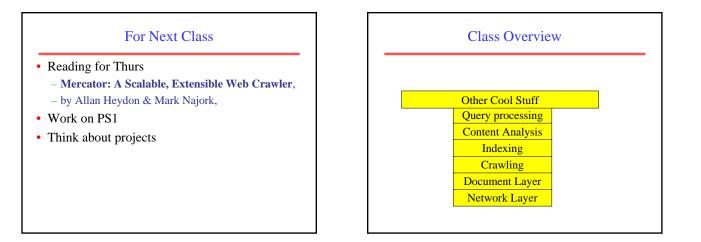
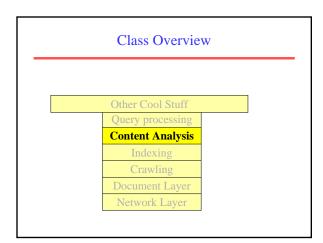
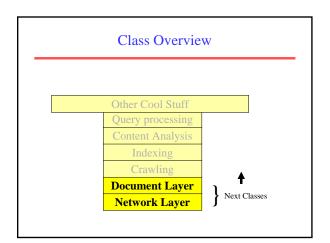


## Administrivia

- Mailing List
- Groups for PS1
- Questions on PS1?
  - See discussion & pseudocode for naive Bayes in "Information Retrieval" by Manning, Raghavan, and Schutze
  - Good textbook and available online for free

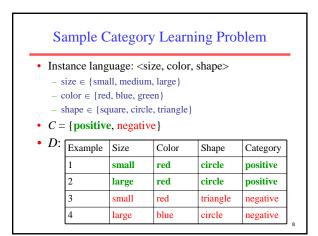


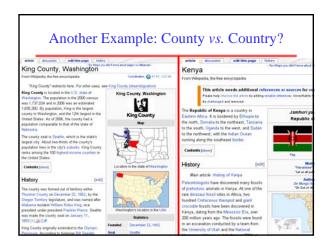


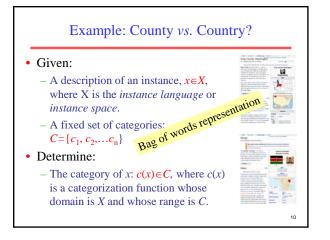


#### Categorization

- Given:
  - A **description of an instance**,  $x \in X$ , where X is the *instance language* or *instance space*.
  - A fixed set of categories:
  - $C = \{c_1, c_2, \dots c_n\}$
- Determine:
  - The **category of** x:  $c(x) \in C$ , where c(x) is a categorization function whose domain is X and whose range is C.



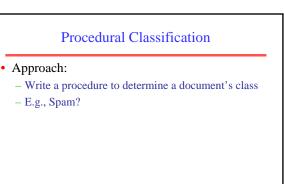




# Text Categorization

- Assigning documents to a fixed set of categories, *e.g.*Web pages
- Web pages
  Yahoo-like classification
- What else?
- Email messages
  - Spam filtering
  - Prioritizing
  - Folderizing
- · News articles
- Personalized newspaper
- Web Ranking
  - Is page related to selling something?

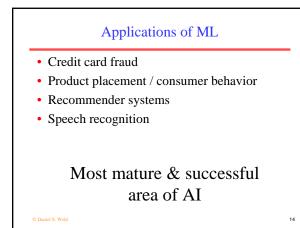
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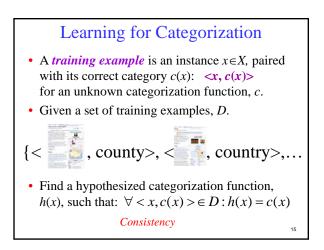


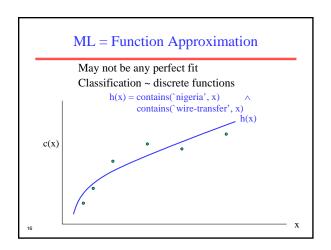


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- Hard to construct text categorization functions.
- Learning Algorithms:
  - Bayesian (naïve)
  - Neural network
  - Relevance Feedback (Rocchio)
  - Rule based (C4.5, Ripper, Slipper)
  - Nearest Neighbor (case based)
  - Support Vector Machines (SVM)

