

CSE 444: Database Internals

Section 4: Operator Algorithms

Notations

- $B(R)$ = # of blocks (i.e. pages) for relation R
- $T(R)$ = # of tuples in relation R
- $V(R, a)$ = # of distinct values of attribute a
- Memory M

Algorithms for Group By and Aggregate Operators

- Modified Tweet Example:

Tweet(tid, uid, tlen) tlen = tweet length

SELECT uid, MIN(tlen)

FROM Tweet

GROUP BY uid

One pass, hash-based grouping

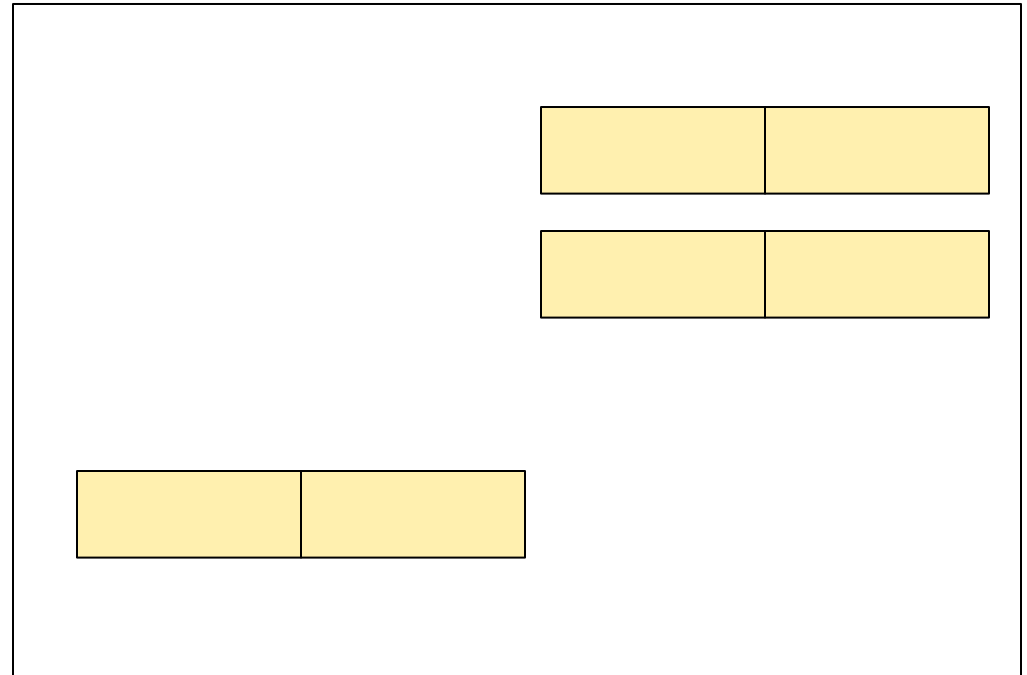
$M = 3$

Showing
tid, uid, tlen

Disk

Tweet

5, 1, 7	4, 2, 10
1, 3, 3	3, 1, 5
7, 3, 8	2, 2, 5
6, 3, 9	8, 1, 10



One pass, hash-based grouping

Main memory data structure
(holds minimum for every
group)

$M = 3$

Showing
tid, uid, tlen

Disk

Tweet

5, 1, 7	4, 2, 10
1, 3, 3	3, 1, 5
7, 3, 8	2, 2, 5
6, 3, 9	8, 1, 10

$H = \text{uid} \% 2$

1, 7

2, 10

5, 1, 7

4, 2, 10

One pass, hash-based grouping

$M = 3$

Showing
tid, uid, tlen

Disk

Tweet

5, 1, 7	4, 2, 10
1, 3, 3	3, 1, 5
7, 3, 8	2, 2, 5
6, 3, 9	8, 1, 10

$H = \text{uid} \% 2$

1, 3, 3	3, 1, 5
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1, 5	3, 3
2, 10	

Minimum
updated
from 7 to 5

Discussion

Cost:

- Clustered?
- Unclustered?

