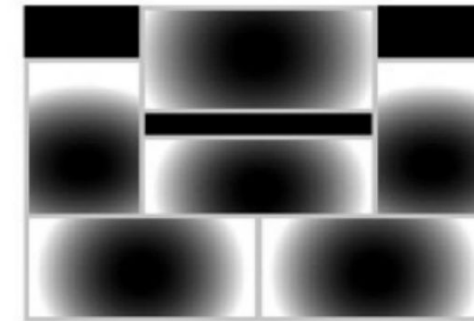
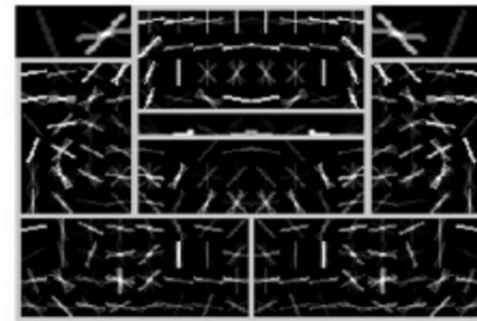
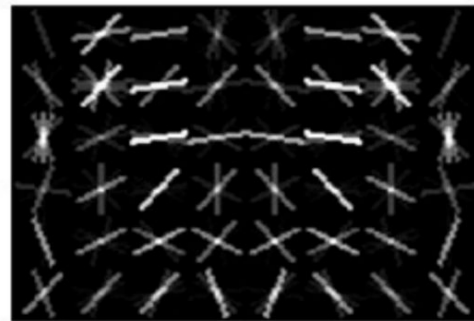
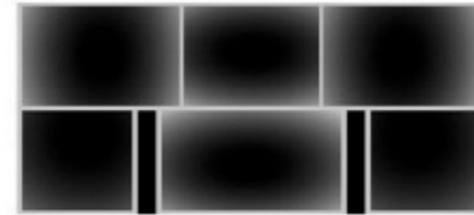
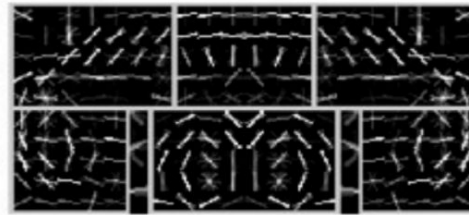
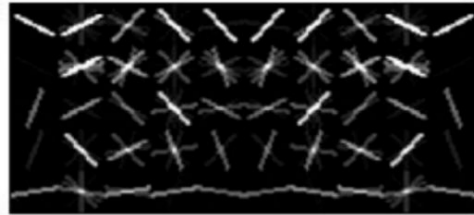
# Calculating the score for a detection

The score for a detection is defined as the **sum of scores for the global and part detectors** *minus* the **sum of deformation costs** for each part.

This means that if a detection's parts are really far away from where they should be, it's probably a false positive.



# Deformable Parts Model (DPM) - bicycle

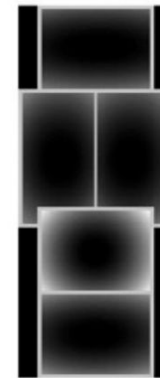
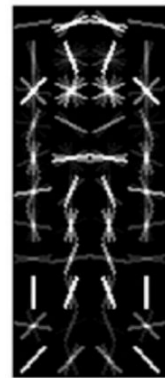
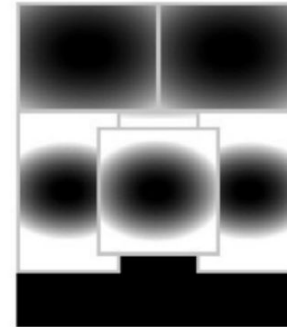
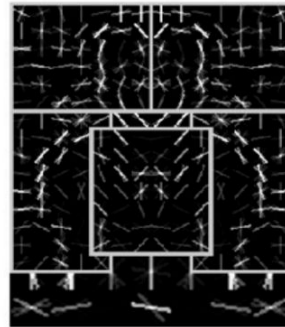
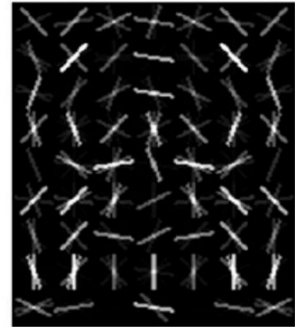


