Information Gain

Which test is more informative?

Split over whether Balance exceeds 50K



Less or equal 50K Over 50K

Split over whether applicant is employed



Unemployed

Information Gain

Impurity/Entropy (informal)

 Measures the level of impurity in a group of examples



Impurity



Entropy: a common way to measure impurity

• Entropy =
$$\sum_{i} - p_i \log_2 p_i$$



 \boldsymbol{p}_i is the probability of class i

Compute it as the proportion of class i in the set.

16/30 are green circles; 14/30 are pink crosses $log_2(16/30) = -.9;$ $log_2(14/30) = -1.1$ Entropy = -(16/30)(-.9) -(14/30)(-1.1) = .99

 Entropy comes from information theory. The higher the entropy the more the information content.

What does that mean for learning from examples?

2-Class Cases:

 What is the entropy of a group in which all examples belong to the same class?

 $- \text{ entropy} = -1 \log_2 1 = 0$

not a good training set for learning

• What is the entropy of a group with 50% in either class?

 $- \text{ entropy} = -0.5 \log_2 0.5 - 0.5 \log_2 0.5 = 1$

good training set for learning





Information Gain

- We want to determine which attribute in a given set of training feature vectors is most useful for discriminating between the classes to be learned.
- Information gain tells us how important a given attribute of the feature vectors is.
- We will use it to decide the ordering of attributes in the nodes of a decision tree.

Calculating Information Gain

Information Gain = entropy(parent) – [average entropy(children)]



Entropy-Based Automatic Decision Tree Construction

Training Set S $\begin{array}{c} x_1 = (f_{11}, f_{12}, \dots f_{1m}) \\ x_2 = (f_{21}, f_{22}, f_{2m}) \end{array}$ $x_n = (f_{n1}, f_{22}, f_{2m})$

Node 1 What feature should be used? What values?

Quinlan suggested information gain in his ID3 system and later the gain ratio, both based on entropy.

Using Information Gain to Construct a Decision Tree (1)



Simple Example

Training Set: 3 features and 2 classes



How would you distinguish class I from class II?





GAIN = 1 - (3/4)(.9184) - (1/4)(0) = .3112



Split on attribute Y

$$Y=1$$

$$I I$$

$$F_{child1}=0$$

$$F_{child2}=0$$

 $E_{parent} = 1$ GAIN = 1 –(1/2) 0 – (1/2)0 = 1; BEST ONE



Split on attribute Z

 $E_{parent} = 1$ GAIN = 1 - (1/2)(1) - (1/2)(1) = 0 ie. NO GAIN; WORST 13