Which operator method does the grouping?

open(), next(), or close()?

What to do for AVG(tlen)?

Discussion

Cost:

- Clustered?
 - $B(R)$: assuming $M - 1$ pages can hold all groups – tuples for groups can be shorter or larger than original tuples
- Unclustered?
 - Also $B(R)$

Which method does the grouping:

`open()`, `next()`, or `close()`?

- Cannot return anything until the entire data is read. `Open()` needs to do grouping

What to do for $AVG(tlen)$?

- Keep both $SUM(tlen)$ and $COUNT(*)$ for each group in memory

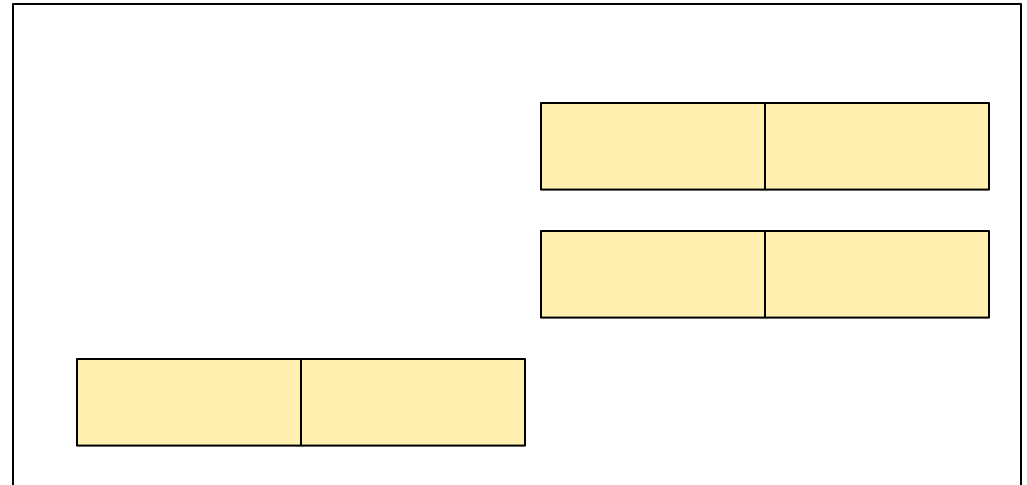
Two pass, hash-based grouping

Showing
tid, uid, tlen

$M = 3$

Tweet

5, 1, 7	4, 2, 10
1, 3, 3	3, 5, 5
7, 3, 1	2, 2, 5
6, 4, 9	8, 4, 10



Two pass, hash-based grouping

Showing
tid, uid, tlen

No aggregation is performed in the first pass

$M = 3$

Tweet

5, 1, 7	4, 2, 10
1, 3, 3	3, 5, 5
7, 3, 1	2, 2, 5
6, 4, 9	8, 4, 10

$H = \text{uid} \% 2$

5, 1, 7

4, 2, 10

5, 1, 7

4, 2, 10

Two pass, hash-based grouping

Showing
tid, uid, tlen

No aggregation is performed in the first pass

$M = 3$

Tweet

5, 1, 7	4, 2, 10
1, 3, 3	3, 5, 5
7, 3, 1	2, 2, 5
6, 4, 9	8, 4, 10

$H = \text{uid} \% 2$

5, 1, 7

1, 3, 3

4, 2, 10

1, 3, 3

3, 5, 5

Flush!

