

Database System Internals Transactions: Recovery (part 1)

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Announcements

- Quiz on lab 1 and 2 next Thursday on Gradescope
 - Relatively short, should only take 30 min or so

Main textbook (Garcia-Molina)

■ Ch. 17.2-4, 18.1-3, 18.8-9

Second textbook (Ramakrishnan)

■ Ch. 16-18

Also: M. J. Franklin. Concurrency Control and Recovery. The Handbook of Computer Science and Engineering, A. Tucker, ed., CRC Press, Boca Raton, 1997.

Transaction Management

Two parts:

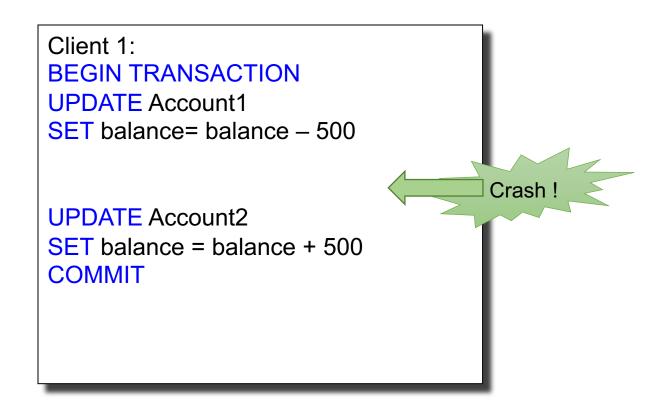
- Concurrency control: ACID
- Recovery from crashes: <u>ACID</u>

We already discussed concurrency control You are implementing locking in lab3

Today, we start recovery

Type of Crash	Prevention		
Wrong data entry	Constraints and Data cleaning		
Disk crashes	Redundancy: e.g. RAID, archive		
Data center failures	Remote backups or replicas		
System failures: e.g. power	DATABASE RECOVERY		

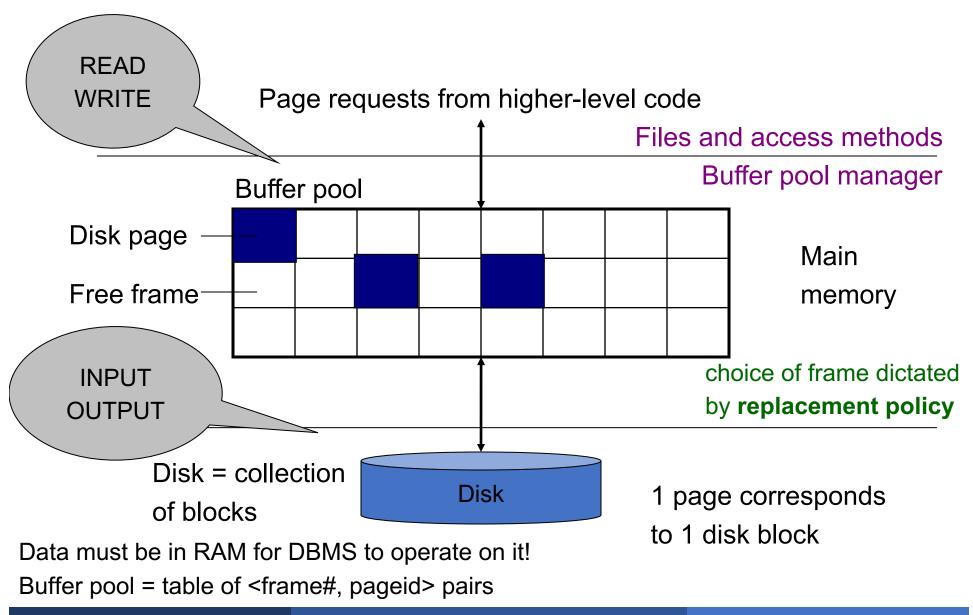
System Crash



System Failures

- Each transaction has internal state
- When system crashes, internal state is lost
 - Don't know which parts executed and which didn't
 - Need ability to undo and redo

Buffer Manager Review



Buffer Manager Review

- Enables higher layers of the DBMS to assume that needed data is in main memory
- Caches data in memory. Problems when crash occurs:
 - 1. If committed data was not yet written to disk
 - 2. If uncommitted data was flushed to disk

Transactions

Assumption: the database is composed of <u>elements</u>.

