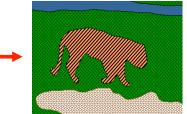
Announcements

Photo shoot at the end of class today! Sign up for Project 3 demo session

From images to objects





1

What Defines an Object?

- · Subjective problem, but has been well-studied
- Gestalt Laws seek to formalize this
 - proximity, similarity, continuation, closure, common fate

Image Segmentation

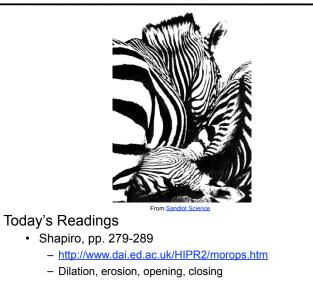


Image Segmentation

We will consider different methods

Already covered:

• Intelligent Scissors (contour-based, manual)

Today—automatic methods:

- K-means clustering (color-based)
- Normalized Cuts (region-based)

Image histograms

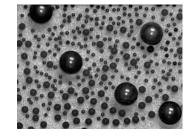


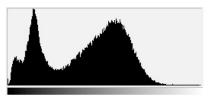
How many "orange" pixels are in this image?

- This type of question answered by looking at the histogram
- A histogram counts the number of occurrences of each color
 - Given an image $F[x,y] \rightarrow RGB$
 - The histogram is $H_F[c] = |\{(x,y) \mid F[x,y] = c\}|$
 - » i.e., for each color value c (x-axis), plot # of pixels with that color (y-axis)
 - What is the dimension of the histogram of an NxN RGB image?

What do histograms look like?

Photoshop demo



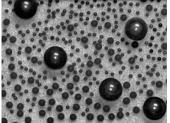


How Many Modes Are There? • Easy to see, hard to compute

Histogram-based segmentation

Goal

- · Break the image into K regions (segments)
- Solve this by reducing the number of colors to K and mapping each pixel to the closest color
 - photoshop demo

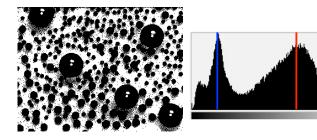




Histogram-based segmentation

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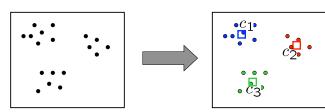


Here's what it looks like if we use two colors

Clustering

How to choose the representative colors?

This is a clustering problem!



Objective

 Each point should be as close as possible to a cluster center - Minimize sum squared distance of each point to closest center

clusters i

 $\sum_{\text{points p in cluster }i} \|p-c_i\|^2$

K-means clustering

K-means clustering algorithm

- 1. Randomly initialize the cluster centers, c₁, ..., c_k
- 2. Given cluster centers, determine points in each cluster
 - For each point p, find the closest c_i. Put p into cluster i
- 3. Given points in each cluster, solve for c_i
 - Set c_i to be the mean of points in cluster i
- 4. If c_i have changed, repeat Step 2

Java demo: http://home.dei.polimi.it/matteucc/Clustering/tutorial html/AppletKM.htm

Properties

- Will always converge to some solution
- Can be a "local minimum"

Σ

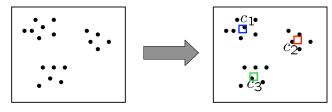
does not always find the global minimum of objective function:

$$\sum_{\text{clusters } i} \sum_{\text{points p in cluster } i} ||p - c_i||^2$$

Break it down into subproblems

Suppose I tell you the cluster centers c_i

- Q: how to determine which points to associate with each c_i?
- A: for each point p, choose closest c,



Suppose I tell you the points in each cluster

- Q: how to determine the cluster centers?
- A: choose c_i to be the mean of all points in the cluster