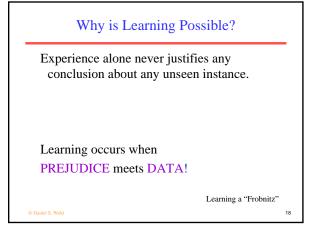


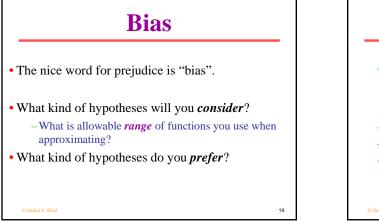




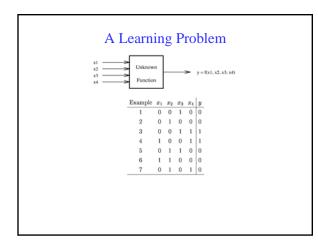
### Generalization

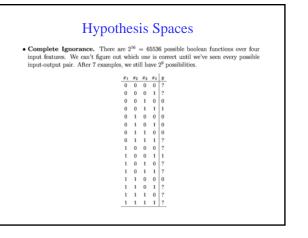
- Hypotheses must *generalize* to correctly classify instances not in the training data.
- Simply memorizing training examples is a consistent hypothesis *that does not generalize*.











## Terminology

- Training example. An example of the form (x, f(x)).
- Target function (target concept). The true function f.
- Hypothesis. A proposed function h believed to be similar to f.
- Concept. A boolean function. Examples for which f(x) = 1 are called positive examples or positive instances of the concept. Examples for which f(x) = 0 are called negative examples or negative instances.
- Classifier. A discrete-valued function. The possible values  $f(\mathbf{x}) \in \{1, ..., K\}$  are called the classes or class labels.
- Hypothesis Space. The space of all hypotheses that can, in principle, be output by a learning algorithm.
- Version Space. The space of all hypotheses in the hypothesis space that have not yet been ruled out by a training example.

#### General Learning Issues

- Many hypotheses consistent with the training data.
- Bias
  - Any criteria other than consistency with the training data that is used to select a hypothesis.
- Classification accuracy
  - % of instances classified correctly
  - (Measured on independent test data.)
- Training time
- Efficiency of training algorithm
- Testing time
  - Efficiency of subsequent classification

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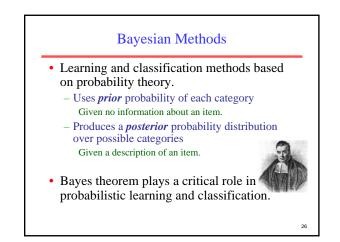


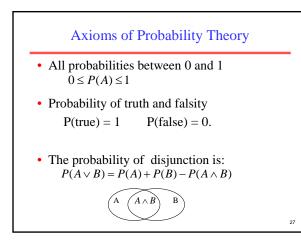
- Restriction bias: use prior knowledge to specify a restricted hypothesis space.
   Naïve Bayes Classifier
- Preference bias: use a broad hypothesis space, but impose an ordering on the hypotheses.

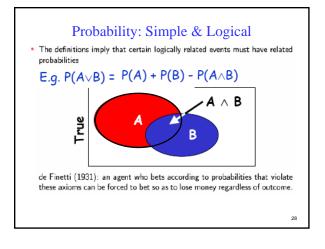
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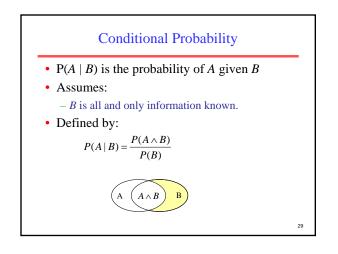
-Decision trees.