- 1 element can be either:
 - 1 page = physical logging
 - 1 record = logical logging
- In Lab 4 we use page-level elements

Primitive Operations of Transactions

- READ(X,t)
 - copy element X to transaction local variable t
- WRITE(X,t)
 - copy transaction local variable t to element X
- INPUT(X)
 - read element X to memory buffer
- OUTPUT(X)
 - write element X to disk

Running Example

BEGIN TRANSACTION

```
READ(A,t);

t := t*2;

WRITE(A,t);

READ(B,t);

t := t*2;

WRITE(B,t)

COMMIT;
```

Initially, A=B=8.

Atomicity requires that either

- (1) T commits and A=B=16, or
- (2) T does not commit and A=B=8.

Running Example

BEGIN TRANSACTION

```
READ(A,t);
```

```
t := t*2;
```

WRITE(A,t);

READ(B,t);

```
t ·= **
```

Will look at various crash scenarios

WF

CO

What behavior do we want in each case?

Initially, A=B=8.

Atomicity requires that either

- (1) T commits and A=B=16, or
- (2) T does not commit and A=B=8.

READ(A,t); t := t*2; WRITE(A,t); READ(B,t); t := t*2; WRITE(B,t)

Transaction

Buffer pool

Disk

Action	t	Mem A	Mem B	Disk A	Disk B
INPUT(A)		8		8	8
READ(A,t)					
t:=t*2					
WRITE(A,t)					
INPUT(B)					
READ(B,t)					
t:=t*2					
WRITE(B,t)					
OUTPUT(A)					
OUTPUT(B)					
COMMIT					

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READ(A,t); t := t*2; WRITE(A,t); READ(B,t); t := t*2; WRITE(B,t)

Transaction

Buffer pool

Disk

Action	t	Mem A	Mem B	Disk A	Disk B
INPUT(A)		8		8	8
READ(A,t)	8	8		8	8
t:=t*2					
WRITE(A,t)					
INPUT(B)					
READ(B,t)					
t:=t*2					
WRITE(B,t)					
OUTPUT(A)					
OUTPUT(B)					
COMMIT					

READ(A,t); t := t*2; WRITE(A,t); READ(B,t); t := t*2; WRITE(B,t)

Transaction

Buffer pool

Disk

Action	t	Mem A	Mem B	Disk A	Disk B
INPUT(A)		8		8	8
READ(A,t)	8	8		8	8
t:=t*2	16	8		8	8
WRITE(A,t)					
INPUT(B)					
READ(B,t)					
t:=t*2					
WRITE(B,t)					
OUTPUT(A)					
OUTPUT(B)					
COMMIT					

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READ(A,t); t := t*2; WRITE(A,t); READ(B,t); t := t*2; WRITE(B,t)

Transaction

Buffer pool

Disk

Action	t	Mem A	Mem B	Disk A	Disk B
INPUT(A)		8		8	8
READ(A,t)	8	8		8	8
t:=t*2	16	8		8	8
WRITE(A,t)	16	16		8	8
INPUT(B)					
READ(B,t)					
t:=t*2					
WRITE(B,t)					
OUTPUT(A)					
OUTPUT(B)					
COMMIT					

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READ(A,t); t := t*2; WRITE(A,t); READ(B,t); t := t*2; WRITE(B,t)

Transaction

Buffer pool

Disk

Action	t	Mem A	Mem B	Disk A	Disk B
INPUT(A)		8		8	8
READ(A,t)	8	8		8	8
t:=t*2	16	8		8	8
WRITE(A,t)	16	16		8	8
INPUT(B)	16	16	8	8	8
READ(B,t)					
t:=t*2					
WRITE(B,t)					
OUTPUT(A)					
OUTPUT(B)					
COMMIT					

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READ(A,t); t := t*2; WRITE(A,t); READ(B,t); t := t*2; WRITE(B,t)

