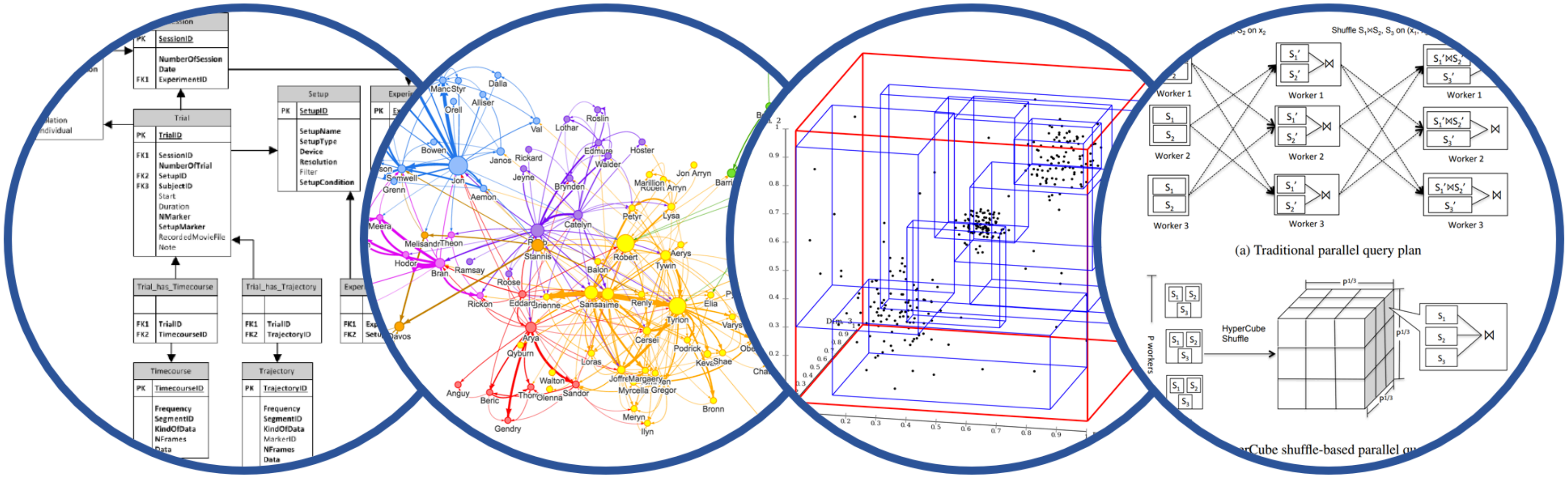

Database System Internals

Operator Algorithms (part 2)

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University of Washington, Seattle

Today's Outline

Query Execution Algorithms:

- Catch-up from last lecture
- Finish operator implementation

Operator Algorithms

Design criteria

- Cost: IO, CPU, Network
- Memory utilization
- Load balance (for parallel operators)

Cost Parameters

- **Cost = total number of I/Os**
  - This is a simplification that ignores CPU, network

- **Parameters:**
  - **B(R)** = # of blocks (i.e., pages) for relation R
  - **T(R)** = # of tuples in relation R
  - **V(R, a)** = # of distinct values of attribute a
    - When **a** is a key, **V(R,a) = T(R)**
    - When **a** is not a key, **V(R,a)** can be anything < **T(R)**

Convention

- Cost = the cost of reading operands from disk, plus cost to read/write intermediate results

- Cost of writing the final result to disk is *not included*; need to count it separately when applicable

Outline

- **Join operator algorithms**
  - One-pass algorithms (Sec. 15.2 and 15.3)
  - Index-based algorithms (Sec 15.6)
  - Two-pass algorithms (Sec 15.4 and 15.5)

- Note about readings:
  - In class, we discuss only algorithms for joins
  - Other operators are easier: book has extra details

Join Algorithms

- Hash join
- Nested loop join
- Sort-merge join

Hash Join

Hash join: $R \bowtie S$

- Scan R, build buckets in main memory
- Then scan S and join
- Cost: B(R) + B(S)

- One-pass algorithm when $B(R) \leq M$

Note: the *inner* relation is the relation on which we build the hash table

- Usually this is the *right* relation of $R \bowtie S$, i.e. S.
- But the following slides choose the *left* relation, i.e. R

Hash Join Example

Patient(pid, name, address)