Two pass, hash-based grouping

Showing
tid, uid, tlen

No aggregation is performed in the first pass

$M = 3$

Tweet

5, 1, 7	4, 2, 10
1, 3, 3	3, 5, 5
7, 3, 1	2, 2, 5
6, 4, 9	8, 4, 10

$$H = \text{uid} \% 2$$

3, 5, 5

4, 2, 10

1, 3, 3

3, 5, 5

5, 1, 7

1, 3, 3

Two pass, hash-based grouping

Showing
tid, uid, tlen

No aggregation is performed in the first pass

$M = 3$

Tweet

5, 1, 7	4, 2, 10
1, 3, 3	3, 5, 5
7, 3, 1	2, 2, 5
6, 4, 9	8, 4, 10

$H = \text{uid} \% 2$

3, 5, 5

7, 3, 1

4, 2, 10

2, 2, 5

7, 3, 1

2, 2, 5

5, 1, 7

1, 3, 3

Two pass, hash-based grouping

Showing
tid, uid, tlen

No aggregation is performed in the first pass

$M = 3$

Tweet

5, 1, 7	4, 2, 10
1, 3, 3	3, 5, 5
7, 3, 1	2, 2, 5
6, 4, 9	8, 4, 10

$H = \text{uid} \% 2$

3, 5, 5

7, 3, 1

4, 2, 10

2, 2, 5

6, 4, 9

8, 4, 10

Flush!

5, 1, 7

1, 3, 3

Two pass, hash-based grouping

Showing
tid, uid, tlen

No aggregation is performed in the first pass

$M = 3$

Tweet

5, 1, 7	4, 2, 10
1, 3, 3	3, 5, 5
7, 3, 1	2, 2, 5
6, 4, 9	8, 4, 10

$H = \text{uid} \% 2$

3, 5, 5

7, 3, 1

6, 4, 9

8, 4, 10

6, 4, 9

8, 4, 10

5, 1, 7

1, 3, 3

4, 2, 10

2, 2, 5

Two pass, hash-based grouping

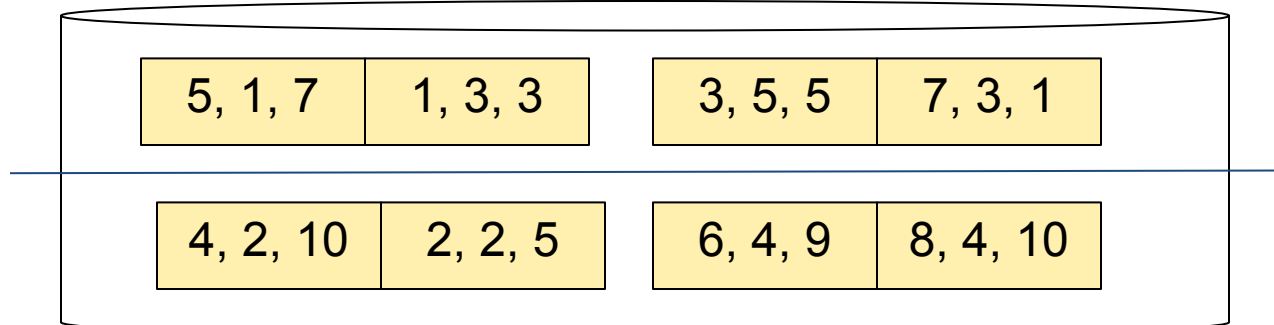
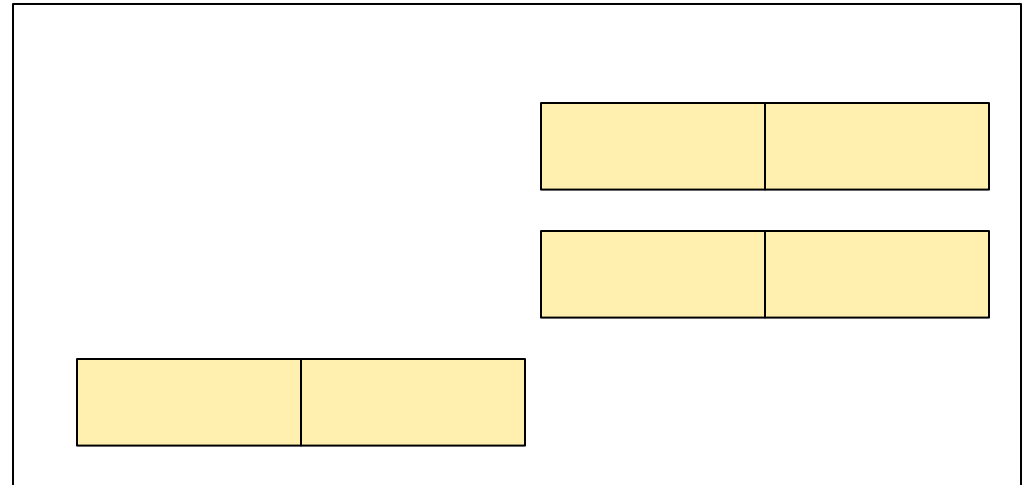
Showing
tid, uid, tlen

