Announcements

Project 1

- due Tuesday at 11:59pm (artifact Wednesday at 11:59pm)
- grading session Wednesday (signup!)

Project 2

choose partners by Wednesday

– signup:

» https://norfolk.cs.washington.edu/htbin-php/gtng/gtng.php

Projection



http://www.julianbeever.net/pave.htm

ReadingsNalwa 2.1

Projection

1



http://www.julianbeever.net/pave.htm

Readings

• Nalwa 2.1

Müller-Lyer Illusion

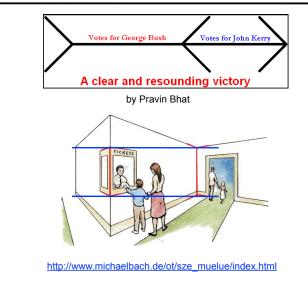
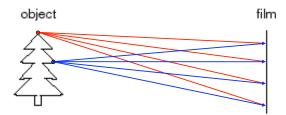


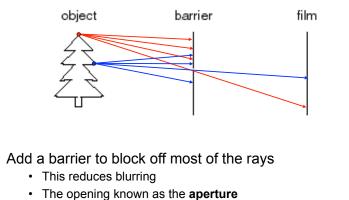
Image formation



Let's design a camera

- Idea 1: put a piece of film in front of an object
- Do we get a reasonable image?

Pinhole camera



• How does this transform the image?

Pinhole cameras everywhere



Sun "shadows" during a solar eclipse by Henrik von Wendt http://www.flickr.com/photos/hvw/2724969199/

Pinhole cameras everywhere



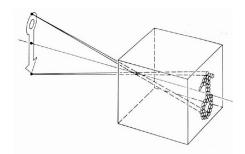
Sun "shadows" during a solar eclipse http://www.flickr.com/photos/73860948@N08/6678331997/

Pinhole cameras everywhere



Tree shadow during a solar eclipse photo credit: Nils van der Burg http://www.physicstogo.org/index.cfm

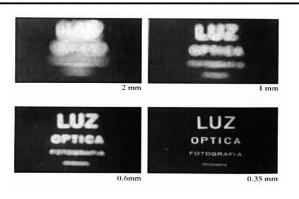
Camera Obscura



The first camera

- Known to Aristotle
- · How does the aperture size affect the image?

Shrinking the aperture



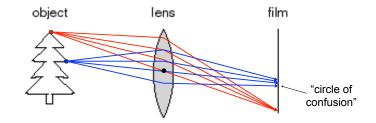
Why not make the aperture as small as possible?

- Less light gets through
- Diffraction effects ...

Shrinking the aperture



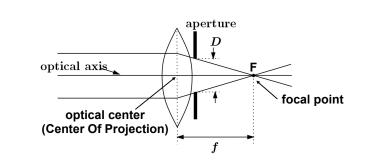
Adding a lens



A lens focuses light onto the film

- There is a specific distance at which objects are "in focus"
 other points project to a "circle of confusion" in the image
- · Changing the shape of the lens changes this distance

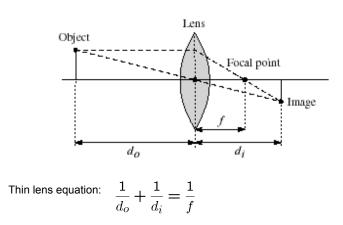
Lenses



A lens focuses parallel rays onto a single focal point

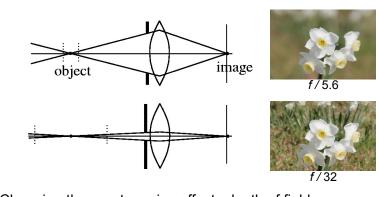
- focal point at a distance *f* beyond the plane of the lens
 f is a function of the shape and index of refraction of the lens
- Aperture of diameter D restricts the range of rays
 aperture may be on either side of the lens
- · Lenses are typically spherical (easier to produce)