Transaction

Buffer pool

Disk

Action	t	Mem A	Mem B	Disk A	Disk B
INPUT(A)		8		8	8
READ(A,t)	8	8		8	8
t:=t*2	16	8		8	8
WRITE(A,t)	16	16		8	8
INPUT(B)	16	16	8	8	8
READ(B,t)	8	16	8	8	8
t:=t*2					
WRITE(B,t)					
OUTPUT(A)					
OUTPUT(B)					
COMMIT					

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READ(A,t); t := t*2; WRITE(A,t); READ(B,t); t := t*2; WRITE(B,t)

Transaction

Buffer pool

Disk

Action	t	Mem A	Mem B	Disk A	Disk B
INPUT(A)		8		8	8
READ(A,t)	8	8		8	8
t:=t*2	16	8		8	8
WRITE(A,t)	16	16		8	8
INPUT(B)	16	16	8	8	8
READ(B,t)	8	16	8	8	8
t:=t*2	16	16	8	8	8
WRITE(B,t)					
OUTPUT(A)					
OUTPUT(B)					
COMMIT					

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READ(A,t); t := t*2; WRITE(A,t); READ(B,t); t := t*2; WRITE(B,t)

Transaction

Buffer pool

Disk

Action	t	Mem A	Mem B	Disk A	Disk B
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READ(A,t)	8	8		8	8
t:=t*2	16	8		8	8
WRITE(A,t)	16	16		8	8
INPUT(B)	16	16	8	8	8
READ(B,t)	8	16	8	8	8
t:=t*2	16	16	8	8	8
WRITE(B,t)	16	16	16	8	8
OUTPUT(A)					
OUTPUT(B)					
COMMIT					

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READ(A,t); t := t*2; WRITE(A,t); READ(B,t); t := t*2; WRITE(B,t)

Transaction

Buffer pool

Disk

Action	t	Mem A	Mem B	Disk A	Disk B
INPUT(A)		8		8	8
READ(A,t)	8	8		8	8
t:=t*2	16	8		8	8
WRITE(A,t)	16	16		8	8
INPUT(B)	16	16	8	8	8
READ(B,t)	8	16	8	8	8
t:=t*2	16	16	8	8	8
WRITE(B,t)	16	16	16	8	8
OUTPUT(A)	16	16	16	16	8
OUTPUT(B)					
COMMIT					

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READ(A,t); t := t*2; WRITE(A,t); READ(B,t); t := t*2; WRITE(B,t)

Transaction

Buffer pool

Disk

Action	t	Mem A	Mem B	Disk A	Disk B
INPUT(A)		8		8	8
READ(A,t)	8	8		8	8
t:=t*2	16	8		8	8
WRITE(A,t)	16	16		8	8
INPUT(B)	16	16	8	8	8
READ(B,t)	8	16	8	8	8
t:=t*2	16	16	8	8	8
WRITE(B,t)	16	16	16	8	8
OUTPUT(A)	16	16	16	16	8
OUTPUT(B)	16	16	16	16	16
COMMIT					

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Action	t	Mem A	Mem B	Disk A	Disk B
INPUT(A)		8		8	8
READ(A,t)	8	8		8	8
t:=t*2	16	8		8	8
WRITE(A,t)	16	16		8	8
INPUT(B)	16	16	8	8	8
READ(B,t)	8	16	8	8	8
t:=t*2	16	16	8	8	8
WRITE(B,t)	16	16	16	8	8
OUTPUT(A)	16	16	16	16	8
OUTPUT(B)	16	16	16	16	16
COMMIT			Spring 2021		

Yes it's bad: A=16, B=8....

Action	t	Mem A	Mem B	Disk A	Disk B
INPUT(A)		8		8	8
READ(A,t)	8	8		8	8
t:=t*2	16	8		8	8
WRITE(A,t)	16	16		8	8
INPUT(B)	16	16	8	8	8
READ(B,t)	8	16	8	8	8
t:=t*2	16	16	8	8	8
WRITE(B,t)	16	16	16	8	8
OUTPUT(A)	16	16	16	16	8
OUTPUT(B)	16	16	16	16	16
COMMIT					