Final buffer and disk after pass 1

$M = 3$

Tweet

5, 1, 7	4, 2, 10
1, 3, 3	3, 5, 5
7, 3, 1	2, 2, 5
6, 4, 9	8, 4, 10



Two pass, hash-based grouping

Showing
tid, uid, tlen

Second pass: compute aggregate in each bucket
Need to keep only one record per group

$M = 3$

Tweet

5, 1, 7	4, 2, 10
1, 3, 3	3, 5, 5
7, 3, 1	2, 2, 5
6, 4, 9	8, 4, 10

	1, 7	3, 3
5, 1, 7	1, 3, 3	

5, 1, 7	1, 3, 3	3, 5, 5	7, 3, 1
4, 2, 10	2, 2, 5	6, 4, 9	8, 4, 10

Two pass, hash-based grouping

Showing
tid, uid, tlen

Second pass: compute aggregate in each bucket
Need to keep only one record per group

$M = 3$

Tweet

5, 1, 7	4, 2, 10
1, 3, 3	3, 5, 5
7, 3, 1	2, 2, 5
6, 4, 9	8, 4, 10

Update min

1, 7	3, 3
5, 5	

3, 5, 5	7, 3, 1
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5, 1, 7	1, 3, 3	3, 5, 5	7, 3, 1
4, 2, 10	2, 2, 5	6, 4, 9	8, 4, 10

Discussion

Cost?

- $3B(R)$

Assumptions?

- Need to hold all distinct values in the same bucket in $M-1$
- Assuming uniformity, $B(R) \leq M^2$ is safe to assume
 - i.e. $B(R)/M \leq M$

Two pass, sort-merge-based grouping

$M = 3$

Showing
tid, uid, tlen

Tweet

5, 1, 7	4, 2, 10
1, 3, 3	3, 5, 5
7, 3, 1	2, 2, 5
6, 4, 9	8, 4, 10

Two pass, sort-merge-based grouping

Showing
tid, uid, tlen

Step 1: Divide R into partitions of size M
sort each partition in memory
(on group by attr = uid)
Write to disk

$M = 3$

Tweet

5, 1, 7	4, 2, 10
1, 3, 3	3, 5, 5
7, 3, 1	2, 2, 5
6, 4, 9	8, 4, 10

5, 1, 7	4, 2, 10
2, 2, 5	1, 3, 3
7, 3, 1	3, 5, 5

5, 1, 7	4, 2, 10	2, 2, 5	1, 3, 3	7, 3, 1	3, 5, 5
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Two pass, sort-merge-based grouping

Showing
tid, uid, tlen

Step 1: Divide R into M partitions
sort each partition in memory
(on group by attr = uid)
Write to disk

$M = 3$

Tweet

5, 1, 7	4, 2, 10
1, 3, 3	3, 5, 5
7, 3, 1	2, 2, 5
6, 4, 9	8, 4, 10

6, 4, 9	8, 4, 10

5, 1, 7	4, 2, 10	2, 2, 5	1, 3, 3	7, 3, 1	3, 5, 5
6, 4, 9	8, 4, 10				

Two pass, sort-merge-based grouping

Showing
tid, uid, tlen

Step 2:

