

Information Gain

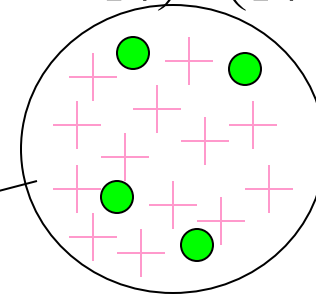
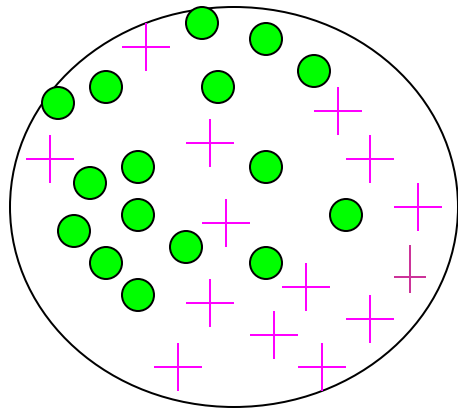
- We want to determine **which attribute** in a given set of training feature vectors is **most useful** for discriminating between the classes to be learned.
- **Information gain** tells us how important a given attribute of the feature vectors is.
- We will use it to decide the ordering of attributes in the nodes of a decision tree.

Calculating Information Gain

Information Gain = entropy(parent) – [average entropy(children)]

child entropy $-\left(\frac{13}{17} \cdot \log_2 \frac{13}{17}\right) - \left(\frac{4}{17} \cdot \log_2 \frac{4}{17}\right) = 0.787$

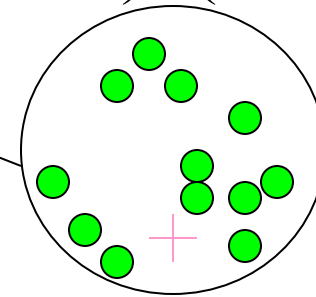
Entire population (30 instances)



17 instances

child entropy $-\left(\frac{1}{13} \cdot \log_2 \frac{1}{13}\right) - \left(\frac{12}{13} \cdot \log_2 \frac{12}{13}\right) = 0.391$

parent entropy $-\left(\frac{14}{30} \cdot \log_2 \frac{14}{30}\right) - \left(\frac{16}{30} \cdot \log_2 \frac{16}{30}\right) = 0.996$



13 instances

(Weighted) Average Entropy of Children = $\left(\frac{17}{30} \cdot 0.787\right) + \left(\frac{13}{30} \cdot 0.391\right) = 0.615$

Information Gain = 0.996 - 0.615 = 0.38 for this split

Entropy-Based Automatic Decision Tree Construction

Training Set S

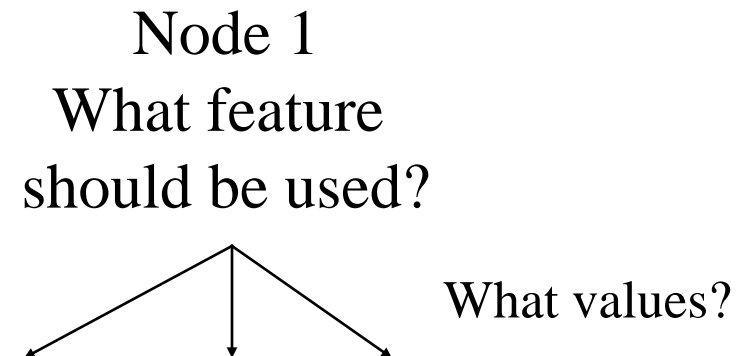
$$x_1 = (f_{11}, f_{12}, \dots, f_{1m})$$

$$x_2 = (f_{21}, f_{22}, \dots, f_{2m})$$

⋮

⋮

$$x_n = (f_{n1}, f_{n2}, \dots, f_{nm})$$

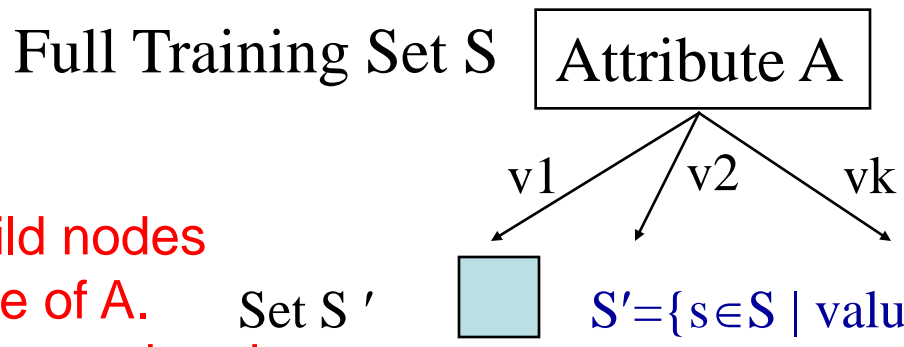


Quinlan suggested **information gain** in his ID3 system and later the **gain ratio**, both based on **entropy**.

