DISKLESS STABLE STORAGE

Ellis Michael

ADMINISTRIVIA

• Lab 4 home stretch!

Problem Set 3 due Wednesday.

• Fill out course evaluation!

THIS WEEK

- New research!
- Work being done at UW by Arvind and me!
 - Diskless stable storage (Today)
 - Datacenter networking and Speculative Paxos (Wednesday)
 - Programmable networks and NOPaxos and Eris (Friday)

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WHAT IF WE HAVE STABLE STORAGE?

Simple method:

- Each node has an attached disk.
- Node synchronously writes message (or timer) to disk before handling it.
- After node fails, upon restart replay log to restore server to previous state since handlers are deterministic.
- Can periodically write full state to disk to clear event log and free space.
- This method works for *any* distributed protocol.



PROBLEM #1: SYNCHRONOUS WRITES TO DISK ARE SLOW (REALLY SLOW) (YES, EVEN IF YOU USE AN SSD)

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We can even skip logging everything except P1A messages. Then, recovering acceptors must either recover all proposals from the latest leader or wait for a new leader to take over.

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• Only invariant a leader needs stable storage to enforce is avoiding using the same ballot with different values.

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Acceptor State

- Write PIA messages synchronously to disk.
- Need to learn about accepted values.
- Solution: learn about missing P2As from the recent leader (or a future one which reads from a quorum not including this node).

- Should save state to disk before garbage collection.
- Everything else can be rebuilt by re-learning accepted values.

Allows acceptors to "forget" certain P2As but still safe. (Why?)

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Certain storage and recovery schemes yield weaker liveness conditions.





PROBLEM #2: DISKS CAN FAIL!

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However, getting diskless recovery right is tricky.

VIEWSTAMPED REPLICATION (REVISITED)

VR is a state-machine re Paxos.

A later version contained a **diskless recovery protocol** that was supposed to allow nodes to recover even when they didn't write any proposals or leader change messages to disk.

VR is a state-machine replication protocol akin to

- Sends (RECOVERY, x) to all other nodes, where x is a unique value to guarantee freshness.
- 2. Nodes that are currently OPERATIONAL (not recovering) respond with
 (RECOVERY-RESPONSE, x, b, l, where b is its
 ballot number and l is its log.
- 3. The recovering node waits for responses from a majority, including one from the leader node associated with the largest ballot seen. It updates its own log and returns its status to OPERATIONAL.



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GOAL: EMULATE STABLE STORAGE

- returned by one read is returned by later reads).
- We want these guarantees to hold even across node failures.
- Nodes can use this set just like stable storage. Therefore, any stable storage is replaced by our diskless storage.

• Our goal is to provide each node with a set that it can add values to and read from. This set need only support a single writer/reader.

 We want to guarantee that values written are later returned and that completed reads are monotonic (i.e., that a value in the set

protocol that is safe with stable storage will still be safe when

- Nodes can crash and restart.
- Upon restart, they lose all of their local state.
- Restarting nodes run a recovery protocol to re-learn any necessary information.
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- Nodes record this clock value upon beginning recovery. This is called the node's incarnation ID.



CRASH VECTORS

- Each node maintains a crash vector, with one entry per node containing the largest incarnation ID known for that node.
- Crash vectors are attached to set operation messages and recovery messages.
- Upon receiving messages, nodes update each entry in their local crash vector, taking the maximum of that entry and the one in the message.

v: 2 3 1 0 1 p_1 p_2 p_3 p_4 p_5

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- This works just like a vector clock!

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CRASH CONSISTENCY

• Two messages with crash vectors v_1 and v_2 , sent by p_1 and p_2 , respectively, are crash-consistent if:

That is, if p₁ doesn't know about a later incarnation of p₂ and viceversa.

- crash-consistent.
- Again, this works exactly like a vector clock.

 $v_1[p_2] \le v_2[p_2]$ and $v_2[p_1] \le v_1[p_1]$

• Similarly, a set of messages is crash-consistent if they are pairwise

STATUS

At any given time, each node has one of three statuses: **OPERATIONAL, DOWN, or RECOVERING.**

- recovery.
- finished the recovery procedure.

A node that is DOWN has crashed and has not yet begun

A node that is RECOVERING has restarted but hasn't yet

A node that is OPERATIONAL has either never crashed or has finished recovering from its most recent crash.

Persistent local state:

- *n* (number of nodes)
- *i* (node ID)

- v (local crash vector)
- σ (current status)
- S (local set)
- Nodes update their crash vectors when receiving a message.
- Nodes can match requests with replies.

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IS IT CORRECT?



QUORUM KNOWLEDGE

- We say that quorum Q knows X if, for all nodes $p \in Q$:
 - 1. p is DOWN,
 - 2. p is OPERATIONAL and knows X, or
 - recovery (if it doesn't crash again first).
- We are concerned with two kinds of quorum knowledge: IDs.

3. *p* is RECOVERING and *guaranteed* to know X upon finishing

knowledge of written values and knowledge of incarnation

Suppose quorum *Q* knows *X* (either an incarnation ID or written value). We will show this knowledge persists by induction.

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- If that node manages to eventually recover, it must use a quorum of OPERATIONAL nodes.

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- Finally, sets σ to OPERATIONAL, declaring the end of recovery.



Suppose quorum *Q* knows *X* (either an incarnation ID or written value). We will show this knowledge persists by induction.