- Load first blocks from all runs
- Find minimum of each key by “Combine” approach in merge-sort
- Repeatedly find the least value of the sort key: next group

M = 3

Two

5, 1, 7	4, 2, 10
1, 3, 3	3, 5, 5
7, 3, 1	2, 2, 5
6, 4, 9	8, 4, 10

5, 1, 7	4, 2, 10
6, 4, 9	8, 4, 10

(uid, min(tlen))
(1, 7)

Not showing the outputs in output buffer

5, 1, 7	4, 2, 10	2, 2, 5	1, 3, 3	7, 3, 1	3, 5, 5
6, 4, 9	8, 4, 10				

Two pass, sort-merge-based grouping

Showing
tid, uid, tlen

Step 3: Find minimum of each key by “Combine”
approach in merge-sort

$M = 3$

Repeatedly find the least value of the sort key:
next group

Tweet

5, 1, 7	4, 2, 10
1, 3, 3	3, 5, 5
7, 3, 1	2, 2, 5
6, 4, 9	8, 4, 10

5, 1, 7	4, 2, 10
6, 4, 9	8, 4, 10

(uid, min(tlen))
(1, 7)
(2, 10)

Not showing the outputs in output buffer

5, 1, 7	4, 2, 10	2, 2, 5	1, 3, 3	7, 3, 1	3, 5, 5
6, 4, 9	8, 4, 10				

Two pass, sort-merge-based grouping

Showing
tid, uid, tlen

Step 2: Find minimum of each key by “Combine”
approach in merge-sort

$M = 3$

Repeatedly find the least value of the sort key:
next group

Tweet

5, 1, 7	4, 2, 10
1, 3, 3	3, 5, 5
7, 3, 1	2, 2, 5
6, 4, 9	8, 4, 10

5, 1, 7	4, 2, 10
6, 4, 9	8, 4, 10

(uid, min(tlen))
(1, 7)
(2, 10)

Not showing the outputs in output buffer

5, 1, 7	4, 2, 10	2, 2, 5	1, 3, 3	7, 3, 1	3, 5, 5
6, 4, 9	8, 4, 10				

Two pass, sort-merge-based grouping

Showing
tid, uid, tlen

Step 2: Find minimum of each key by “Combine”
approach in merge-sort

$M = 3$

Repeatedly find the least value of the sort key:
next group

Tweet

5, 1, 7	4, 2, 10
1, 3, 3	3, 5, 5
7, 3, 1	2, 2, 5
6, 4, 9	8, 4, 10

2, 2, 5	1, 3, 3
6, 4, 9	8, 4, 10

(uid, min(tlen))
(1, 7)
(2, 10)

Not showing the outputs in output buffer

5, 1, 7	4, 2, 10	2, 2, 5	1, 3, 3	7, 3, 1	3, 5, 5
6, 4, 9	8, 4, 10				

Two pass, sort-merge-based grouping

Showing
tid, uid, tlen

Step 2: Find minimum of each key by “Combine”
approach in merge-sort

$M = 3$

Repeatedly find the least value of the sort key:
next group

Tweet

5, 1, 7	4, 2, 10
1, 3, 3	3, 5, 5
7, 3, 1	2, 2, 5
6, 4, 9	8, 4, 10

2, 2, 5	1, 3, 3
6, 4, 9	8, 4, 10

(uid, min(tlen))
(1, 7)
(2, 5)
(3, 3)