Action	t	Mem A	Mem B	Disk A	Disk B
INPUT(A)		8		8	8
READ(A,t)	8	8		8	8
t:=t*2	16	8		8	8
WRITE(A,t)	16	16		8	8
INPUT(B)	16	16	8	8	8
READ(B,t)	8	16	8	8	8
t:=t*2	16	16	8	8	8
WRITE(B,t)	16	16	16	8	8
OUTPUT(A)	16	16	16	16	8
OUTPUT(B)	16	16	16	16	16
COMMIT					

Yes it's bad: A=B=16, but not committed

Action	t	Mem A	Mem B	Disk A	Disk B
INPUT(A)		8		8	8
READ(A,t)	8	8		8	8
t:=t*2	16	8		8	8
WRITE(A,t)	16	16		8	8
INPUT(B)	16	16	8	8	8
READ(B,t)	8	16	8	8	8
t:=t*2	16	16	8	8	8
WRITE(B,t)	16	16	16	8	8
OUTPUT(A)	16	16	16	16	8
OUTPUT(B)	16	16	16	16	16
COMMIT					

Action	t	Mem A	Mem B	Disk A	Disk B
INPUT(A)		8		8	8
READ(A,t)	8	8		8	8
t:=t*2	16	8		8	8
WRITE(A,t)	16	16		8	8
INPUT(B)	16	16	8	8	8
READ(B,t)	8	16	8	8	8
t:=t*2	16	16	8	8	8
WRITE(B,t)	16	16	16	8	8
OUTPUT(A)	16	16	16	16	8
OUTPUT(B)	16	16	16	16	16
COMMIT			Spring 2021		

Action	t	Mem A	Mem B	Disk A	Disk B	
INPUT(A)		8		8	8	
READ(A,t)	8	8		8	8	
t:=t*2	16	8		8	8	
WRITE(A,t)	16	16		8	8	
INPUT(B)	16	16	8	8	8	
READ(B,t)	8	16	8	8	8	
t:=t*2	16	16	8	8	8	
WRITE(B,t)	16	16	16	8	8	Crash !
OUTPUT(A)	16	16	16	16	8	
OUTPUT(B)	16	16	16	16	16	
COMMIT			Spring 2021			

No: that's OK

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OUTPUT can also happen after COMMIT (details coming)

Action	t	Mem A	Mem B	Disk A	Disk B
INPUT(A)		8		8	8
READ(A,t)	8	8		8	8
t:=t*2	16	8		8	8
WRITE(A,t)	16	16		8	8
INPUT(B)	16	16	8	8	8
READ(B,t)	8	16	8	8	8
t:=t*2	16	16	8	8	8
WRITE(B,t)	16	16	16	8	8
COMMIT					
OUTPUT(A)	16	16	16	16	8
OUTPUT(B)	16	16	16	16	16

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OUTPUT can also happen after COMMIT (details coming)

Action	t	Mem A	Mem B	Disk A	Disk B
INPUT(A)		8		8	8
READ(A,t)	8	8		8	8
t:=t*2	16	8		8	8
WRITE(A,t)	16	16		8	8
INPUT(B)	16	16	8	8	8
READ(B,t)	8	16	8	8	8
t:=t*2	16	16	8	8	8
WRITE(B,t)	16	16	16	8	8
COMMIT					
OUTPUT(A)	16	16	16	16	8 \geq
OUTPUT(B)	16	16	16	16	16

Atomic Transactions

FORCE or NO-FORCE

 Should all updates of a transaction be forced to disk before the transaction commits?

STEAL or NO-STEAL

 Can an update made by an uncommitted transaction overwrite the most recent committed value of a data item on disk?

Force/No-steal (most strict)

 FORCE: Pages of committed transactions must be forced to disk before commit

 NO-STEAL: Pages of uncommitted transactions cannot be written to disk

Easy to implement (how?) and ensures atomicity

No-Force/Steal (least strict)

 NO-FORCE: Pages of committed transactions need not be written to disk

STEAL: Pages of uncommitted transactions may be written to disk

In both cases, need a Write Ahead Log (WAL) to provide atomicity in face of failures

Write-Ahead Log (WAL)

The Log: append-only file containing log records

- Records every single action of every TXN
- Forces log entries to disk as needed
- After a system crash, use log to recover