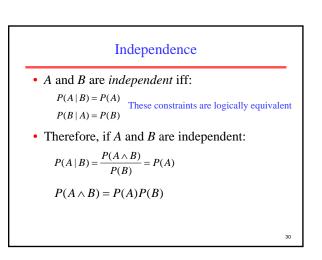
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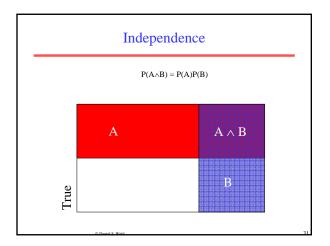


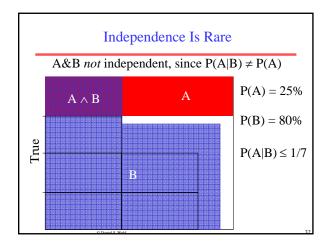


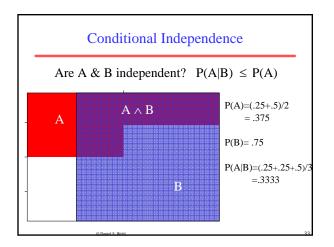


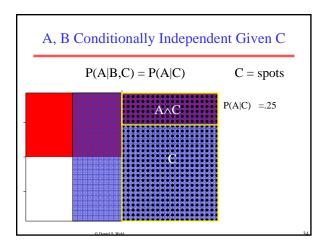


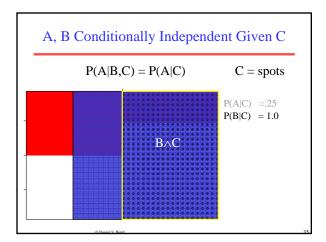


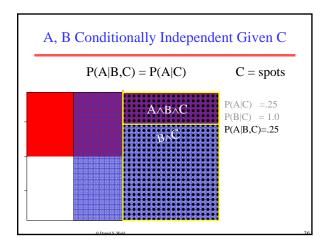


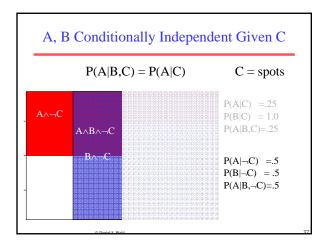


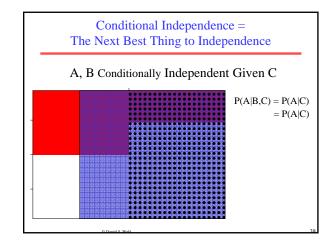


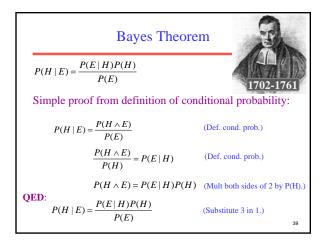


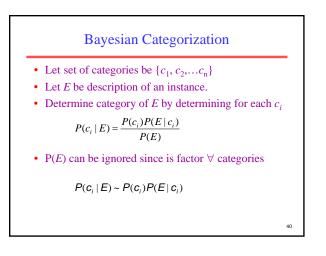


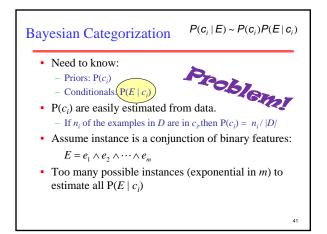


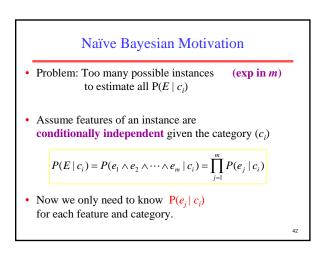


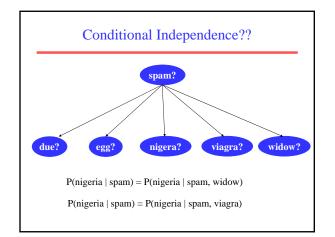


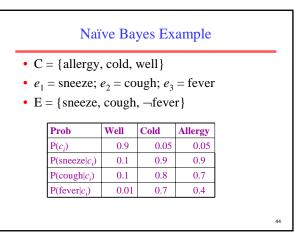


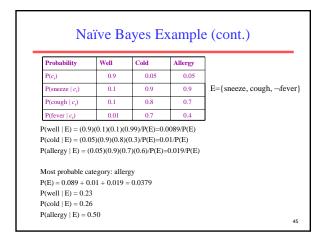


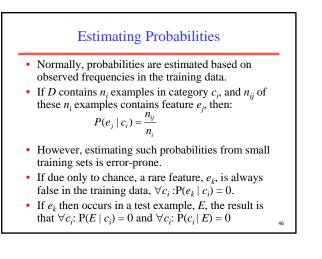












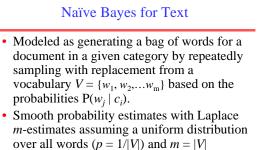
#### Smoothing

- To account for estimation from small samples, probability estimates are adjusted or *smoothed*.
- **Laplace smoothing** using an *m*-estimate assumes that each feature is given a prior probability, *p*, that is assumed to have been previously observed in a "virtual" sample of size *m*.

$$P(e_{j} | c_{i}) = \frac{n_{ij} + mp}{n_{i} + m} = (n_{ij} + 1) / (n_{i} + 2)$$

• For binary features, p is simply assumed to be 0.5.

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- Equivalent to a virtual sample of seeing each word in each category exactly once.

#### Text Naïve Bayes Algorithm (Train)

Let V be the vocabulary of all words in the documents in D For each category  $c_i \in C$ 

Let  $D_i$  be the subset of documents in D in category  $c_i$  $P(c_i) = |D_i| / |D|$ 