Thin lenses



- Any object point satisfying this equation is in focus
- · What is the shape of the focus region?
- How can we change the focus region?
- Thin lens applet: http://www.phy.ntnu.edu.tw/java/Lens/lens_e.html (by Fu-Kwun Hwang)

Depth of field

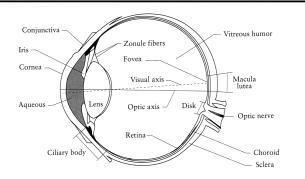


Changing the aperture size affects depth of field

A smaller aperture increases the range in which the object is approximately in focus

Flower images from Wikipedia http://en.wikipedia.org/wiki/Depth_of_field

The eye



The human eye is a camera

- Iris colored annulus with radial muscles
- Pupil the hole (aperture) whose size is controlled by the iris
- · What's the "film"?
 - photoreceptor cells (rods and cones) in the retina

Digital camera



A digital camera replaces film with a sensor array

- Each cell in the array is a Charge Coupled Device
 - light-sensitive diode that converts photons to electrons
 - other variants exist: CMOS is becoming more popular
 - http://electronics.howstuffworks.com/digital-camera.htm

Issues with digital cameras



```
    big difference between consumer vs. SLR-style cameras
    low light is where you most notice <u>noise</u>
    Compression
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creates <u>artifacts</u> except in uncompressed formats (tiff, raw)

Color

<u>color fringing</u> artifacts from <u>Bayer patterns</u>

Blooming

charge <u>overflowing</u> into neighboring pixels

In-camera processing

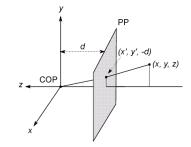
- oversharpening can produce <u>halos</u>
- Interlaced vs. progressive scan video
 - even/odd rows from different exposures
- Are more megapixels better?
 - requires higher quality lens
 noise issues
- Stabilization

- compensate for camera shake (mechanical vs. electronic)

More info online, e.g.,

- http://electronics.howstuffworks.com/digital-camera.htm
- http://www.dpreview.com/

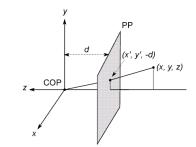
Modeling projection



The coordinate system

- · We will use the pin-hole model as an approximation
- Put the optical center (Center Of Projection) at the origin
- Put the image plane (Projection Plane) in front of the COP
 Why?
- The camera looks down the negative z axis
 - we need this if we want right-handed-coordinates

Modeling projection



Projection equations

- Compute intersection with PP of ray from (x,y,z) to COP
- Derived using similar triangles (on board)

$$(x,y,z)
ightarrow (-drac{x}{z},\ -drac{y}{z},\ -d)$$

• We get the projection by throwing out the last coordinate:

$$(x, y, z)
ightarrow (-drac{x}{z}, -drac{y}{z})$$

Perspective Projection

Projection is a matrix multiply using homogeneous coordinates:

$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & -1/d & 0 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix} = \begin{bmatrix} x \\ y \\ -z/d \end{bmatrix} \Rightarrow (-d\frac{x}{z}, -d\frac{y}{z})$$

divide by third coordinate

This is known as perspective projection

- The matrix is the projection matrix
- Can also formulate as a 4x4 (today's reading does this)

$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & -1/d & 0 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix} = \begin{bmatrix} x \\ y \\ z \\ -z/d \end{bmatrix} \Rightarrow (-d\frac{x}{z}, -d\frac{y}{z})$$
divide by fourth coordinate

Homogeneous coordinates

Is this a linear transformation?

• no-division by z is nonlinear

Trick: add one more coordinate:

$$(x,y) \Rightarrow \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$
 $(x,y,z) \Rightarrow \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$

homogeneous image coordinates

homogeneous scene coordinates

