

Unsupervised Learning: K-Means & Agglomerative Clustering

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Types of Learning

	from input <i>x</i> , output:
unsupervised	summary z
supervised	prediction y
reinforcement	action a to maximize reward r

Types of Learning



Unsupervised Learning

- Supervised learning used labeled data pairs (x, y) to learn a function f : X→Y
 - But, what if we don't have labels?
- No labels = unsupervised learning

Clustering

Clustering: group together similar points and represent them with a single token

Key Design Choices:

1) What makes two data points similar?

2) How do we compute an overall grouping from pairwise similarities?

How might we cluster?

- K-means
 - Iteratively re-assign points to the nearest cluster center
- Agglomerative clustering
 - Start with each point as its own cluster and iteratively merge the closest clusters

Clustering Data



K-Means (k, X)

- Randomly choose k cluster center locations (centroids)
- Loop until convergence
 - Assign each point to the cluster of the closest centroid
 - Re-estimate the cluster centroids based on the data assigned to each cluster



K-Means (k, X)

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K-Means Objective Function

• K-means finds a local optimum of the following objective function:

$$\arg\min_{\boldsymbol{\mathcal{S}}} \sum_{i=1}^{k} \sum_{\mathbf{x} \in \mathcal{S}_{i}} \|\mathbf{x} - \boldsymbol{\mu}_{i}\|_{2}^{2}$$

where
$$S = \{S_1, \dots, S_k\}$$
 is a partitioning over
 $X = \{\mathbf{x}_1, \dots, \mathbf{x}_n\}$ s.t. $X = \bigcup_{i=1}^k S_i$
and $\boldsymbol{\mu}_i = \operatorname{mean}(S_i)$

K-means Demo



K-Means pros and cons

• Pros

- Finds cluster centers that minimize variance (good representation of data)
- Easy to implement
- Cons
 - Need to choose K
 - Sensitive to outliers
 - Prone to local minima
 - All clusters have the same parameters (e.g., distance measure is non-adaptive)



K-means Demo

K-Means: initialization

- Very sensitive to the initial points
 - Do many runs of K-Means, each with different initial centroids
 - Seed the centroids using a better method than randomly choosing the centroids
 - e.g., Farthest-first sampling
- Must manually choose k
 - Learn the optimal k for the clustering
 - Note that this requires a performance measure

K-medoids

- Just like K-means except
 - Represent the cluster with one of its members, rather than the mean of its members
 - Choose the member (data point) that minimizes cluster dissimilarity

Applicable when a mean is not meaningful
 – E.g., clustering values of hue

How might we cluster?

- K-means
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 Say "Every point is its own cluster"

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K-means and Hierarchical Clustering: Slide 40

- Say "Every point is its own cluster"
- 2. Find "most similar" pair of clusters

K-means and Hierarchical Clustering: Slide 41

- Say "Every point is its own cluster"
- Find "most similar" pair of clusters
- 3. Merge it into a parent cluster

K-means and Hierarchical Clustering: Slide 42

- Say "Every point is its own cluster"
- Find "most similar" pair of clusters
- 3. Merge it into a parent cluster
- 4. Repeat

K-means and Hierarchical Clustering: Slide 43

- Say "Every point is its own cluster"
- 2. Find "most similar" pair of clusters
- 3. Merge it into a parent cluster
- 4. Repeat

K-means and Hierarchical Clustering: Slide 44

How to define cluster similarity?

- Average distance between points, maximum distance, minimum distance
- Distance between means or medoids

How many clusters?

- Clustering creates a dendrogram (a tree)
- Threshold based on max number of clusters or based on distance between merges

