## Announcements

- Midterm due now
- Project 3 out today
- demo session at the end of class


## Photometric Stereo



Readings

- Forsyth and Ponce, section 5.4
- online: http://muw.cs.berkeley.edu/-daf/bookpages/pdf/chap05-final.pdf

Diffuse reflection


$$
R_{e}=k_{d} \mathbf{N} \cdot \mathbf{L} R_{i}
$$

image intensity of $\mathrm{P} \longrightarrow I=k_{d} \mathrm{~N} \cdot \mathrm{~L}$
Simplifying assumptions

- $I=R_{e}$ : camera response function $f$ is the identity function: - can always achieve this in practice by solving for $f$ and applying $f^{-1}$ to each pixel in the image
- $R_{i}=1$ : light source intensity is 1
- can achieve this by dividing each pixel in the image by $R_{i}$


## Shape from shading

| Suppose $k_{d}=1$ |  |
| ---: | :--- |
| $I$ | $=k_{d} \mathbf{N} \cdot \mathbf{L}$ |
|  | $=\mathbf{N} \cdot \mathbf{L}$ |
|  | $=\cos \theta_{i}$ |

You can directly measure angle between normal and light source

- Not quite enough information to compute surface shape
- But can be if you add some additional info, for example - assume a few of the normals are known (e.g., along silhouette)
- constraints on neighboring normals-"integrability" - smoothness
- Hard to get it to work well in practice
- plus, how many real objects have constant albedo?



## Solving the equations



$$
\begin{aligned}
\mathrm{G} & =\mathrm{IL}^{-1} \\
k_{d} & =\|\mathbf{G}\| \\
\mathrm{N} & =\frac{1}{k_{d}} \mathbf{G}
\end{aligned}
$$

## More than three lights

Get better results by using more lights

## Color images

The case of RGB images

- get three sets of equations, one per color channel:

$$
\begin{aligned}
& \mathbf{I}_{R}=k_{d R} \mathrm{~N}^{T} \mathcal{L} \\
& \mathbf{I}_{G}=k_{d G} \mathbf{N}^{T} \mathcal{L} \\
& \mathbf{I}_{B}=k_{d B} \mathbf{N}^{T} \mathcal{L}
\end{aligned} \quad \text { call this } \mathbf{J}, \quad \text { What's the size of } \mathrm{J} ?
$$

- Simple solution: first solve for $\mathbf{N}$ using one channel
- Then substitute known $\mathbf{N}$ into above equations to get $\mathrm{k}_{\mathrm{d}} \mathrm{s}$ :

$$
\begin{aligned}
\mathbf{I}_{R} & =k_{d R} \mathbf{J} \\
\mathbf{J} \cdot \mathbf{I}_{R} & =k_{d R} \mathbf{J} \cdot \mathbf{J} \\
k_{d R} & =\frac{\mathbf{J} \cdot \mathbf{I}_{R}}{\mathbf{J} \cdot \mathbf{J}}
\end{aligned}
$$

## Computing light source directions

Trick: place a chrome sphere in the scene


Recall the rule for specular reflection
For a perfect mirror, light is reflected about $\mathbf{N}$
$R_{e}=\left\{\begin{array}{cc}R_{i} & \text { if } \mathbf{V}=\mathbf{R} \\ 0 & \text { otherwise }\end{array}\right.$

L

We see a highlight when $\mathbf{V}=\mathbf{R}$

- then $L$ is given as follows:
$\mathbf{L}=2(\mathbf{N} \cdot \mathbf{R}) \mathbf{N}-\mathbf{R}$

Computing the light source direction
Depth from normals
Chrome sphere that has a highlight at position $\mathbf{h}$ in the image


Can compute $\mathbf{N}$ by studying this figure

- Hints:
- use this equation: $\|H-C\|=r$
- can measure $\mathbf{c}, \mathbf{h}$, and $r$ in the image


Get a similar equation for $\mathbf{V}_{2}$

- Each normal gives us two linear constraints on z
- compute z values by solving a matrix equation (project 3)



## Limitations

Big problems

- doesn't work for shiny things, semi-translucent things
- shadows, inter-reflections

Smaller problems

- camera and lights have to be distant
- calibration requirements
- measure light source directions, intensities
- camera response function


## Trick for handling shadows

Weight each equation by the pixel brightness:

$$
I_{i}\left(I_{i}\right)=I_{i}\left[k_{d} \mathbf{N} \cdot \mathbf{L}_{\mathrm{i}}\right]
$$

Gives weighted least-squares matrix equation:

$$
\left[\begin{array}{lll}
I_{1}^{2} & \ldots & I_{n}^{2}
\end{array}\right]=k_{d} \mathbf{N}^{T}\left[\begin{array}{lll}
I_{1} \mathbf{L}_{1} & \ldots & I_{n} \mathbf{L}_{\mathbf{n}}
\end{array}\right]
$$

Solve for $N, k_{d}$ as before