root filters  
coarse resolution

part filters  
finer resolution

deformation  
models

# DPM with HoG features - person



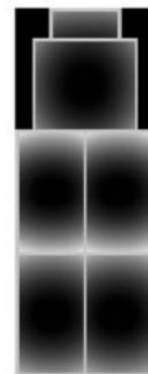
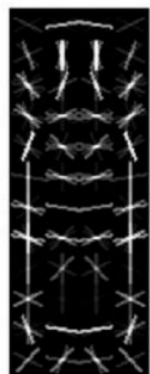
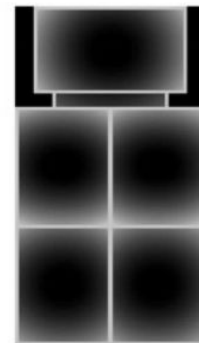
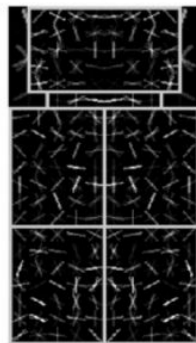
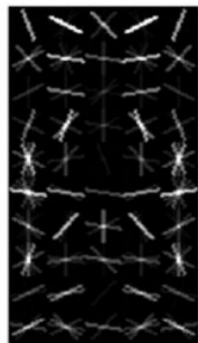
root filters  
coarse resolution

part filters  
finer resolution

deformation  
models



# DPM - bottle



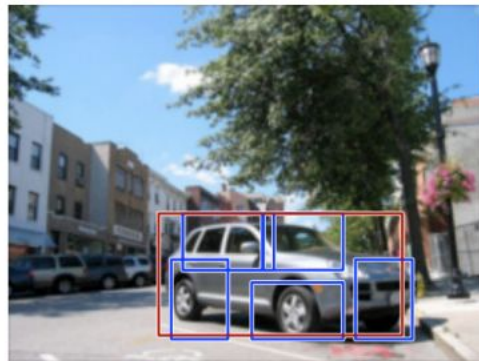
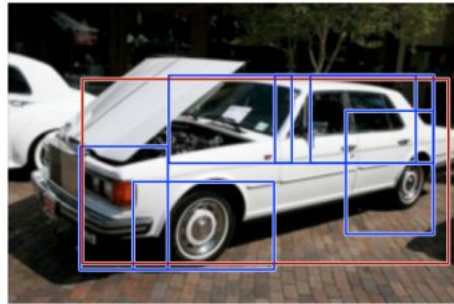
root filters  
coarse resolution

part filters  
finer resolution

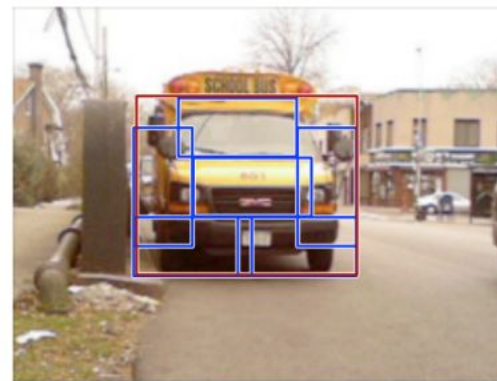
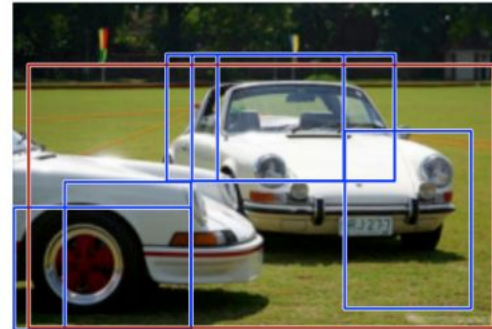
deformation  
models