Using Information Gain to Construct a Decision Tree

①

Choose the attribute A with highest information gain for the full training set at the root of the tree.



②

Construct child nodes for each value of A. Each has an associated subset of vectors in which A has a particular value.

③

repeat recursively till when?

Simple Example

Training Set: 3 features and 2 classes

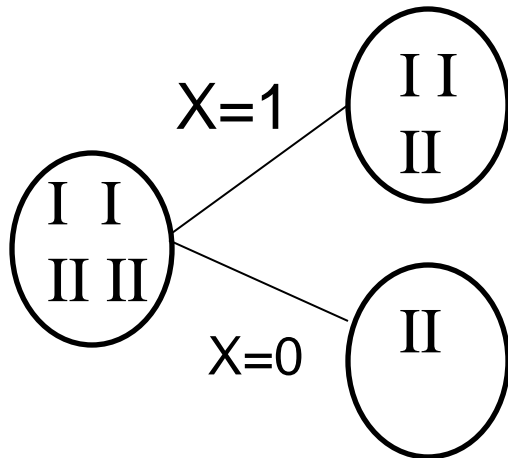
X	Y	Z	C
1	1	1	I
1	1	0	I
0	0	1	II
1	0	0	II

How would you distinguish class I from class II?

X	Y	Z	C
1	1	1	I
1	1	0	I
0	0	1	II
1	0	0	II

Split on attribute X

If X is the best attribute, this node would be further split.



$$\begin{aligned}
 E_{\text{child1}} &= -(1/3)\log_2(1/3) - (2/3)\log_2(2/3) \\
 &= .5284 + .39 \\
 &= .9184
 \end{aligned}$$

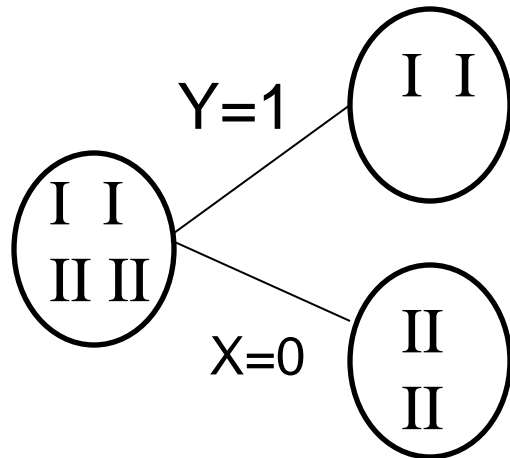
$$E_{\text{child2}} = 0$$

$$E_{\text{parent}} = 1$$

$$\text{GAIN} = 1 - (3/4)(.9184) - (1/4)(0) = .3112$$

X	Y	Z	C
1	1	1	I
1	1	0	I
0	0	1	II
1	0	0	II

Split on attribute Y



$$E_{\text{child1}} = 0$$

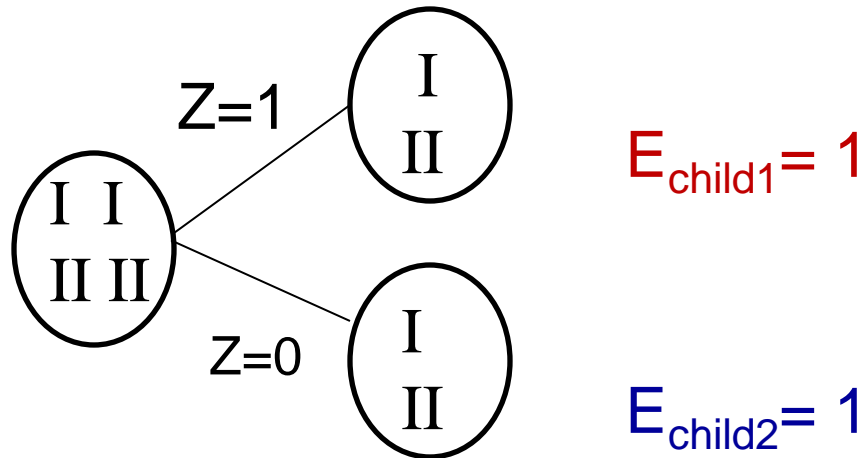
$$E_{\text{child2}} = 0$$

$$E_{\text{parent}} = 1$$

$$\text{GAIN} = 1 - (1/2) \cdot 0 - (1/2) \cdot 0 = 1; \text{ BEST ONE}$$

X	Y	Z	C
1	1	1	I
1	1	0	I
0	0	1	II
1	0	0	II

Split on attribute Z



$$E_{\text{parent}} = 1$$

$$\text{GAIN} = 1 - (1/2)(1) - (1/2)(1) = 0 \quad \text{ie. NO GAIN; WORST}$$