Announcements

Midterms back today (end of class) Photo shoot on Thursday!

1

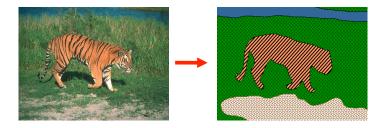
Image Segmentation



Today's Readings

- Shapiro, pp. 279-289
 - http://www.dai.ed.ac.uk/HIPR2/morops.htm
 - Dilation, erosion, opening, closing

From images to objects



What Defines an Object?

- · Subjective problem, but has been well-studied
- Gestalt Laws seek to formalize this
 - proximity, similarity, continuation, closure, common fate

Image Segmentation

We will consider different methods

Already covered:

• Intelligent Scissors (contour-based, manual)

Today—automatic methods:

- K-means clustering (color-based)
- · Normalized Cuts (region-based)

Image histograms

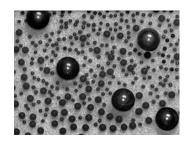


How many "orange" pixels are in this image?

- This type of question answered by looking at the histogram
- · A histogram counts the number of occurrences of each color
 - Given an image $\ F[x,y] o RGB$
 - The histogram is $H_F[c] = |\{(x,y) \mid F[x,y] = c\}|$
 - » i.e., for each color value c (x-axis), plot # of pixels with that color (y-axis)
 - What is the dimension of the histogram of an NxN RGB image?

What do histograms look like?

Photoshop demo





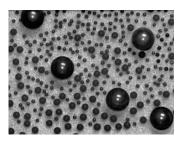
How Many Modes Are There?

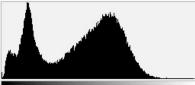
· Easy to see, hard to compute

Histogram-based segmentation

Goal

- · Break the image into K regions (segments)
- Solve this by reducing the number of colors to K and mapping each pixel to the closest color
 - photoshop demo

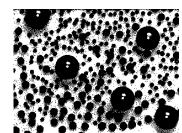


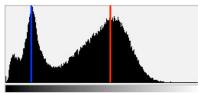


Histogram-based segmentation

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 - photoshop demo



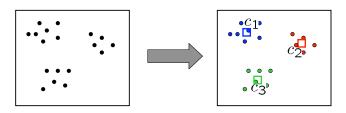


Here's what it looks like if we use two colors

Clustering

How to choose the representative colors?

· This is a clustering problem!



Objective

- Each point should be as close as possible to a cluster center
 - Minimize sum squared distance of each point to closest center

$$\sum_{\text{clusters } i} \sum_{\text{points p in cluster } i} ||p - c_i||^2$$

K-means clustering

K-means clustering algorithm

- 1. Randomly initialize the cluster centers, c₁, ..., c_K
- 2. Given cluster centers, determine points in each cluster
 - For each point p, find the closest c_{i} . Put p into cluster i
- 3. Given points in each cluster, solve for c_i
 - Set c_i to be the mean of points in cluster i
- 4. If c_i have changed, repeat Step 2

Java demo: http://home.dei.polimi.it/matteucc/Clustering/tutorial html/AppletKM.htm

Properties

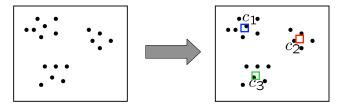
- · Will always converge to some solution
- Can be a "local minimum"
 - does not always find the global minimum of objective function:

$$\sum_{\text{Clusters } i} \sum_{\text{points p in cluster } i} \|p - c_i\|^2$$

Break it down into subproblems

Suppose I tell you the cluster centers c_i

- Q: how to determine which points to associate with each ci?
- A: for each point p, choose closest c_i



Suppose I tell you the points in each cluster

- Q: how to determine the cluster centers?
- A: choose c_i to be the mean of all points in the cluster

Cleaning up the result

Problem:

- · Histogram-based segmentation can produce messy regions
 - segments do not have to be connected
 - may contain holes

How can these be fixed?

photoshop demo

Dilation operator: $G = H \oplus F$

Assume: binary image

0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	1	1	1	1	1	0	0
0	0	0	1	1	1	1	1	0	0
0	0	0	1	1	1	1	1	0	0
0	0	0	1	0	1	1	1	0	0
0	0	0	1	1	1	1	1	0	0
0	0	0	0	0	0	0	0	0	0
0	0	1	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
F[x, y]									

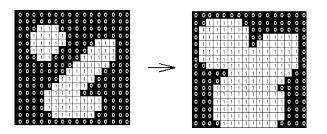
Dilation: does H "overlap" F around [x,y]?