# Results – car detection

high scoring true positives

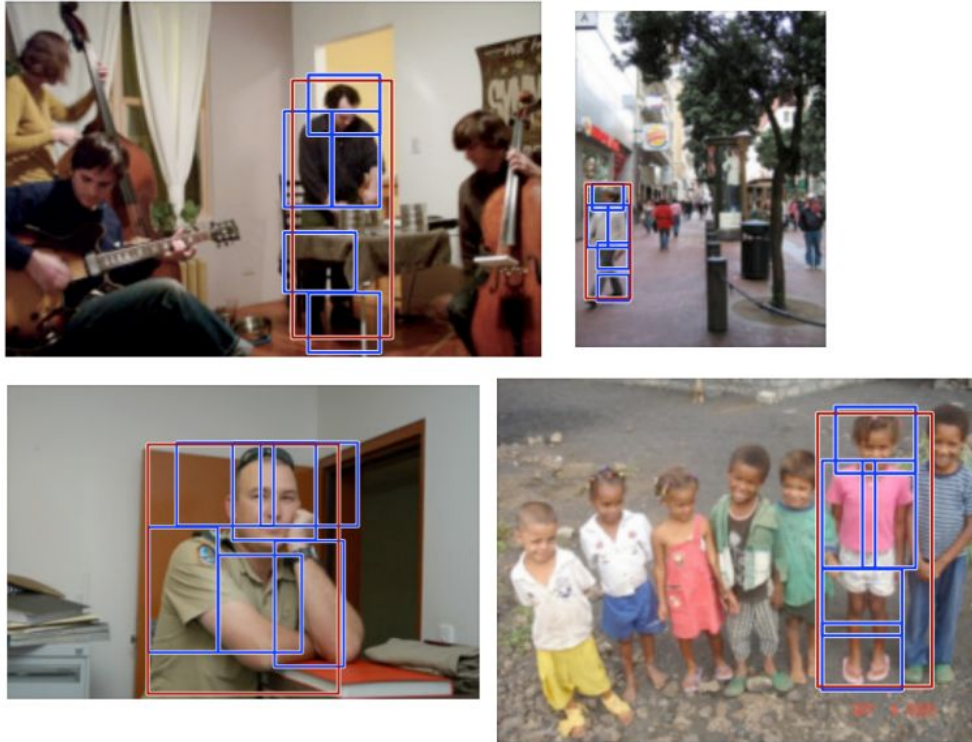


high scoring false positives

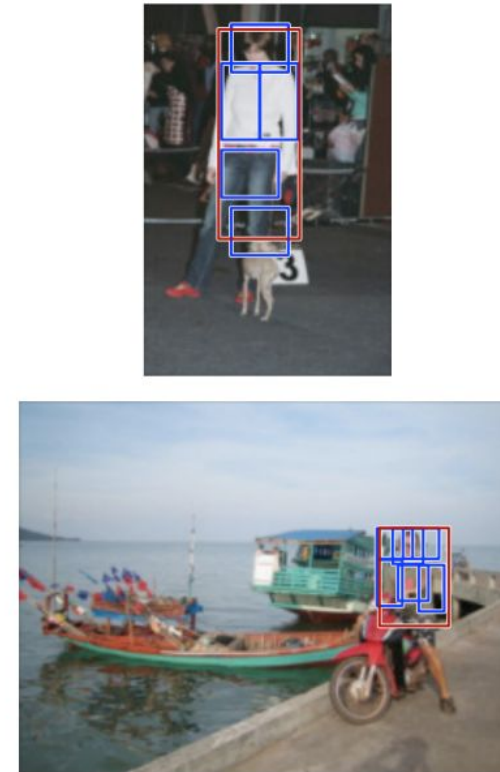


# Results – Person detection

high scoring true positives

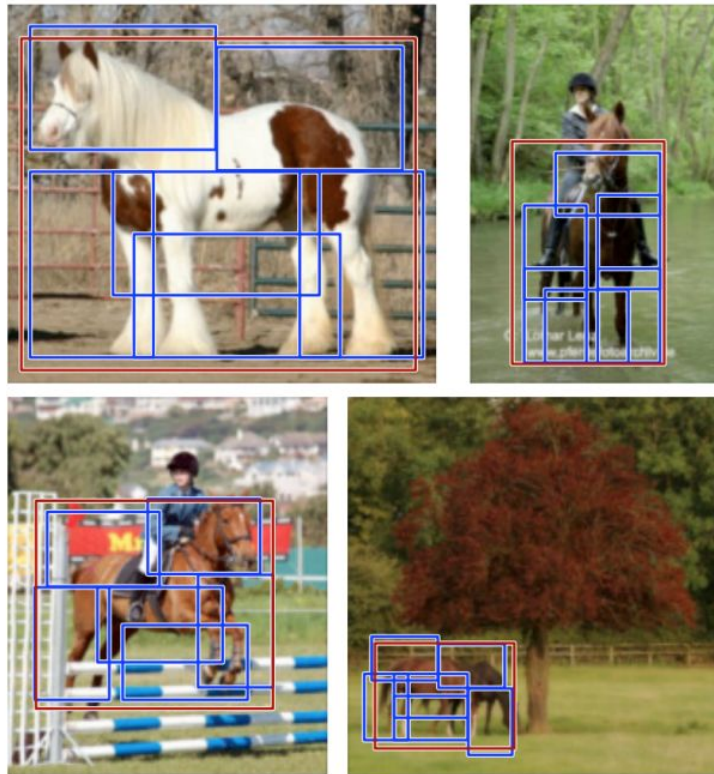


high scoring false positives  
(not enough overlap)