- The only step a node can take to falsify our invariant is beginning recovery.
- If that node manages to eventually recover, it must use a quorum of OPERATIONAL nodes.
- That quorum will contain at least one node from *Q*, which by induction knows *X*.

write(s)

- Sends $\langle WRITE, v, s \rangle$ to all nodes
- Currently operational nodes add *s* to their local set, respond with \langle WRITE-REPLY, *v*, *s* \rangle
- Writer waits for a *crash-consistent* set of replies from a majority, resending when necessary.

read()

• Simply returns its local set

- Sets its entry in its local crash vector to be its new incarnation ID
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- If that node manages to eventually recover, it must use a quorum of OPERATIONAL nodes.
- That quorum will contain at least one node from *Q*, which by induction knows *X*.
- Therefore, our node will learn *X* if/when it finishes recovery.

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- We want to show that a crash-consistent set of replies implies quorum knowledge.
- For writes, we want to know that the value being written was persisted.
- On recovery, we want to know that our new (larger) incarnation ID was persisted.

We will prove this by induction. replies for X from quorum Q, then Q knows X.

and p is currently OPERATIONAL, then p knows X.

- **Invariant 1**: If a node receives a crash-consistent set of
- Invariant 2: If node *p* ever sent a reply that makes it into a crash-consistent set of replies for X from a quorum,

Suppose *p* received a crash-consistent set of replies from *Q*.

Invariant 1: If a node receives a crashconsistent set of replies for X from quorum Q, then Q knows X.



Suppose *p* received a crash-consistent set of replies from *Q*.

Then, for all nodes in *Q*, *at the time they sent their replies*, they hadn't yet helped any other node in *Q* recover to a later incarnation (than the one that sent the reply).

Invariant 1: If a node receives a crashconsistent set of replies for *X* from quorum *Q*, then *Q* knows *X*.



Suppose *p* received a crash-consistent set of replies from *Q*.

Then, for all nodes in *Q*, at the time they sent their replies, they hadn't yet helped any other node in *Q* recover to a later incarnation (than the one that sent the reply).

Otherwise, by induction, it would have known about that later incarnation and the replies wouldn't be crash-consistent.

Invariant 1: If a node receives a crashconsistent set of replies for *X* from quorum *Q*, then *Q* knows *X*.



Now, suppose for the sake of contradiction, that a node in $p \in Q$ is OPERATIONAL but does not know *X*.

Invariant 1: If a node receives a crashconsistent set of replies for *X* from quorum *Q*, then *Q* knows *X*.



Now, suppose for the sake of contradiction, that a node in $p \in Q$ is OPERATIONAL but does not know *X*.

It must have crashed and recovered since sending its reply. At least one of the nodes that helped it recover must have been in *Q* (by quorum intersection). Call that node *r*.

Invariant 1: If a node receives a crashconsistent set of replies for *X* from quorum *Q*, then *Q* knows *X*.



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It must have crashed and recovered since sending its reply. At least one of the nodes that helped it recover must have been in Q (by quorum intersection). Call that node r.

As we just showed, *r* couldn't have participated in the recovery before sending its own reply. But then by induction, it would have known *X* during the recovery, implying that *p* now knows *X*.

Invariant 1: If a node receives a crashconsistent set of replies for *X* from quorum *Q*, then *Q* knows *X*.



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Contradiction. Invariant 1 holds.

Invariant 1: If a node receives a crashconsistent set of replies for *X* from quorum *Q*, then *Q* knows *X*.



Crash-consistent replies for p's recovery

>n/2

p

>n/2

r

Crash-consistent replies for X



Next, suppose that *p* sent a reply that will make it into a crash-consistent set of replies and is currently operational but doesn't know *X*.

Again, it must have crashed and recovered, and there must be some node in the intersection of those that it recovered from and the other nodes that sent replies, *r*.

When could *r* send its reply for *X*?

p would know X (Invariant 2)

Not crash-consistent (Invariant 2)

r sends the RECOVERY-REPLY to *p*

Not crash-consistent (Invariant I + Persistence of Quorum Knowledge)

p finishes recovery

Invariant 1: If a node receives a crashconsistent set of replies for *X* from quorum *Q*, then *Q* knows *X*.



COMPLETED WRITES ENSURE QUORUM KNOWLEDGE, WHICH IS PERSISTENT!

WHAT DID WE ACCOMPLISH?

- We created a set which a writer can store values in. Upon recovery, the writer will re-learn the values of all completed writes.
- We can run *n* copies of this protocol in parallel, one for each server.
- when disk-based storage is replaced with our diskless storage.
- diskless storage when disks fail.
- If latency between nodes is small, writing to diskless storage is faster.
- But what about liveness?

• Any protocol which is safe when you assume stable storage will be safe

• Furthermore, you could recover from disk normally and only recover from

WHEN DISKLESS STORAGE IS LIVE

- recover (depending on what you were storing).
- So, we can't hope for the same liveness guarantees. Moreover,
- If, for all points in time, there is always some quorum that is operational, we can make progress.
- don't need consensus!

 Obviously, if all servers crash simultaneously and you don't have stable storage, you're stuck. If you have stable storage, you could still

specifying exactly when this protocol can make progress is hard.

 If there exists some particular quorum that stays OPERATIONAL long enough, then our diskless stable storage algorithm is wait-free! We

QUESTIONS?

