## Making Panoramas

#### Input:



### Output:



# Input: A set of images taken from the same optical center.

For this project, the images will also have the same horizontal orientation.



### Steps

- 1. Convert each image to cylindrical coordinates.
  - a. Remove radial distortion.
- 2. Find the alignment parameters between each adjacent pair of images.
- 3. Blend the images into a single panorama.

1. Convert each image to cylindrical coordinates.

The image plane is z = 1.
We compute the inverse transformation of (θ, y, 1) onto the image plane:

$$\Box x = \tan \theta$$

$$\Box \quad y = y / \cos \theta$$





a. Remove radial distortion.

Again, perform the inverse transformation on (x,y):
x´ = x + κ<sub>1</sub>r<sup>2</sup>x + κ<sub>2</sub>r<sup>4</sup>x
y´ = y + κ<sub>1</sub>r<sup>2</sup>y + κ<sub>2</sub>r<sup>4</sup>y

2. Find the alignment parameters between each adjacent pair of images.

- The images lie on a cylinder and have the same horizontal orientation.
- Therefore we can represent the alignment by a single (u,v) offset.



2. Find the alignment parameters between each adjacent pair of images.

The Lucas-Kanade optical flow algorithm can discover this offset.

$$\Box \quad \mathbf{I}_{x}u + \mathbf{I}_{y}v = -\mathbf{It} \text{ at each pixel.}$$

- We have two unknowns and many equations, so we can solve this with a 2-by-2 least-squares system.
- We do this for each level of the image pyramid, traversing coarse-to-fine.

# 3. Blend the images into a single panorama.



What do we do with pixels shared by multiple images?

- 3. Blend the images into a single panorama.
  - Have each image *i* assign a weight α<sub>i</sub> to each pixel. Then, the color of a pixel (*r*,*g*,*b*) in the panorama is:

$$(r,g,b) = \frac{\sum_{i} \alpha_{i}(r_{i},g_{i},b_{i})}{\sum_{i} a_{i}}$$

- 3. Blend the images into a single panorama.
  - Assigning weights:
  - i. Uniform weights ( $\alpha_i = 1$  for all *i*).
  - ii. Horizontal hat function ( $\alpha_i$  inversely proportional to distance from horizontal center, within some window.
  - iii. Something else?



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### Project 4

For Project 4, you will make a panorama.

- Most of the code has been given to you. You only need to write code for:
  - Forming and solving the matrix equation in Lucas-Kanade flow estimation.

□ Image blending.

This project should be less timeconsuming than the last.