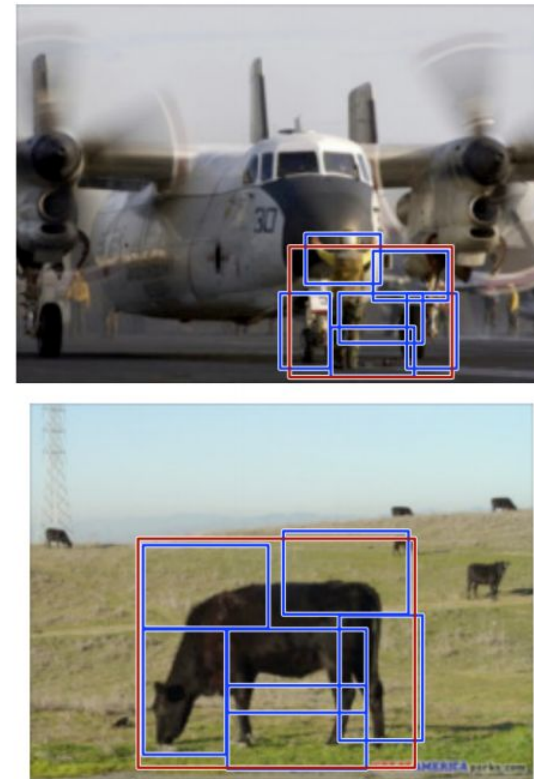


# Results – horse detection

high scoring true positives



high scoring false positives



# DPM - discussion

- **Approach**

- Manually selected set of parts - Specific detector trained for each part
- Spatial model trained on part activations
- Evaluate joint likelihood of part activations

- **Pros**

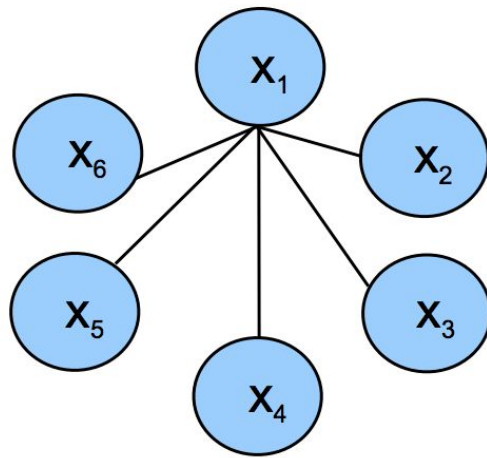
- Parts have intuitive meaning.
- Standard detection approaches can be used for each part.
- Works well for specific categories.

- **Disadvantages**

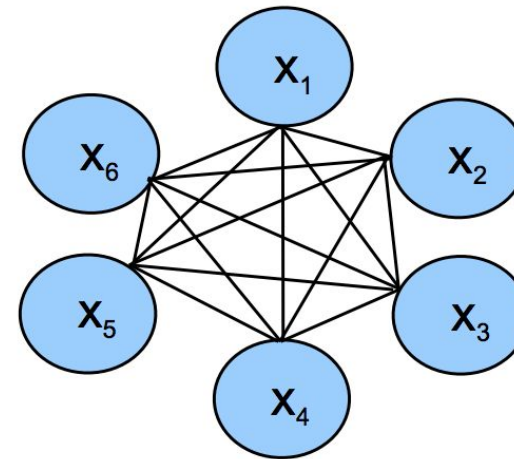
- Parts need to be selected manually
- Some parts don't have a simple appearance
- No guarantee that some important part hasn't been missed
- When adding a new category, it takes a lot of manual effort

# Extensions - From star shaped model to constellation model

“Star” shape model



Fully connected shape model



# Today's agenda

- Object detection
  - Task and evaluation
- A simple detector
- Deformable parts model

# Next lecture

Motion and Tracking



# Calculating the score for a detection

The score for a detection is defined as the **sum of scores for the global and part detectors** *minus* the **sum of deformation costs** for each part.

