## Making Panoramas

## Input:



## Output:



## - Input:

$\square$ A set of images taken from the same optical center.
$\square$ For this project, the images will also have the same horizontal orientation.


## Steps

1. Convert each image to cylindrical coordinates.
a. Remove radial distortion.
2. Find the alignment parameters between each adjacent pair of images.
3. Blend the images into a single panorama.

## 1. Convert each image to cylindrical coordinates.

The image plane is $z=1$.
We compute the inverse transformation of $(\theta, y, 1)$ onto the image plane:
$\square \quad x=\tan \theta$
$\square \quad y=y / \cos \theta$
$\square \quad z=1$

a. Remove radial distortion.

- Again, perform the inverse transformation on ( $x, y$ ):
$\square \quad x^{\prime}=x+K_{1} r^{2} x+K_{2} r^{4} x$
$\square \quad y^{\prime}=y+K_{1} r^{2} y+\kappa_{2} r^{4} y$

2. Find the alignment parameters between each adjacent pair of images.

- The images lie on a cylinder and have the same horizontal orientation.
- Therefore we can represent the alignment by a single ( $u, v$ ) offset.


2. Find the alignment parameters between each adjacent pair of images.

The Lucas-Kanade optical flow algorithm can discover this offset.
$\square \quad I_{x} u+I_{y} v=-$ It at each pixel.
$\square \quad$ We have two unknowns and many equations, so we can solve this with a 2-by-2 least-squares system.

- We do this for each level of the image pyramid, traversing coarse-to-fine.

3. Blend the images into a single panorama.


- What do we do with pixels shared by multiple images?


## 3. Blend the images into a single panorama.

Have each image $i$ assign a weight $\alpha_{i}$ to each pixel. Then, the color of a pixel ( $r, g, b$ ) in the panorama is:

$$
(r, g, b)=\frac{\sum_{i} \alpha_{i}\left(r_{i}, g_{i}, b_{i}\right)}{\sum_{i} a_{i}}
$$

## 3. Blend the images into a single panorama.

Assigning weights:
i. Uniform weights ( $\alpha_{i}=1$ for all $i$ ).
ii. Horizontal hat function ( $\alpha_{i}$ inversely proportional to distance from horizontal center, within some window.

iii. Something else?


## Project 4

- For Project 4, you will make a panorama.
- Most of the code has been given to you. You only need to write code for:
$\square$ Forming and solving the matrix equation in Lucas-Kanade flow estimation.
$\square$ Image blending.

■ This project should be less timeconsuming than the last.