Three types: UNDO, REDO, UNDO-REDO

Aries: is an UNDO-REDO log

Policies and Logs

	NO-STEAL	STEAL
FORCE	Lab 3	Undo Log
NO-FORCE	Redo Log	Undo-Redo Log

"UNDO" Log

FORCE and **STEAL**

Undo Logging

Log records

- START T>
 - transaction T has begun
- <COMMIT T>
 - T has committed
- <ABORT T>
 - T has aborted
- <T,X,∨>
 - T has updated element X, and its <u>old</u> value was v
 - Idempotent, physical log records

Action	t	Mem A	Mem B	Disk A	Disk B	UNDO Log
						<start t=""></start>
INPUT(A)		8		8	8	
READ(A,t)	8	8		8	8	
t:=t*2	16	8		8	8	
WRITE(A,t)	16	16		8	8	<t,a,<mark>8></t,a,<mark>
INPUT(B)	16	16	8	8	8	
READ(B,t)	8	16	8	8	8	
t:=t*2	16	16	8	8	8	
WRITE(B,t)	16	16	16	8	8	<t,b,8></t,b,8>
OUTPUT(A)	16	16	16	16	8	
OUTPUT(B)	16	16	16	16	16	
COMMIT						<commit t=""></commit>

Action	t	Mem A	Mem B	Disk A	Disk B	UNDO Log
						<start t=""></start>
INPUT(A)		8		8	8	
READ(A,t)	8	8		8	8	
t:=t*2	16	8		8	8	
WRITE(A,t)	16	16		8	8	<t,a,8></t,a,8>
INPUT(B)	16	16	8	8	8	
READ(B,t)	8	16	8	8	8	
t:=t*2	16	16	8	8	8	
WRITE(B,t)	16	16	16	8	8	<t,b,8></t,b,
OUTPUT(A)	16	16	16	16	8	Crach
OUTPUT(B)	16	16	16	16	16	Crash!
COMMIT						<commit t=""></commit>

WHAT DO WE DO?

Action	t	Mem A	Mem B	Disk A	Disk B	UNDO Log
						<start t=""></start>
INPUT(A)		8		8	8	
READ(A,t)	8	8		8	8	
t:=t*2	16	8		8	8	
WRITE(A,t)	16	16		8	8	<t,a,8></t,a,8>
INPUT(B)	16	16	8	8	8	
READ(B,t)	8	16	8	8	8	
t:=t*2	16	16	8	8	8	
WRITE(B,t)	16	16	16	8	8	<t,b,8></t,b,8>
OUTPUT(A)	16	16	16	16	8	
OUTPUT(B)	16	16	16	16	16	Crash!
COMMIT						<commit t=""></commit>

WHAT DO WE DO?

We UNDO by setting B=8 and A=8

Action	t	Mem A	Mem B	Disk A	Disk B	UNDO Log
						<start t=""></start>
INPUT(A)		8		8	8	
READ(A,t)	8	8		8	8	
t:=t*2	16	8		8	8	
WRITE(A,t)	16	16		8	8	<t,a,8></t,a,8>
INPUT(B)	16	16	8	8	8	
READ(B,t)	8	16	8	8	8	
t:=t*2	16	16	8	8	8	
WRITE(B,t)	16	16	16	8	8	<t,b,8></t,b,8>
OUTPUT(A)	16	16	16	16	8	
OUTPUT(B)	16	16	16	16	16	
COMMIT						<commit t=""></commit>

What do we do now?

Action	t	Mem A	Mem B	Disk A	Disk B	UNDO Log
						<start t=""></start>
INPUT(A)		8		8	8	
READ(A,t)	8	8		8	8	
t:=t*2	16	8		8	8	
WRITE(A,t)	16	16		8	8	<t,a,8></t,a,8>
INPUT(B)	16	16	8	8	8	
READ(B,t)	8	16	8	8	8	
t:=t*2	16	16	8	8	8	
WRITE(B,t)	16	16	16	8	8	<t,b,8></t,b,8>
OUTPUT(A)	16	16	16	16	8	
OUTPUT(B)	16	16	16	16	16	
COMMIT						<commit t=""></commit>

What do we do now?