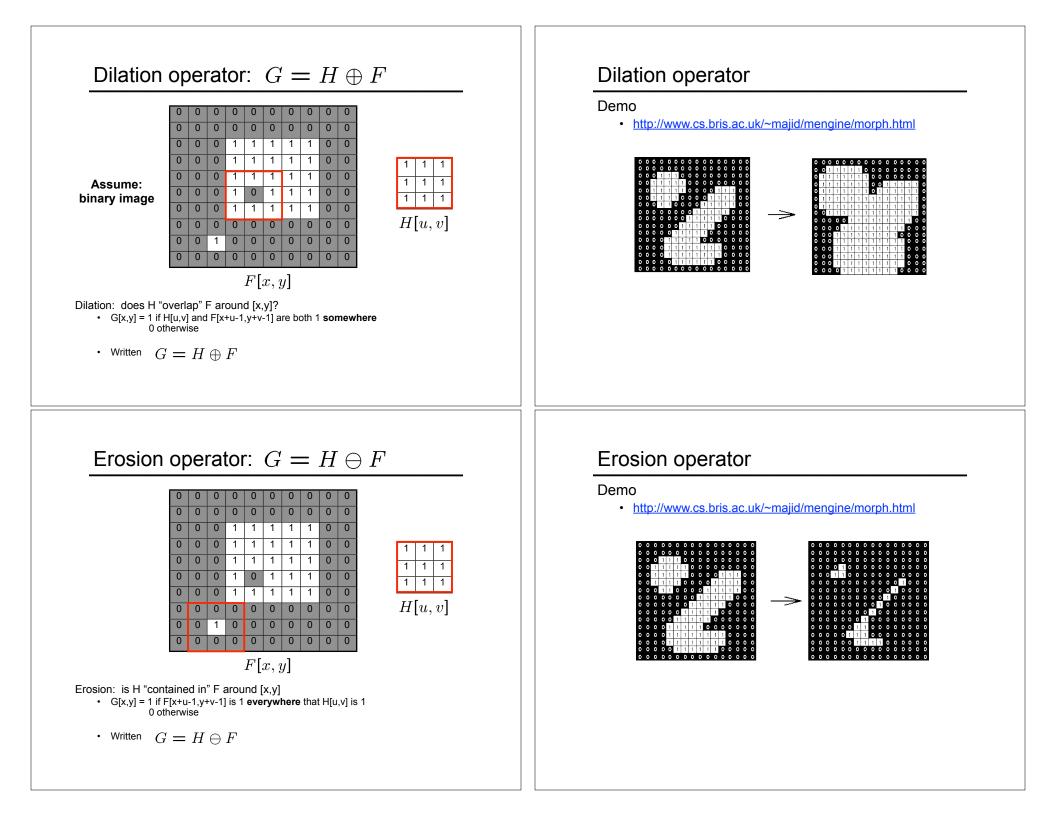
Cleaning up the result

Problem:

- Histogram-based segmentation can produce messy regions
 - segments do not have to be connected
 - may contain holes

How can these be fixed?

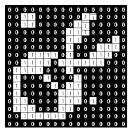




Nested dilations and erosions

What does this operation do?

$$G = H \ominus (H \oplus F)$$



this is called a closing operation

Nested dilations and erosions

What does this operation do?

 $G = H \oplus (H \ominus F)$

- this is called an **opening** operation
- http://www.dai.ed.ac.uk/HIPR2/open.htm

You can clean up binary pictures by applying combinations of dilations and erosions

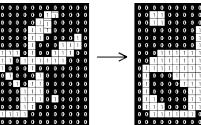
Dilations, erosions, opening, and closing operations are known as morphological operations

• see http://www.dai.ed.ac.uk/HIPR2/morops.htm

Nested dilations and erosions

What does this operation do?

 $G = H \ominus (H \oplus F)$



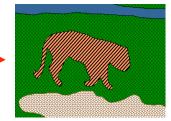


this is called a closing operation

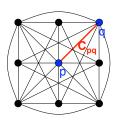
Is this the same thing as the following? $G = H \oplus (H \ominus F)$

Automating Intelligent Scissors?





Images as graphs

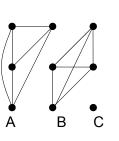




Fully-connected graph

- · node for every pixel
- link between every pair of pixels, p,q
- cost c_{pq} for each link
 - c_{pq} measures similarity
 - » similarity is inversely proportional to difference in color and position
 - » this is different than the costs for intelligent scissors

Segmentation by Graph Cuts

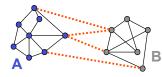




Break Graph into Segments

- · Delete links that cross between segments
- · Easiest to break links that have low cost (low similarity)
 - similar pixels should be in the same segments
 - dissimilar pixels should be in different segments

Cuts in a graph



Link Cut

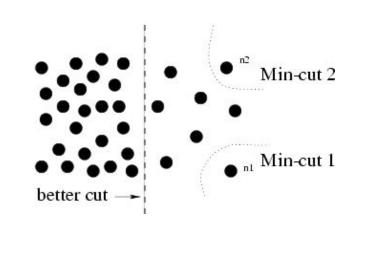
- · set of links whose removal makes a graph disconnected
- cost of a cut:

$$cut(A,B) = \sum_{p \in A, q \in B} c_{p,q}$$

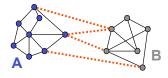
Find minimum cut

- gives you a segmentation
- · fast algorithms exist for doing this

But min cut is not always the best cut...



Cuts in a graph



Normalized Cut

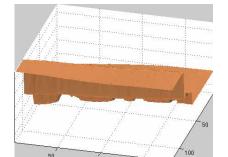
- a cut penalizes large segments
- fix by normalizing for size of segments

 $Ncut(A,B) = \frac{cut(A,B)}{volume(A)} + \frac{cut(A,B)}{volume(B)}$

• volume(A) = sum of costs of all edges that touch A

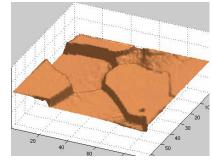
Interpretation as a Dynamical System





Interpretation as a Dynamical System





Treat the links as springs and shake the system

- elasticity proportional to cost
- vibration "modes" correspond to segments
 - can compute these by solving an eigenvector problem
 - for more details, see
 - » J. Shi and J. Malik, Normalized Cuts and Image Segmentation, CVPR, 1997

Color Image Segmentation