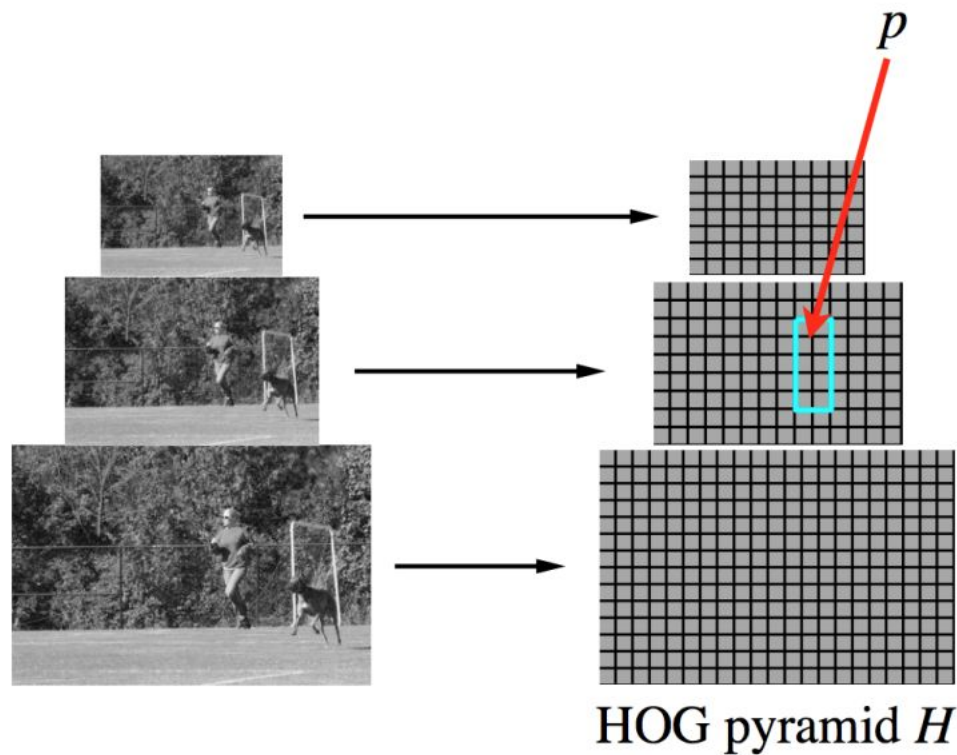
$$\begin{aligned} & \textit{detection score} \\ &= \sum_{i=0}^n F_i \phi(p_i, H) - \sum_{i=1}^n d_i(\Delta x_i, \Delta y_i, \Delta x_i^2, \Delta y_i^2) \end{aligned}$$

# Calculating the score for a detection

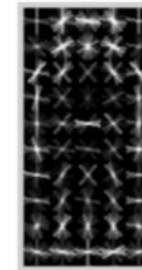
$$\begin{aligned} & \textit{detection score} \\ &= \sum_{i=0}^n F_i \phi(p_i, H) - \sum_{i=1}^n d_i(\Delta x_i, \Delta y_i, \Delta x_i^2, \Delta y_i^2) \end{aligned}$$

Scores for each part filter + global filter (similar to Dalal and Triggs).