Nothing: log contains COMMIT CSE 444 - Spring 2021

• This is all we see (for example):

Disk A	Disk B
8	16

• This is all we see (for example):

Disk A	Disk B
8	16

```
<START T>
<T,A,8>
<T,B,8>
```

- This is all we see (for example):
- Need to step through the log

Disk A	Disk B
8	16

```
<START T>
<T,A,8>
<T,B,8>
```

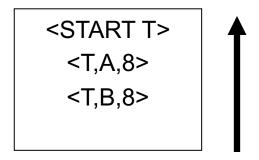
- This is all we see (for example):
- Need to step through the log

Disk A	Disk B
8	16

What direction?

- This is all we see (for example):
- Need to step through the log

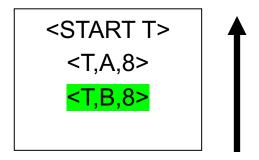
Disk A	Disk B
8	16



- What direction?
- In UNDO log, we start at the most recent and go backwards in time

- This is all we see (for example):
- Need to step through the log

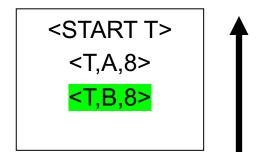
Disk A	Disk B
8	16



- What direction?
- In UNDO log, we start at the most recent and go backwards in time

- This is all we see (for example):
- Need to step through the log

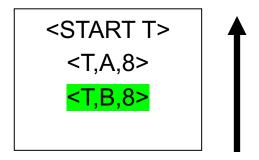
Disk A	Disk B
8	<mark>16</mark>



- What direction?
- In UNDO log, we start at the most recent and go backwards in time

- This is all we see (for example):
- Need to step through the log

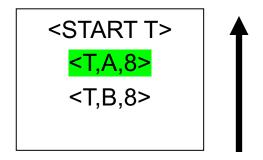
Disk A	Disk B
8	8



- What direction?
- In UNDO log, we start at the most recent and go backwards in time

- This is all we see (for example):
- Need to step through the log

Disk A	Disk B
<mark>8</mark>	8



- What direction?
- In UNDO log, we start at the most recent and go backwards in time

- If we see NO Commit statement:
 - We UNDO both changes: A=8, B=8
 - The transaction is atomic, since none of its actions have been executed
- In we see that T has a Commit statement
 - We don't undo anything
 - The transaction is atomic, since both it's actions have been executed

After system's crash, run recovery manager

 Decide for each transaction T whether it is completed or not

```
• <START T>....<COMMIT T>.... = yes
```

Undo all modifications by incomplete transactions

Recovery manager:

Read log from the end; cases:

<COMMIT T>: mark T as completed

<ABORT T>: mark T as completed

<T,X,v>: if T is not completed then write X=v to disk

else ignore

<START T>: ignore

```
... <T6,X6,v6> ... <START T5> <START T4> <T1,X1,v1> <T5,X5,v5> <T4,X4,v4> <COMMIT T5> <T3,X3,v3> <T2,X2,v2>
```

Question1: Which updates are undone?

Question 2:

How far back do we need to read in the log?

Question 3:

What happens if second crash during recovery?

```
... <T6,X6,v6> ... <START T5> <START T4> <T1,X1,v1> <T5,X5,v5> <T4,X4,v4> <COMMIT T5> <T3,X3,v3> <T2,X2,v2>
```

Question1: Which updates are undone?

Question 2:

How far back do we need to read in the log?
To the beginning.

Question 3:

What happens if second crash during recovery?

```
... <T6,X6,v6> ... <START T5> <START T4> <T1,X1,v1> <T5,X5,v5> <T4,X4,v4> <COMMIT T5> <T3,X3,v3> <T2,X2,v2>
```

Question1: Which updates are undone?

Question 2:

How far back do we need to read in the log?
To the beginning.

Question 3:

What happens if second crash during recovery?

No problem! Log records are idempotent. Can reapply.

