### Announcements

• Midterm back today (end of class)

# Recognition





# Recognition





The "Margaret Thatcher Illusion", by Peter Thompson

- Readings
  C. Bishop, "Neural Networks for Pattern Recognition", Oxford University Press, 1998, Chapter 1.
  Forsyth and Ponce, 22.3 (eigenfaces)

# Recognition problems

What is it?

· Object detection

Who is it?

Recognizing identity

What are they doing?

• Activities

All of these are classification problems

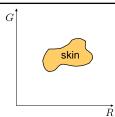
Choose one class from a list of possible candidates

### Face detection



How to tell if a face is present?

# One simple method: skin detection

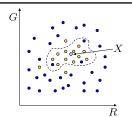


Skin pixels have a distinctive range of colors

- Corresponds to region(s) in RGB color space
  - for visualization, only R and G components are shown above

- A pixel X = (R,G,B) is skin if it is in the skin region
- But how to find this region?

### Skin detection



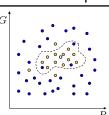
Learn the skin region from examples

- Manually label pixels in one or more "training images" as skin or not skin
   Plot the training data in RGB space
   skin pixels shown in orange, non-skin pixels shown in blue
- - some skin pixels may be outside the region, non-skin pixels inside. Why?

### Skin classifier

• Given X = (R,G,B): how to determine if it is skin or not?

### Skin classification techniques



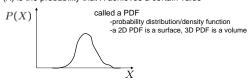
### Skin classifier

- Given X = (R,G,B): how to determine if it is skin or not?
- · Nearest neighbor
  - find labeled pixel closest to X
- choose the label for that pixel
- Data modeling
  - fit a model (curve, surface, or volume) to each class
- · Probabilistic data modeling
  - fit a probability model to each class

### Probability

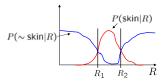
### Basic probability

- X is a random variable
- P(X) is the probability that X achieves a certain value



- $0 \le P(X) \le 1$
- $\int_{-\infty}^{\infty} P(X)dX = 1$  $\sum P(X) = 1$ discrete X
- Conditional probability: P(X | Y)
  - probability of X given that we already know Y

### Probabilistic skin classification



Now we can model uncertainty

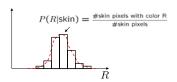
- Each pixel has a probability of being skin or not skin
  - $P(\sim \text{skin}|R) = 1 P(\text{skin}|R)$

### Skin classifier

- Given X = (R,G,B): how to determine if it is skin or not?
- · Choose interpretation of highest probability
  - set X to be a skin pixel if and only if  $R_1 < X \leq R_2$

Where do we get P(skin|R) and  $P(\sim \text{skin}|R)$  ?

### Learning conditional PDF's



We can calculate P(R | skin) from a set of training images

- It is simply a histogram over the pixels in the training images
- each bin R<sub>i</sub> contains the proportion of skin pixels with color R<sub>i</sub>

This doesn't work as well in higher-dimensional spaces. Why not?

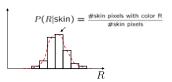


Approach: fit parametric PDF functions

- · common choice is rotated Gaussian

  - $\begin{array}{l} \text{- center } \mathbf{c} = \overline{X} \\ \text{- covariance } \sum_{X} (X \overline{X}) (X \overline{X})^T \end{array}$ 
    - » orientation, size defined by eigenvecs, eigenvals

### Learning conditional PDF's



We can calculate P(R | skin) from a set of training images

- · It is simply a histogram over the pixels in the training images
  - each bin R<sub>i</sub> contains the proportion of skin pixels with color R<sub>i</sub>

But this isn't quite what we want

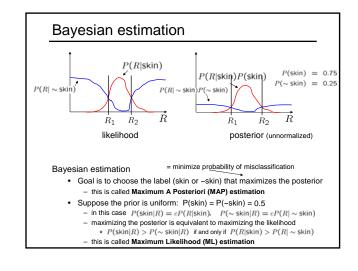
- · Why not? How to determine if a pixel is skin?
- We want P(skin | R) not P(R | skin)
- · How can we get it?

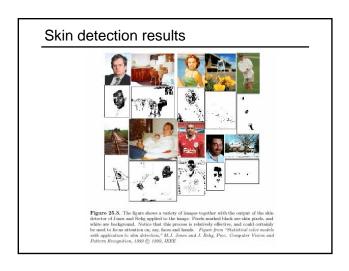
# Bayes rule $P(X|Y) = \frac{P(Y|X)P(X)}{P(Y)}$ In terms of our problem: $P(\mathsf{skin}|R) = \frac{P(R|\mathsf{skin})\ P(\mathsf{skin})}{P(R)} + \frac{P(R|\mathsf{skin})\ P(\mathsf{skin})}{P(R|\mathsf{skin})P(\mathsf{skin})+P(R|\sim\mathsf{skin})P(\sim\mathsf{skin})}$ What could we use for the prior P(skin)? • Could use domain knowledge - P(skin) may be larger if we know the image contains a person

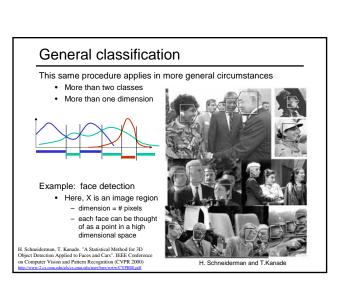
- for a portrait, P(skin) may be higher for pixels in the center

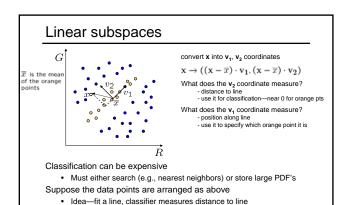
Could learn the prior from the training set. How?