# Remember from Dalal and Triggs



Filter  $F$

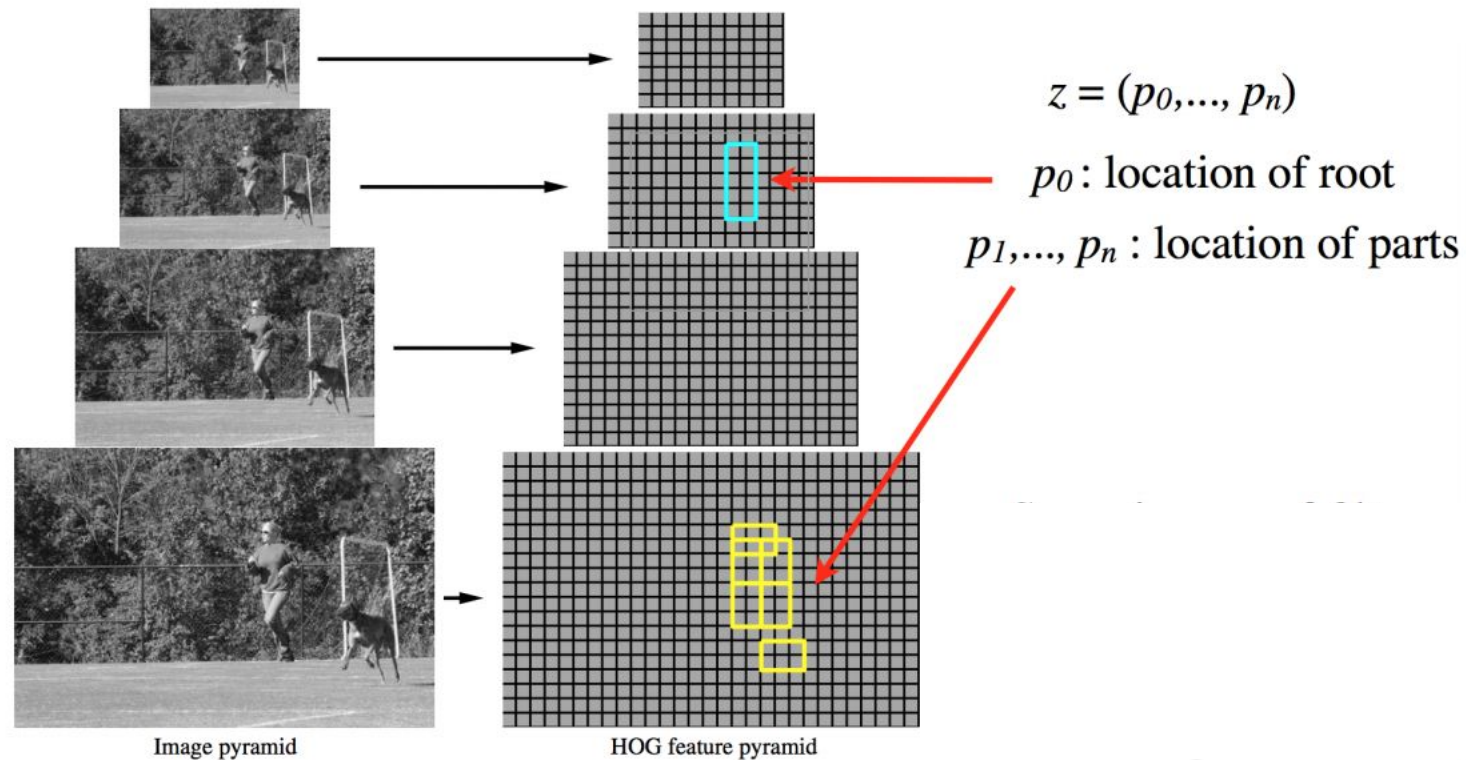


Score of  $F$  at position  $p$  is  
 $F \cdot \phi(p, H)$

$\phi(p, H) =$  concatenation of  
HOG features from  
subwindow specified by  $p$

Deformable parts calculates a score for each **part** along with a **global** score