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Converting from homogeneous coordinates

$$\begin{bmatrix} x \\ y \\ w \end{bmatrix} \Rightarrow (x/w, y/w) \qquad \begin{bmatrix} x \\ y \\ z \\ w \end{bmatrix} \Rightarrow (x/w, y/w, z/w)$$

Perspective Projection

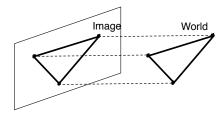
How does scaling the projection matrix change the transformation?

$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & -1/d & 0 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix} = \begin{bmatrix} x \\ y \\ -z/d \end{bmatrix} \Rightarrow (-d\frac{x}{z}, -d\frac{y}{z})$$
$$\begin{bmatrix} -d & 0 & 0 & 0 \\ 0 & -d & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix} = \begin{bmatrix} -dx \\ -dy \\ z \end{bmatrix} \Rightarrow (-d\frac{x}{z}, -d\frac{y}{z})$$

Orthographic projection

Special case of perspective projection

Distance from the COP to the PP is infinite



- · Good approximation for telephoto optics
- Also called "parallel projection": (x, y, z) \rightarrow (x, y)
- What's the projection matrix?

$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix} = \begin{bmatrix} x \\ y \\ 1 \end{bmatrix} \Rightarrow (x, y)$$

Camera parameters

A camera is described by several parameters

- Translation T of the optical center from the origin of world coords
- Rotation R of the image plane

wx

wy

w

- focal length f, principle point (x'_c, y'_c), pixel size (s_x, s_y)
- blue parameters are called "extrinsics," red are "intrinsics"

Projection equation

 $\mathbf{x} =$

- The projection matrix models the cumulative effect of all parameters
- · Useful to decompose into a series of operations

$$\mathbf{\Pi} = \begin{bmatrix} -f\hat{s}_{x} & 0 & x'_{c} \\ 0 & -f\hat{s}_{y} & y'_{c} \\ 0 & 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} \mathbf{R}_{3x3} & \mathbf{0}_{3x1} \\ \mathbf{0}_{1x3} & 1 \end{bmatrix} \begin{bmatrix} \mathbf{I}_{3x3} & \mathbf{T}_{3x1} \\ \mathbf{0}_{1x3} & 1 \end{bmatrix}$$

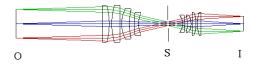
ntrinsics projection rotation translation

The definitions of these parameters are **not** completely standardized
 – especially intrinsics—varies from one book to another

Orthographic ("telecentric") lenses

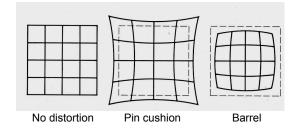


Navitar telecentric zoom lens



http://www.lhup.edu/~dsimanek/3d/telecent.htm

Distortion



Radial distortion of the image

- Caused by imperfect lenses
- Deviations are most noticeable for rays that pass through the edge of the lens

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Modeling distortion	Many other types of projection exist
$\begin{array}{rcl} \text{Project} \ (\hat{x},\hat{y},\hat{z}) & x'_n &=& \hat{x}/\hat{z} \\ \text{to "normalized"} & y'_n &=& \hat{y}/\hat{z} \end{array}$	
$\begin{array}{rcl} r^2 &=& {x'_n}^2 + {y'_n}^2 \\ \text{Apply radial distortion} && x'_d &=& {x'_n}(1 + \kappa_1 r^2 + \kappa_2 r^4) \\ && y'_d &=& y'_n(1 + \kappa_1 r^2 + \kappa_2 r^4) \end{array}$	
Apply focal length $x' = fx'_d + x_c$ translate image center $y' = fy'_d + y_c$	
 To model lens distortion Use above projection operation instead of standard projection matrix multiplication 	32

360 degree field of view...



Basic approach

- Take a photo of a parabolic mirror with an orthographic lens (Nayar)
- Or buy one a lens from a variety of omnicam manufacturers...
 - See http://www.cis.upenn.edu/~kostas/omni.html

Tilt-shift



http://www.northlight-images.co.uk/article_pages/tilt_and_shift_ts-e.html





Tilt-shift images from <u>Olivo Barbieri</u> and Photoshop <u>imitations</u>

Rotating sensor (or object)



Rollout Photographs © Justin Kerr http://research.famsi.org/kerrmaya.html

Also known as "cyclographs", "peripheral images"

Photofinish