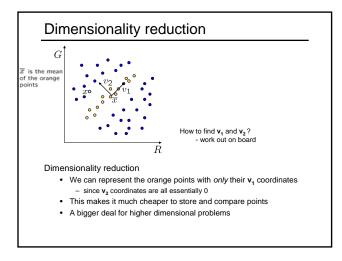
- P(skin) may be proportion of skin pixels in training set

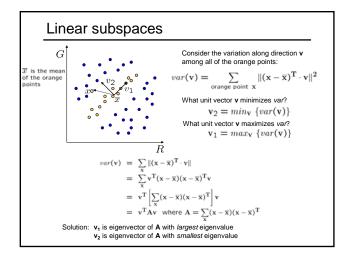












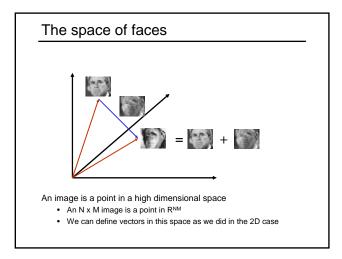
### Principal component analysis

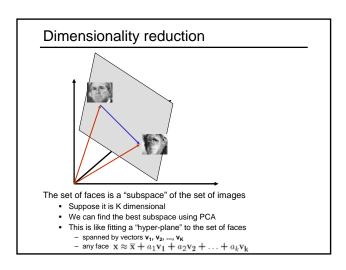
Suppose each data point is N-dimensional

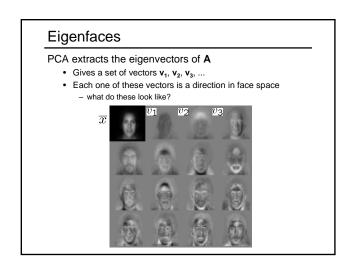
Same procedure applies:

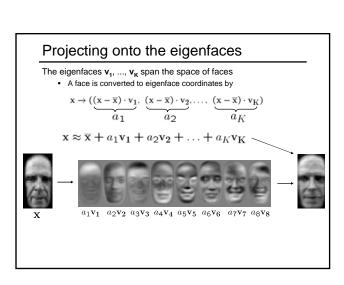
$$\begin{array}{ll} \mathit{var}(\mathbf{v}) &=& \sum\limits_{X} \|(\mathbf{x} - \overline{\mathbf{x}})^{\mathbf{T}} \cdot \mathbf{v}\| \\ &=& \mathbf{v}^{\mathbf{T}} \mathbf{A} \mathbf{v} \ \ \text{where} \ \mathbf{A} = \sum\limits_{X} (\mathbf{x} - \overline{\mathbf{x}}) (\mathbf{x} - \overline{\mathbf{x}})^{\mathbf{T}} \end{array}$$

- The eigenvectors of A define a new coordinate system
  - eigenvector with largest eigenvalue captures the most variation among training vectors x
  - eigenvector with smallest eigenvalue has least variation
- We can compress the data by only using the top few eigenvectors
  - corresponds to choosing a "linear subspace"
     » represent points on a line, plane, or "hyper-plane"
  - $\,-\,$  these eigenvectors are known as the  $\emph{principal components}$









# Recognition with eigenfaces

- 1. Process the image database (set of images with labels)

  - Run PCA—compute eigenfaces
    Calculate the K coefficients for each image
- 2. Given a new image (to be recognized)  $\mathbf{x}$ , calculate K coefficients

$$\mathbf{x} \to (a_1, a_2, \dots, a_K)$$

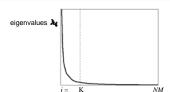
3. Detect if x is a face

$$\|\mathbf{x} - (\overline{\mathbf{x}} + a_1\mathbf{v}_1 + a_2\mathbf{v}_2 + \ldots + a_K\mathbf{v}_K)\| < \mathsf{threshold}$$

- 4. If it is a face, who is it?

  - Find closest labeled face in database
     nearest-neighbor in K-dimensional space

# Choosing the dimension K



How many eigenfaces to use?

Look at the decay of the eigenvalues

- the eigenvalue tells you the amount of variance "in the direction" of that eigenface
- ignore eigenfaces with low variance

# Object recognition

This is just the tip of the iceberg

- We've talked about using pixel color as a feature
- Many other features can be used:
  - edges
  - motion (e.g., optical flow)
  - object size
  - SIFT
- Classical object recognition techniques recover 3D information as well
  - given an image and a database of 3D models, determine which model(s) appears in that image
  - often recover 3D pose of the object as well