$p_i = (x_i, y_i, l_i)$  specifies the level and position of the  $i$ -th filter

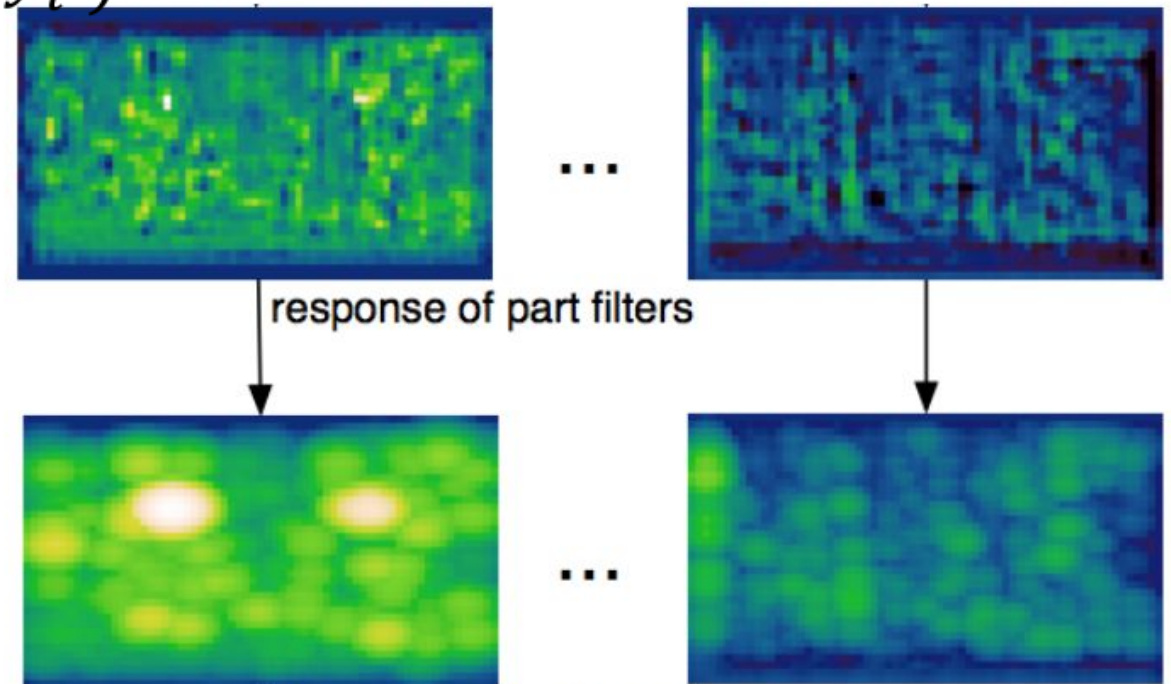


# Detection pipeline

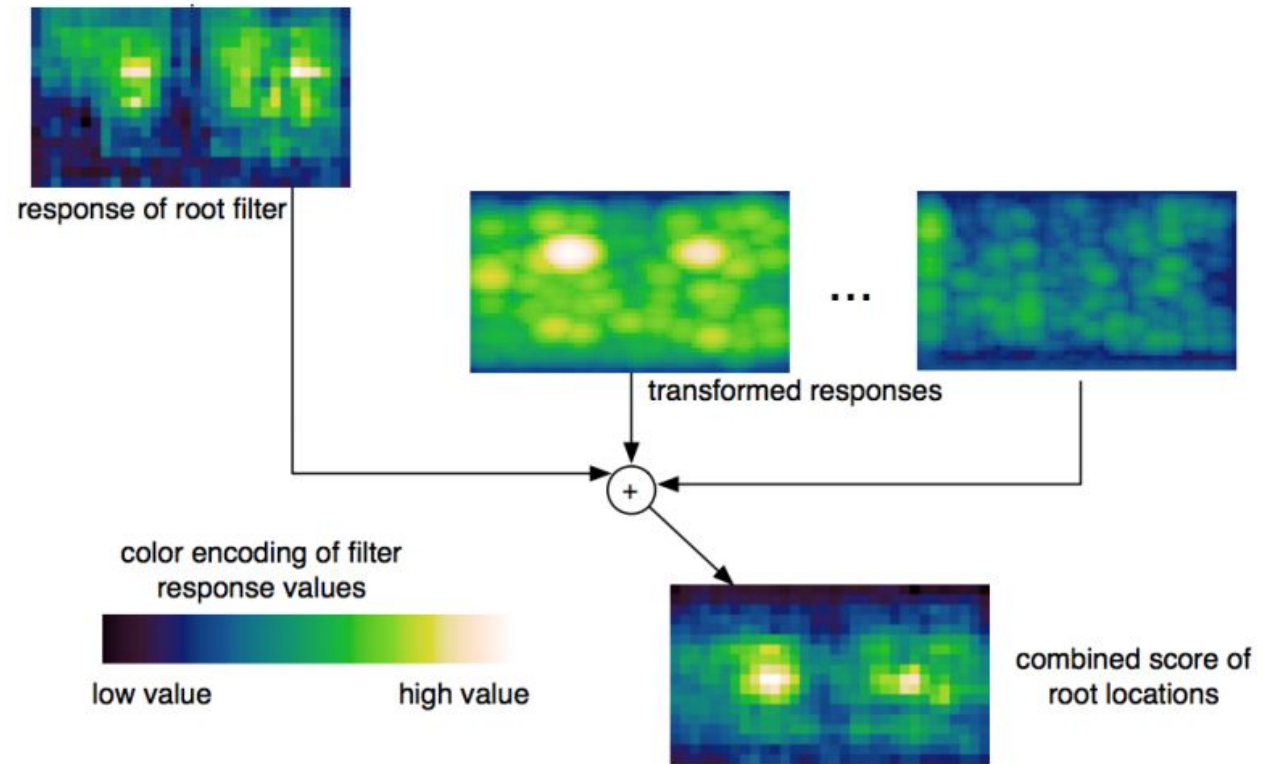
Now apply the spatial costs for each part:

*detection score*

$$= F_i \phi(p_i, H) - d_i(\Delta x_i, \Delta y_i, \Delta x_i^2, \Delta y_i^2)$$



# Detection pipeline



Now add the global filter:

*detection score*

$$= F_0 \phi(p_i, H) + \sum_{i=1}^n F_i \phi(p_i, H) - \sum_{i=1}^n d_i(\Delta x_i, \Delta y_i, \Delta x_i^2, \Delta y_i^2)$$

# Calculating the score for a detection

$$\begin{aligned} & \textit{detection score} \\ &= \sum_{i=0}^n F_i \phi(p_i, H) - \sum_{i=1}^n d_i(\Delta x_i, \Delta y_i, \Delta x_i^2, \Delta y_i^2) \end{aligned}$$

The deformation costs for each part.

$\Delta x_i$  measures the distance in the x-direction from where part  $i$  should be.

$\Delta y_i$  measures the same in the y-axis direction.

$d_i$  is the weight associated for part  $i$  that penalizes the part for being away.

# Calculating the score for a detection

$$\begin{aligned} & \textit{detection score} \\ &= \sum_{i=0}^n F_i \phi(p_i, H) - \sum_{i=1}^n d_i(\Delta x_i, \Delta y_i, \Delta x_i^2, \Delta y_i^2) \end{aligned}$$

If  $d_i = (0, 0, 1, 0)$ . What does this mean?

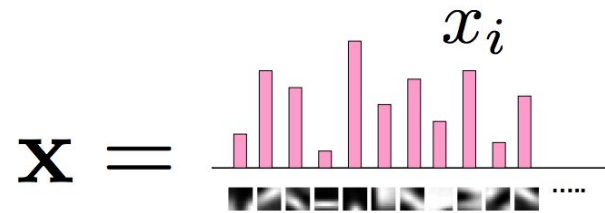


# What we will learn today

- Naïve Bayes

# Naïve Bayes

- Classify image using histograms of occurrences on visual words:



- where:
  - $x_i$  is the event of visual word  $v_i$  appearing in the image,
  - $N(i)$  the number of times word  $v_i$  occurs in the image,
  - $m$  is the number of words in our vocabulary.