Action	t	Mem A	Mem B	Disk A	Disk B	UNDO Log
						<start t=""></start>
INPUT(A)			Vhen mu		8	
READ(A,t)	8		ve force	pages	8	
t:=t*2	16	8	o disk?	8		
WRITE(A,t)	16	16		8	8	<t,a,8></t,a,8>
INPUT(B)	16	16	8	8	8	
READ(B,t)	8	16	8	8	8	
t:=t*2	16	16	8	8	8	
WRITE(B,t)	16	16	16	8	8	<t,b,8></t,b,8>
OUTPUT(A)	1 6	16	16	16	8	
OUTPUT(B)	16	16	16	16	16	
COMMIT						<commit t=""></commit>

Action	t	Mem A	Mem B	Disk A	Disk B	UNDO Log
						<start t=""></start>
INPUT(A)		8		8	8	
READ(A,t)	8	8		8	8	
t:=t*2	16	8		8	8	
WRITE(A,t)	16	16		8	8	<t,a,8></t,a,8>
INPUT(B)	16	16	8	8	8	
READ(B,t)	8	16	8	8	8	
t:=t*2	16	16	8	8	8	
WRITE(B,t)	16	16	16	8	8	<t,b,8></t,b,8>
OUTPUT(A)	16	16	16	16	8	
OUTPUT(B)	16	16	16	16	16	
COMMIT				FOR	CE	◆ <commit t=""></commit>

RULES: log entry <u>before</u> OUTPUT <u>before</u> COMMIT

Undo-Logging Rules

U1: If T modifies X, then <T,X,v> must be written to disk before OUTPUT(X)

U2: If T commits, then OUTPUT(X) must be written to disk before <COMMIT T>

 Hence: OUTPUTs are done <u>early</u>, before the transaction commits

FORCE

Checkpointing

Checkpoint the database periodically

- Stop accepting new transactions
- Wait until all current transactions complete
- Flush log to disk
- Write a <CKPT> log record, flush
- Resume transactions

Undo Recovery with Checkpointing

During recovery, Can stop at first <CKPT>

```
<T9,X9,v9>
(all completed)
<CKPT>
<START T2>
<START T3
<START T5>
<START T4>
<T1,X1,v1>
<T5,X5,v5>
<T4,X4,v4>
<COMMIT T5>
<T3,X3,v3>
<T2,X2,v2>
```

> other transactions

> transactions T2,T3,T4,T5

Nonquiescent Checkpointing

- Problem with checkpointing: database freezes during checkpoint
- Would like to checkpoint while database is operational
- Idea: nonquiescent checkpointing

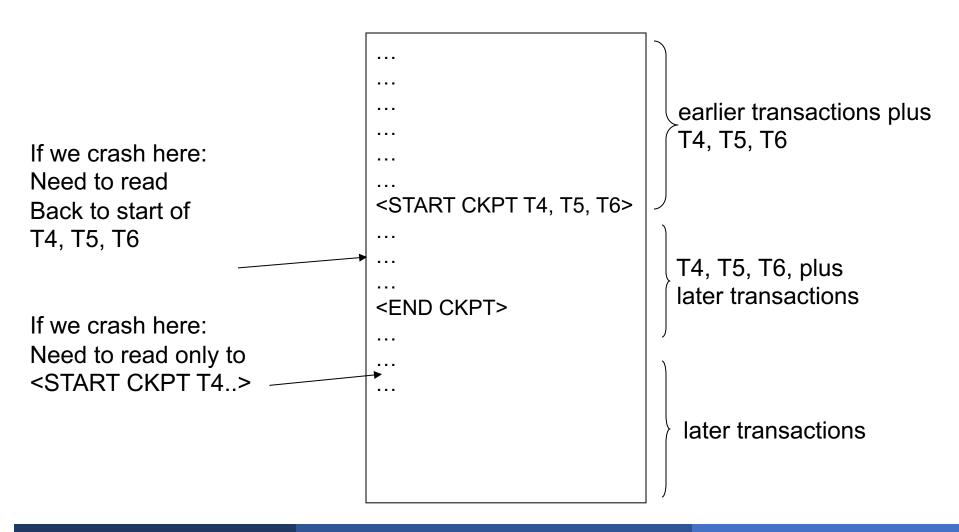
Quiescent = being quiet, still, or at rest; inactive Non-quiescent = allowing transactions to be active

Nonquiescent Checkpointing

Write a <START CKPT(T1,...,Tk)>
 where T1,...,Tk are all active transactions. Flush
log to disk

