Announcements

- · Project 3 out today
 - demo session at the end of class

Photometric Stereo



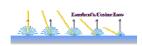
Merle Norman Cosmetics, Los Angeles

Readings

- Forsyth and Ponce, section 5.4
 - online: http://www.cs.berkeley.edu/~daf/bookpages/pdf/chap05-final.pdf

Diffuse reflection





$$R_e = k_d \mathbf{N} \cdot \mathbf{L} R_i$$

image intensity of $\mathbf{P} \longrightarrow I = k_d \mathbf{N} \cdot \mathbf{L}$

Simplifying assumptions

- I = R_e : camera response function f is the identity function:
 - can always achieve this in practice by solving for f and applying f⁻¹ to each pixel in the image
- R_i = 1: light source intensity is 1
 - can achieve this by dividing each pixel in the image by R_i

Shape from shading



Suppose
$$k_d = 1$$

$$I = k_d \mathbf{N} \cdot \mathbf{L}$$

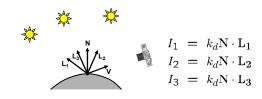
$$= \mathbf{N} \cdot \mathbf{L}$$

$$= \cos \theta_i$$

You can directly measure angle between normal and light source

- · Not quite enough information to compute surface shape
- But can be if you add some additional info, for example
 - assume a few of the normals are known (e.g., along silhouette)
 - constraints on neighboring normals—"integrability"
 - smoothness
- · Hard to get it to work well in practice
 - plus, how many real objects have constant albedo?

Photometric stereo



Can write this as a matrix equation:

$$\left[\begin{array}{ccc}I_1 & I_2 & I_3\end{array}\right] = k_d \mathbf{N}^T \left[\begin{array}{ccc}\mathbf{L}_1 & \mathbf{L}_2 & \mathbf{L}_3\end{array}\right]$$

Solving the equations

$$\begin{bmatrix} I_1 & I_2 & I_3 \end{bmatrix} = k_d \mathbf{N}^T \begin{bmatrix} \mathbf{L}_1 & \mathbf{L}_2 & \mathbf{L}_3 \end{bmatrix}$$

$$\mathbf{G} = \mathbf{I} \mathbf{L}^{-1}$$

$$k_d = \|\mathbf{G}\|$$

$$\mathbf{N} = \frac{1}{k_d} \mathbf{G}$$

More than three lights

Get better results by using more lights

$$\begin{bmatrix} I_1 & \dots & I_n \end{bmatrix} = k_d \mathbf{N}^T \begin{bmatrix} \mathbf{L}_1 & \dots & \mathbf{L}_n \end{bmatrix}$$

Least squares solution:

$$\begin{split} \mathbf{I} &= \mathbf{GL} \\ \mathbf{IL^T} &= \mathbf{GLL^T} \\ \mathbf{G} &= (\mathbf{IL^T})(\mathbf{LL^T})^{-1} \end{split}$$

Solve for N, k_d as before

What's the size of LLT?

Color images

The case of RGB images

• get three sets of equations, one per color channel:

$$\mathbf{I}_R = k_{dR} \mathbf{N}^T \mathcal{L}$$
 call this \mathbf{J} $\mathbf{I}_G = k_{dG} \mathbf{N}^T \mathcal{L}$ $\mathbf{I}_B = k_{dB} \mathbf{N}^T \mathcal{L}$

- Simple solution: first solve for ${\bf N}$ using one channel
- Then substitute known ${f N}$ into above equations to get ${\bf k}_{\rm d}$ s:

$$\begin{aligned} \mathbf{I}_{R} &= k_{dR}\mathbf{J} \\ \mathbf{J} \cdot \mathbf{I}_{R} &= k_{dR}\mathbf{J} \cdot \mathbf{J} \\ k_{dR} &= \frac{\mathbf{J} \cdot \mathbf{I}_{R}}{\mathbf{J} \cdot \mathbf{J}} \end{aligned}$$

Computing light source directions

Trick: place a chrome sphere in the scene





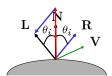




• the location of the highlight tells you where the light source is

Recall the rule for specular reflection

For a perfect mirror, light is reflected about ${\bf N}$



$$R_e = \begin{cases} R_i & \text{if } \mathbf{V} = \mathbf{R} \\ 0 & \text{otherwise} \end{cases}$$

We see a highlight when V = R

• then L is given as follows:

$$L = 2(N \cdot R)N - R$$

Computing the light source direction

Chrome sphere that has a highlight at position **h** in the image

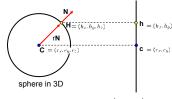
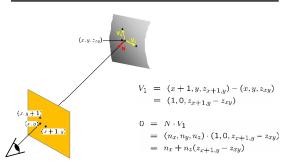


image plane

Can compute N by studying this figure

- · Hints:
 - use this equation: $\|H C\| = r$
 - can measure **c**, **h**, and **r** in the image

Depth from normals



Get a similar equation for V2

- Each normal gives us two linear constraints on z
- compute z values by solving a matrix equation (project 3)

Project 3





Limitations

Big problems

- · doesn't work for shiny things, semi-translucent things
- · shadows, inter-reflections

Smaller problems

- · camera and lights have to be distant
- · calibration requirements
 - measure light source directions, intensities
 - camera response function

Trick for handling shadows

Weight each equation by the pixel brightness:

$$I_i(I_i) = I_i[k_d \mathbf{N} \cdot \mathbf{L_i}]$$

Gives weighted least-squares matrix equation:

$$\begin{bmatrix} I_1^2 & \dots & I_n^2 \end{bmatrix} = k_d \mathbf{N}^T \begin{bmatrix} I_1 \mathbf{L}_1 & \dots & I_n \mathbf{L}_n \end{bmatrix}$$

Solve for N, $k_{\rm d}$ as before