Let  $T_i$  be the concatenation of all the documents in  $D_i$ Let  $n_i$  be the total number of word occurrences in  $T_i$ For each word  $w_i \in V$ 

Let  $n_{ij}$  be the number of occurrences of  $w_j$  in  $T_i$ Let  $P(w_i | c_i) = (n_{ij} + 1) / (n_i + |V|)$ 

## Text Naïve Bayes Algorithm (Test)

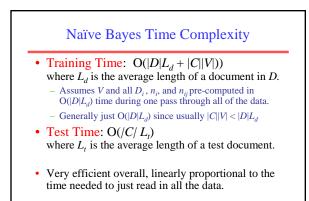
Given a test document XLet n be the number of word occurrences in XReturn the category:

$$\underset{c \in C}{\operatorname{argmax}} P(c_i) \prod_{i=1}^n P(a_i \mid c_i)$$

where  $a_i$  is the word occurring the *i*th position in X

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• But...

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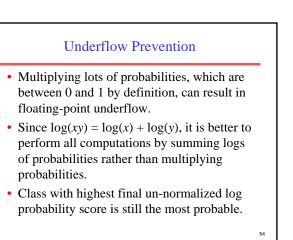
• If you do... it probably won't work...

## Probabilities: Important Detail! • $P(spam | E_1 ... E_n) = \prod_i P(spam | E_i)$ Any more potential problems here?

• We are multiplying lots of small numbers Danger of underflow!

■ 0.5<sup>57</sup> = 7 E - 18

- Solution? Use logs and add!
  - $p_1 * p_2 = e^{\log(p1) + \log(p2)}$
  - Always keep in log form



## Naïve Bayes Posterior Probabilities

- Classification results of naïve Bayes
  - I.e. the class with maximum posterior probability...Usually fairly accurate (?!?!?)
- However, due to the inadequacy of the conditional independence assumption...
  - Actual posterior-*probability* estimates *not* accurate.
  - Output probabilities generally very close to 0 or 1.

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#### **Multi-Class Categorization**

- Pick the category with max probability
- Create many 1 vs other classifiers
- Use a hierarchical approach (wherever hierarchy available)