Not showing the outputs in output buffer

5, 1, 7	4, 2, 10	2, 2, 5	1, 3, 3	7, 3, 1	3, 5, 5
6, 4, 9	8, 4, 10				

Two pass, sort-merge-based grouping

Showing
tid, uid, tlen

Step 2: Find minimum of each key by “Combine”
approach in merge-sort

$M = 3$

Repeatedly find the least value of the sort key:
next group

Tweet

5, 1, 7	4, 2, 10
1, 3, 3	3, 5, 5
7, 3, 1	2, 2, 5
6, 4, 9	8, 4, 10

7, 3, 1	3, 5, 5
6, 4, 9	8, 4, 10

(uid, min(tlen))
(1, 7)
(2, 5)
(3, 3)

Not showing the outputs in output buffer

5, 1, 7	4, 2, 10	2, 2, 5	1, 3, 3	7, 3, 1	3, 5, 5
6, 4, 9	8, 4, 10				

Two pass, sort-merge-based grouping

Showing
tid, uid, tlen

Step 2: Find minimum of each key by “Combine”
approach in merge-sort

$M = 3$

Repeatedly find the least value of the sort key:
next group

Tweet

5, 1, 7	4, 2, 10
1, 3, 3	3, 5, 5
7, 3, 1	2, 2, 5
6, 4, 9	8, 4, 10

7, 3, 1	3, 5, 5
6, 4, 9	8, 4, 10

(uid, min(tlen))
(1, 7)
(2, 5)
(3, 1)
(4, 9)
(5, 5)

Not showing the outputs in output buffer

5, 1, 7	4, 2, 10	2, 2, 5	1, 3, 3	7, 3, 1	3, 5, 5
6, 4, 9	8, 4, 10				

Discussion

Cost?

- $3B(R)$

Assumptions?

- Need to hold one block from each run in M pages
- $B(R) \leq M^2$

One pass vs. Two pass

- One pass:
 - smaller disk I/O cost
 - e.g. $B(R)$ for one-pass hash-based aggregation
 - Handles smaller relations
 - e.g. $B(R) \leq M$
- Two/Multi pass:
 - Larger disk I/O cost
 - e.g. $3B(R)$ for two-pass hash-based aggregation
 - Can handle larger relations
 - e.g. $B(R) \leq M^2$

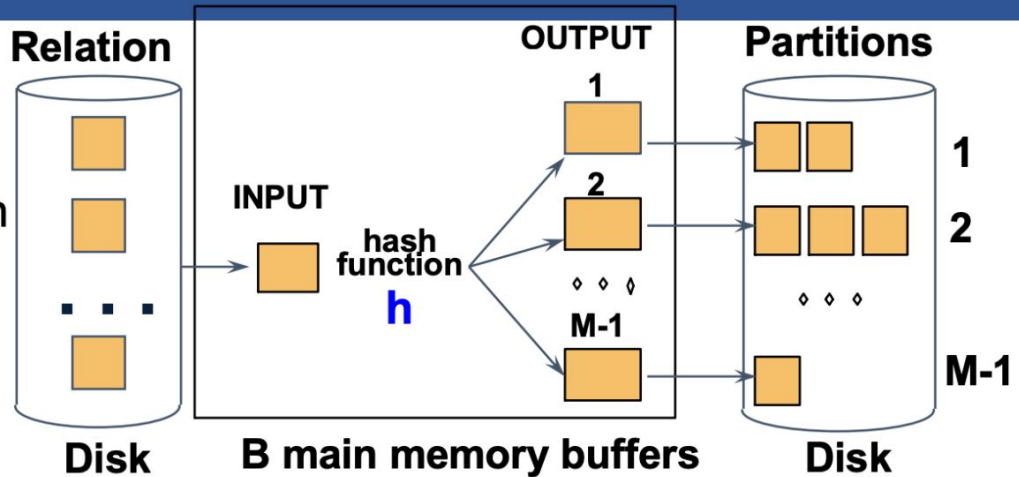
Review for Joins

- Two-pass Hash-based Join
 - Cost: $3B(R) + 3B(S)$
 - Assumption: $\min(B(R), B(S)) \leq M^2$
- Two-pass Sort-merge-based Join
 - Implementation:
 - Cost: $3B(R) + 3B(S)$
 - For R, S: sort runs/sublists (2 I/O, read + write)
 - Join by combining all runs of R and S (only read, write not counted - 1 I/O)

