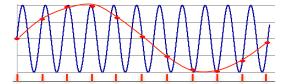


Even worse for synthetic images



Sampling and the Nyquist rate

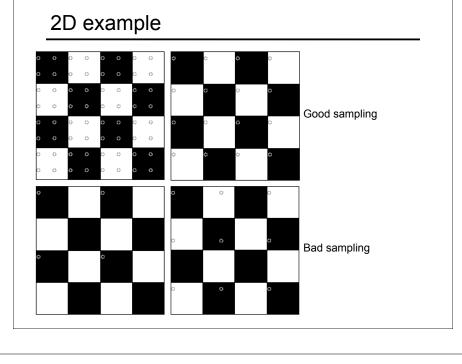


Aliasing can arise when you sample a continuous signal or image

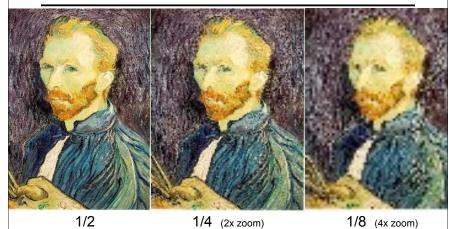
- occurs when your sampling rate is not high enough to capture the amount of detail in your image
- Can give you the wrong signal/image—an alias
- formally, the image contains structure at different scales
 called "frequencies" in the Fourier domain
- the sampling rate must be high enough to capture the highest frequency in the image

To avoid aliasing:

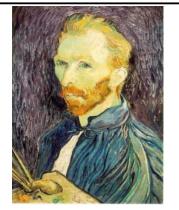
- sampling rate ≥ 2 * max frequency in the image
 said another way: ≥ two samples per cycle
- This minimum sampling rate is called the Nyquist rate



How to fix this?



Subsampling with Gaussian pre-filtering





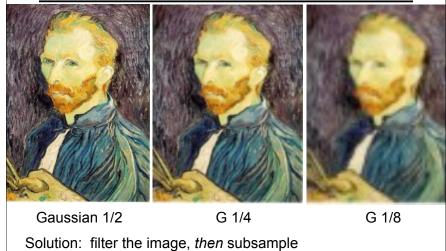
G 1/8

Gaussian 1/2

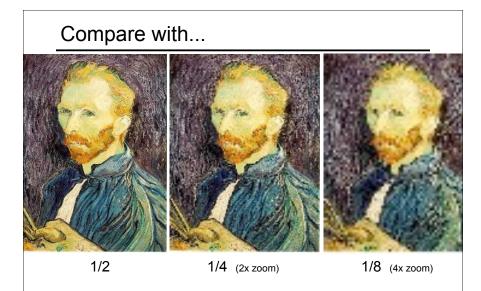
Solution: filter the image, then subsample

• Filter size should double for each ½ size reduction. Why?

Subsampling with Gaussian pre-filtering



• Why does this work?





Moire patterns in real-world images. Here are comparison images by Dave Etchells of <u>Imaging Resource</u> using the Canon D60 (with an antialias filter) and the Sigma SD-9 (which has no antialias filter). The bands below the fur in the image at right are the kinds of artifacts that appear in images when no antialias filter is used. Sigma chose to eliminate the filter to get more sharpness, but the resulting apparent detail may or may not reflect features in the image.

Subsampling with Gaussian pre-filtering Some times we want many resolutions Idea: Represent NxN image as a "pyramid" of 1x1, 2x2, 4x4,..., 2kx2k images (assuming N=2k) level k (= 1 pixel) level k level 0 (= original image) Known as a Gaussian Pyramid [Burt and Adelson, 1983] Gaussian 1/2 G 1/4 G 1/8 • In computer graphics, a *mip map* [Williams, 1983] Solution: filter the image, then subsample A precursor to wavelet transform Gaussian Pyramids have all sorts of applications in computer vision Filter size should double for each ½ size reduction. Why? We'll talk about these later in the course • How can we speed this up?

d = 1 in this

example

