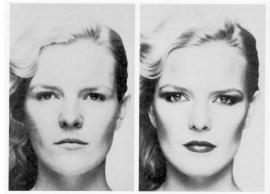
Announcements

Midterm due Tuesday beginning of class

Photometric Stereo

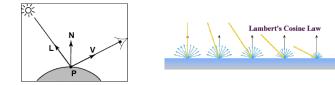


Merle Norman Cosmetics, Los Angeles

Readings

Optional: Woodham's original photometric stereo paper
<u>http://www.cs.ubc.ca/~woodham/papers/Woodham80c.pdf</u>

Diffuse reflection

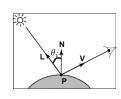


 $R_e = k_d \mathbf{N} \cdot \mathbf{L} R_i$ image intensity of P \longrightarrow $I = k_d \mathbf{N} \cdot \mathbf{L}$

Simplifying assumptions

- I = R_e: camera response function f is the identity function:
 - can always achieve this in practice by solving for f and applying f $^{\rm -1}$ to each pixel in the image
- R_i = 1: light source intensity is 1
 - $_$ can achieve this by dividing each pixel in the image by R_{i}

Shape from shading



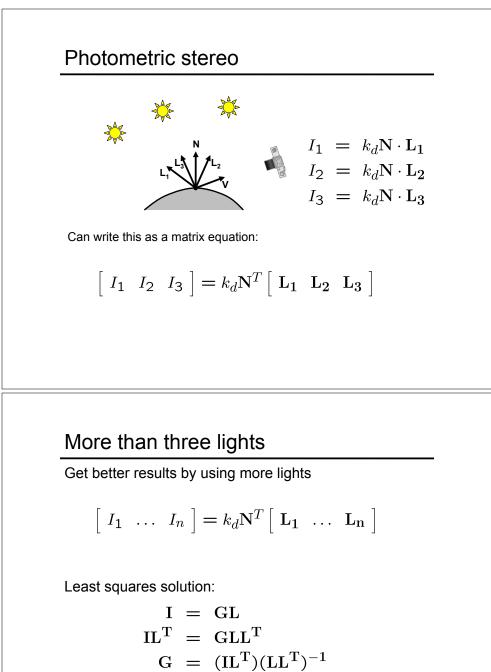
Suppose $k_d = 1$ $I = k_d \mathbf{N} \cdot \mathbf{L}$ $= \mathbf{N} \cdot \mathbf{L}$

 $= \cos \theta_i$



You can directly measure angle between normal and light source

- Not quite enough information to compute surface shape
- But can be if you add some additional info, for example
 - assume a few of the normals are known (e.g., along silhouette)
 - constraints on neighboring normals—"integrability"
 - smoothness
- · Hard to get it to work well in practice
 - plus, how many real objects have constant albedo?



Solving the equations

$$\begin{bmatrix} I_1 & I_2 & I_3 \end{bmatrix} = k_d \mathbf{N}^T \begin{bmatrix} \mathbf{L}_1 & \mathbf{L}_2 & \mathbf{L}_3 \end{bmatrix}$$
$$\underbrace{\mathbf{I}}_{1 \times 3} \qquad \underbrace{\mathbf{G}}_{1 \times 3} \qquad \underbrace{\mathbf{L}}_{3 \times 3}$$

$$G = IL^{-1}$$

$$k_d = \|\mathbf{G}\|$$
$$\mathbf{N} = \frac{1}{k_d}\mathbf{G}$$

Color images

The case of RGB images

• get three sets of equations, one per color channel:

$$\mathbf{I}_{R} = k_{dR} \mathbf{N}^{T} - \text{ call this J}$$
$$\mathbf{I}_{G} = k_{dG} \mathbf{N}^{T} \mathcal{L}$$
$$\mathbf{I}_{B} = k_{dB} \mathbf{N}^{T} \mathcal{L}$$

- Simple solution: first solve for N using one channel
- Then substitute known \boldsymbol{N} into above equations to get \boldsymbol{k}_d s:

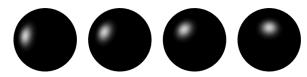
$$\mathbf{I}_{R} = k_{dR}\mathbf{J}$$
$$\mathbf{J} \cdot \mathbf{I}_{R} = k_{dR}\mathbf{J} \cdot \mathbf{J}$$
$$k_{dR} = \frac{\mathbf{J} \cdot \mathbf{I}_{R}}{\mathbf{J} \cdot \mathbf{J}}$$

Solve for N, k_d as before

What's the size of LL^T?

Computing light source directions

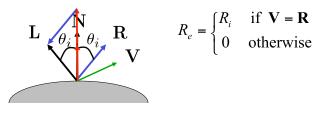
Trick: place a chrome sphere in the scene



· the location of the highlight tells you where the light source is

Recall the rule for specular reflection

For a perfect mirror, light is reflected about ${\bf N}$



We see a highlight when **V** = **R** • then L is given as follows:

 $L = 2(N \cdot R)N - R$

Computing the light source direction

Chrome sphere that has a highlight at position ${\boldsymbol{h}}$ in the image

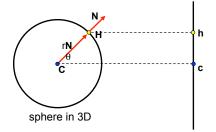
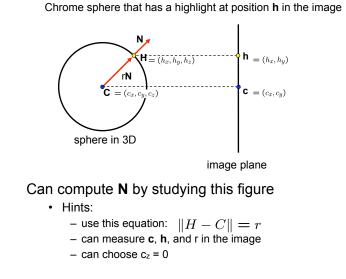


image plane

Can compute θ (and hence **N**) from this figure Now just reflect **V** about **N** to obtain **L**

Computing the light source direction



Depth from normals orthographic projection $V_1 = (x + 1, y, z_{x+1,y}) - (x, y, z_{xy})$ $= (1, 0, z_{x+1,y} - z_{xy})$ $0 = N \cdot V_1$ $= (n_x, n_y, n_z) \cdot (1, 0, z_{x+1,y} - z_{xy})$ $= n_x + n_z(z_{x+1,y} - z_{xy})$

Get a similar equation for V_2

- Each normal gives us two linear constraints on z
- compute z values by solving a matrix equation

Results...

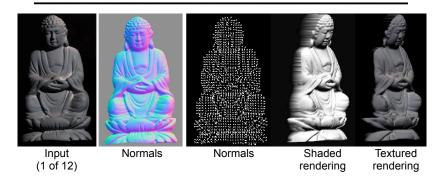






from Athos Georghiades http://cvc.yale.edu/people/Athos.html

Results...



Limitations

Big problems

- doesn't work for shiny things, semi-translucent things
- shadows, inter-reflections

Smaller problems

- · camera and lights have to be distant
- · calibration requirements
 - measure light source directions, intensities
 - camera response function

Trick for handling shadows

Weight each equation by the pixel brightness:

 $I_i(I_i) = I_i[k_d \mathbf{N} \cdot \mathbf{L_i}]$

Gives weighted least-squares matrix equation:

$$\begin{bmatrix} I_1^2 & \dots & I_n^2 \end{bmatrix} = k_d \mathbf{N}^T \begin{bmatrix} I_1 \mathbf{L}_1 & \dots & I_n \mathbf{L}_n \end{bmatrix}$$

Solve for N, k_d as before