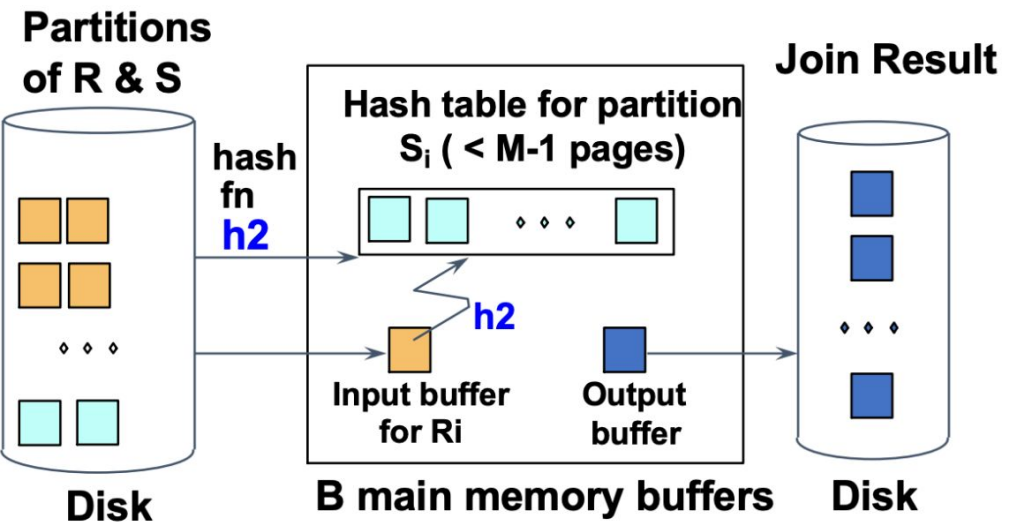
Partitioned Hash-Join

- Partition both relations using hash fn **h**: R tuples in partition *i* will only match S tuples in partition *i*.