Csurka Bray, Dance & Fan, 2004

# Naïve Bayes - classification

- Our goal is to classify that the image represented by  $\mathbf{x}$  is belongs class that has the highest *posterior* probability:

$$c^* = \mathit{arg} \max_c P(c | \mathbf{x})$$

# Naïve Bayes – conditional independence

- Naïve Bayes classifier assumes that visual words are conditionally independent given object class.
- Therefore, we can multiply the probability of each visual word to obtain the joint probability.
- Model for image  $x$  under object class  $c$ :

$$P(x | c) = \prod_{i=1}^m P(x_i | c)$$

- How do we compute  $P(x_i | c)$  ?

Csurka Bray, Dance & Fan, 2004

# Naïve Bayes – prior

- Class priors  $P(c)$  encode how likely we are to see one class versus others.
- Note that:

$$\sum_c P(c) = 1$$

Csurka Bray, Dance & Fan, 2004

# Naïve Bayes - posterior

- With the equations from the previous slides, we can now calculate the probability that an image represented by  $\mathbf{x}$  belongs to class category  $c$ .

$$P(c | \mathbf{x}) = \frac{P(c) P(\mathbf{x} | c)}{\sum_{c'} P(c') P(\mathbf{x} | c')}$$

Bayes Theorem

# Naïve Bayes – posterior

- With the equations from the previous slides, we can now calculate the probability that an image represented by  $\mathbf{x}$  belongs to class category  $c$ .

$$P(c | \mathbf{x}) = \frac{P(c) P(\mathbf{x} | c)}{\sum_{c'} P(c') P(\mathbf{x} | c')}$$

$$P(c | \mathbf{x}) = \frac{P(c) \prod_{i=1}^m P(x_i | c)}{\sum_{c'} P(c') \prod_{i=1}^m P(x_i | c')}$$

# Let's break down the posterior

The probability that  $\mathbf{x}$  belongs to class  $c_1$ :

$$P(c_1 | \mathbf{x}) = \frac{P(c_1) \prod_{i=1}^m P(x_i | c_1)}{\sum_{c'} P(c') \prod_{i=1}^m P(x_i | c')}$$

And the probability that  $\mathbf{x}$  belongs to class  $c_2$ :

$$P(c_2 | \mathbf{x}) = \frac{P(c_2) \prod_{i=1}^m P(x_i | c_2)}{\sum_{c'} P(c') \prod_{i=1}^m P(x_i | c')}$$



# Both their denominators are the same

The probability that  $\mathbf{x}$  belongs to class  $c_1$ :

$$P(c_1 | \mathbf{x}) = \frac{P(c_1) \prod_{i=1}^m P(x_i | c_1)}{\sum_{c'} P(c') \prod_{i=1}^m P(x_i | c')}$$

And the probability that  $\mathbf{x}$  belongs to class  $c_2$ :

$$P(c_2 | \mathbf{x}) = \frac{P(c_2) \prod_{i=1}^m P(x_i | c_2)}{\sum_{c'} P(c') \prod_{i=1}^m P(x_i | c')}$$

# Both their denominators are the same

- Since we only want the max, we can ignore the denominator:

$$P(c_1 | \mathbf{x}) \propto P(c_1) \prod_{i=1}^m P(x_i | c_1)$$

$$P(c_2 | \mathbf{x}) \propto P(c_2) \prod_{i=1}^m P(x_i | c_2)$$

For the general class  $c$ ,

$$P(c | \mathbf{x}) \propto P(c) \prod_{i=1}^m P(x_i | c)$$

For the general class  $c$ ,

$$P(c | \mathbf{x}) \propto P(c) \prod_{i=1}^m P(x_i | c)$$

We can take the log:

$$\log P(c | \mathbf{x}) \propto \log P(c) + \sum_{i=1}^m \log P(x_i | c)$$

# Naïve Bayes - classification

- We can now classify that the image represented by  $\mathbf{x}$  is belongs class that has the highest probability:

$$c^* = \mathit{arg} \max_c P(c | \mathbf{x})$$
$$c^* = \mathit{arg} \max_c \log P(c | \mathbf{x})$$

# Naïve Bayes - classification

- So, the following classification becomes:

$$c^* = \operatorname{arg\,max}_c P(c | \mathbf{x})$$
$$c^* = \operatorname{arg\,max}_c \log P(c | \mathbf{x})$$

$$c^* = \operatorname{arg\,max}_c \log P(c) + \sum_{i=1}^m \log P(x_i | c)$$