- Continue normal operation
- When all of T1,...,Tk have completed, write <END CKPT>, flush log to disk

Undo with Nonquiescent Checkpointing



Implementing ROLLBACK

- Recall: a transaction can end in COMMIT or ROLLBACK
- Idea: use the undo-log to implement ROLLBACK
- How ?
 - LSN = Log Sequence Number
 - Log entries for the same transaction are linked, using the LSN's
 - Read log in reverse, using LSN pointers

Implementing ROLLRACK

RecRO

- Ide
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 - •
 - •

•

```
...
<T9,X9,v9>
```

· · ·

(all completed)

<CKPT>

<START T2>

<START T3

<START T5>

<START T4>

<T1,X1,v1>

<T5,X5,v5>

<T2,X1,v2>

<T4,X4,v4>

<COMMIT T5>

<T3,X3,v3>

<T2,X2,v2>

CK

sing



NO-FORCE and NO-STEAL

Action	t	Mem A	Mem B	Disk A	Disk B
READ(A,t)	8	8		8	8
t:=t*2	16	8		8	8
WRITE(A,t)	16	16		8	8
READ(B,t)	8	16	8	8	8
t:=t*2	16	16	8	8	8
WRITE(B,t)	16	16	16	8	8
COMMIT					
OUTPUT(A)	16	16	16	16	8
OUTPUT(B)	16	16	16	16	16

Is this bad?

Action	t	Mem A	Mem B	Disk A	Disk B
READ(A,t)	8	8		8	8
t:=t*2	16	8		8	8
WRITE(A,t)	16	16		8	8
READ(B,t)	8	16	8	8	8
t:=t*2	16	16	8	8	8
WRITE(B,t)	16	16	16	8	8
COMMIT					
OUTPUT(A)	16	16	16	16	8
OUTPUT(B)	16	16	16	16	16

~ /-

Action	t	Mem A	Mem B	Disk A	Disk B	
READ(A,t)	8	8		8	8	
t:=t*2	16	8		8	8	
WRITE(A,t)	16	16		8	8	
READ(B,t)	8	16	8	8	8	
t:=t*2	16	16	8	8	8	
WRITE(B,t)	16	16	16	8	8	
COMMIT						
OUTPUT(A)	16	16	16	16	8	Cra
OUTPUT(B)	16	16	16	16	16	1

Is this bad?

Action	t	Mem A	Mem B	Disk A	Disk B
READ(A,t)	8	8		8	8
t:=t*2	16	8		8	8
WRITE(A,t)	16	16		8	8
READ(B,t)	8	16	8	8	8
t:=t*2	16	16	8	8	8
WRITE(B,t)	16	16	16	8	8
COMMIT					
OUTPUT(A)	16	16	16	16	8
OUTPUT(B)	16	16	16	16	16

Action	t	Mem A	Mem B	Disk A	Disk B
READ(A,t)	8	8		8	8
t:=t*2	16	8		8	8
WRITE(A,t)	16	16		8	8
READ(B,t)	8	16	8	8	8
t:=t*2	16	16	8	8	8
WRITE(B,t)	16	16	16	8	8
COMMIT					
OUTPUT(A)	16	16	16	16	8
OUTPUT(B)	16	16	16	16	16

Is this bad?

Action	t	Mem A	Mem B	Disk A	Disk B
READ(A,t)	8	8		8	8
t:=t*2	16	8		8	8
WRITE(A,t)	16	16		8	8
READ(B,t)	8	16	8	8	8
t:=t*2	16	16	8	8	8
WRITE(B,t)	16	16	16	8	8
COMMIT					
OUTPUT(A)	16	16	16	16	8
OUTPUT(B)	16	16	16	16	16

Action	t	Mem A	Mem B	Disk A	Disk B
READ(A,t)	8	8		8	8
t:=t*2	16	8		8	8
WRITE(A,t)	16	16		8	8
READ(B,t)	8	16	8	8	8
t:=t*2	16	16	8	8	8
WRITE(B,t)	16	16	16	8	8
COMMIT					
OUTPUT(A)	16	16	16	16	8
OUTPUT(B)	16	16	16	16	16