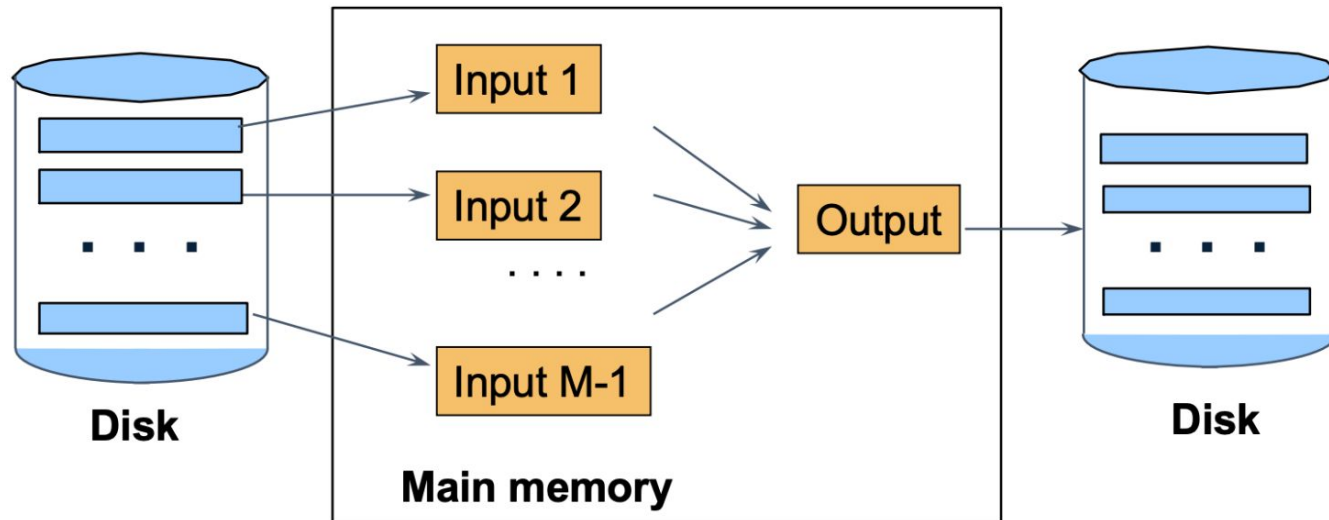
Original Relation



- Read in a partition of R, hash it using **h2** ($\neq h!$). Scan matching partition of S, search for matches.



Merge-Join



$M_1 = B(R)/M$ runs for R

$M_2 = B(S)/M$ runs for S

Merge-join $M_1 + M_2$ runs;

need $M_1 + M_2 \leq M$ to process all runs

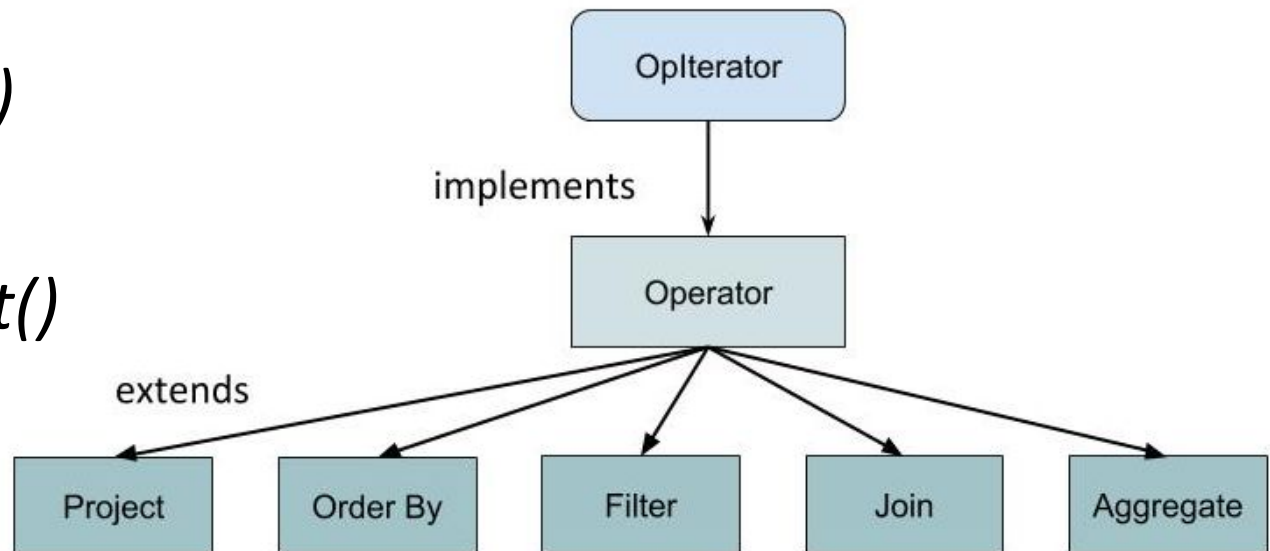
i.e. $B(R) + B(S) \leq M^2$

Homework 2

- Problem 1
 - B+ Trees (inserting/deleting/lookups)
- Problem 2
 - Operator Algorithms
- Problem 3
 - Multi-Pass Algorithms

Lab 2: Operator

- TODO: Implement Operator *Filter*, *Join* and *Aggregate*
 - *open()*
 - *close()*
 - *hasNext()*
 - *next()*
 - *fetchNext()*



Lab2: Aggregator

- TODO: Implement *IntegerAggregator* and *StringAggregator*
 - `mergeTupleIntoGroup()`: merge a tuple into aggregate
 - `iterator()`: return *a Oplterator over group aggregate results*