- G[x,y] = 1 if H[u,v] and F[x+u-1,y+v-1] are both 1 somewhere 0 otherwise
- $\cdot \quad \text{Written} \quad G = H \oplus F$

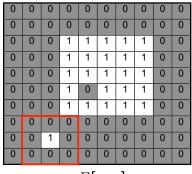
Dilation operator

Demo

• http://www.cs.bris.ac.uk/~majid/mengine/morph.html



Erosion operator: $G = H \ominus F$



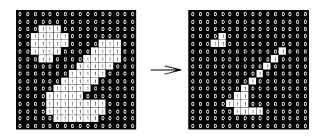
Erosion: is H "contained in" F around [x,y]

- G[x,y] = 1 if F[x+u-1,y+v-1] is 1 **everywhere** that H[u,v] is 1 0 otherwise
- Written $G = H \ominus F$

Erosion operator

Demo

• http://www.cs.bris.ac.uk/~majid/mengine/morph.html



Nested dilations and erosions

What does this operation do?

$$G = H \ominus (H \oplus F)$$

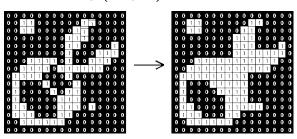


• this is called a **closing** operation

Nested dilations and erosions

What does this operation do?

$$G = H \ominus (H \oplus F)$$



• this is called a **closing** operation

Is this the same thing as the following?

$$G = H \oplus (H \ominus F)$$

Nested dilations and erosions

What does this operation do?

$$G = H \oplus (H \ominus F)$$

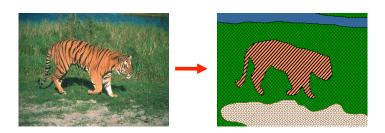
- this is called an **opening** operation
- http://www.dai.ed.ac.uk/HIPR2/open.htm

You can clean up binary pictures by applying combinations of dilations and erosions

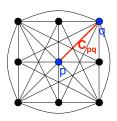
Dilations, erosions, opening, and closing operations are known as **morphological operations**

• see http://www.dai.ed.ac.uk/HIPR2/morops.htm

Automating Intelligent Scissors?



Images as graphs

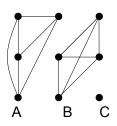




Fully-connected graph

- · node for every pixel
- link between every pair of pixels, p,q
- cost c_{pq} for each link
 - c_{pq} measures similarity
 - » similarity is inversely proportional to difference in color and position
 - » this is different than the costs for intelligent scissors

Segmentation by Graph Cuts

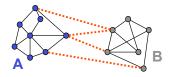




Break Graph into Segments

- · Delete links that cross between segments
- Easiest to break links that have low cost (low similarity)
 - similar pixels should be in the same segments
 - dissimilar pixels should be in different segments

Cuts in a graph



Link Cut

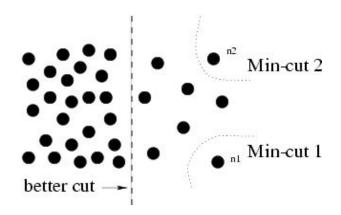
- · set of links whose removal makes a graph disconnected
- · cost of a cut:

$$cut(A,B) = \sum_{p \in A, q \in B} c_{p,q}$$

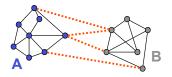
Find minimum cut

- gives you a segmentation
- · fast algorithms exist for doing this

But min cut is not always the best cut...



Cuts in a graph



Normalized Cut

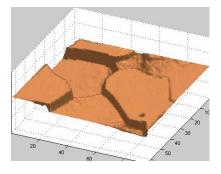
- · a cut penalizes large segments
- · fix by normalizing for size of segments

$$Ncut(A,B) = \frac{cut(A,B)}{volume(A)} + \frac{cut(A,B)}{volume(B)}$$

• volume(A) = sum of costs of all edges that touch A

Interpretation as a Dynamical System



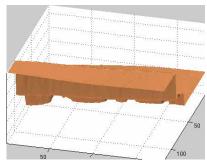


Treat the links as springs and shake the system

- · elasticity proportional to cost
- · vibration "modes" correspond to segments
 - can compute these by solving an eigenvector problem
 - for more details, see
 - » J. Shi and J. Malik, Normalized Cuts and Image Segmentation, CVPR, 1997

Interpretation as a Dynamical System





Color Image Segmentation