Insurance(pid, provider, policy_nb)

Patient $\bowtie$ Insurance

Two tuples per page

Patient

1	'Bob'	'Seattle'
2	'Ela'	'Everett'

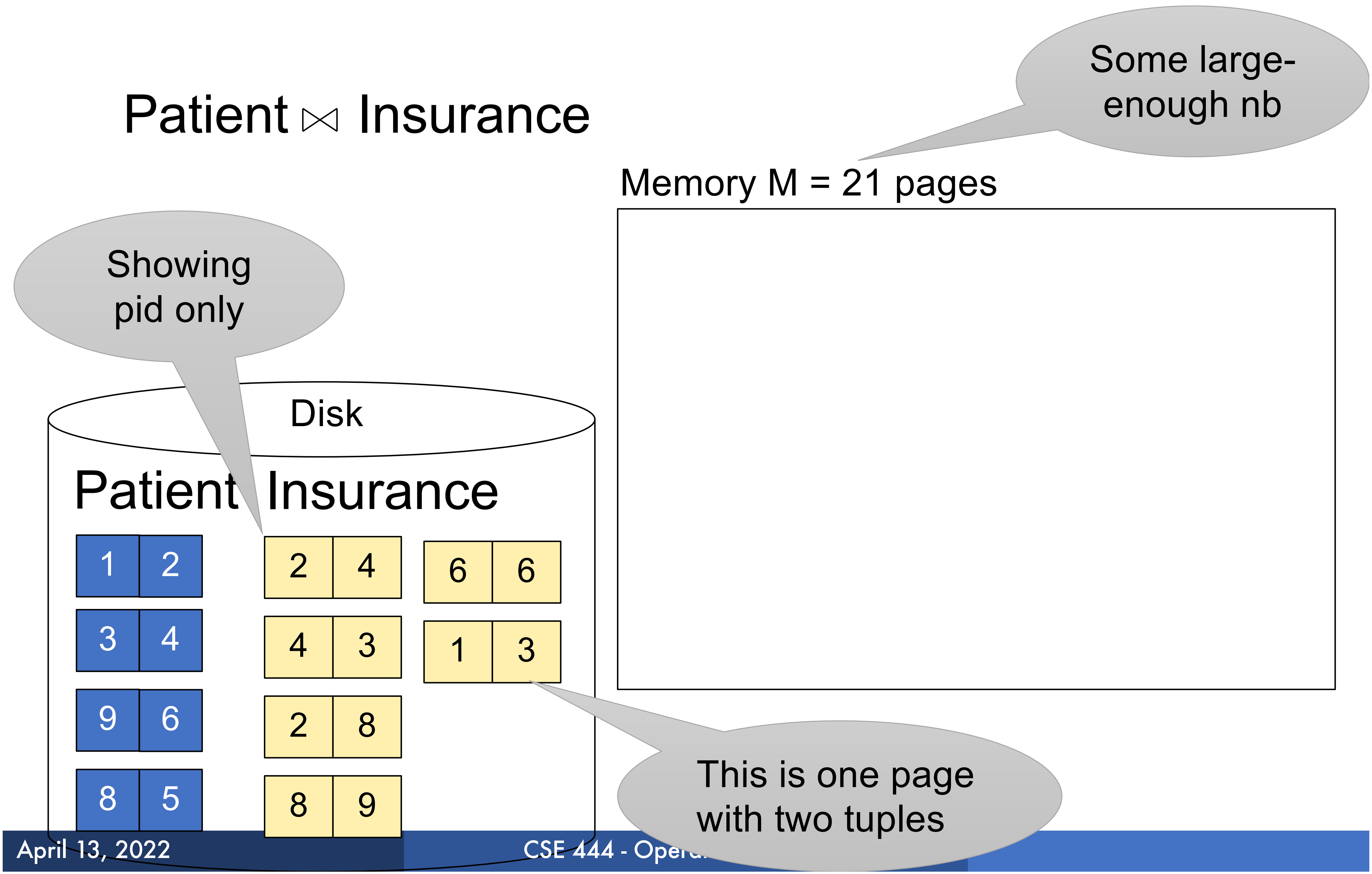
3	'Jill'	'Kent'
4	'Joe'	'Seattle'

Insurance

2	'Blue'	123
4	'Prem'	432

4	'Prem'	343
1	'GrpH'	554

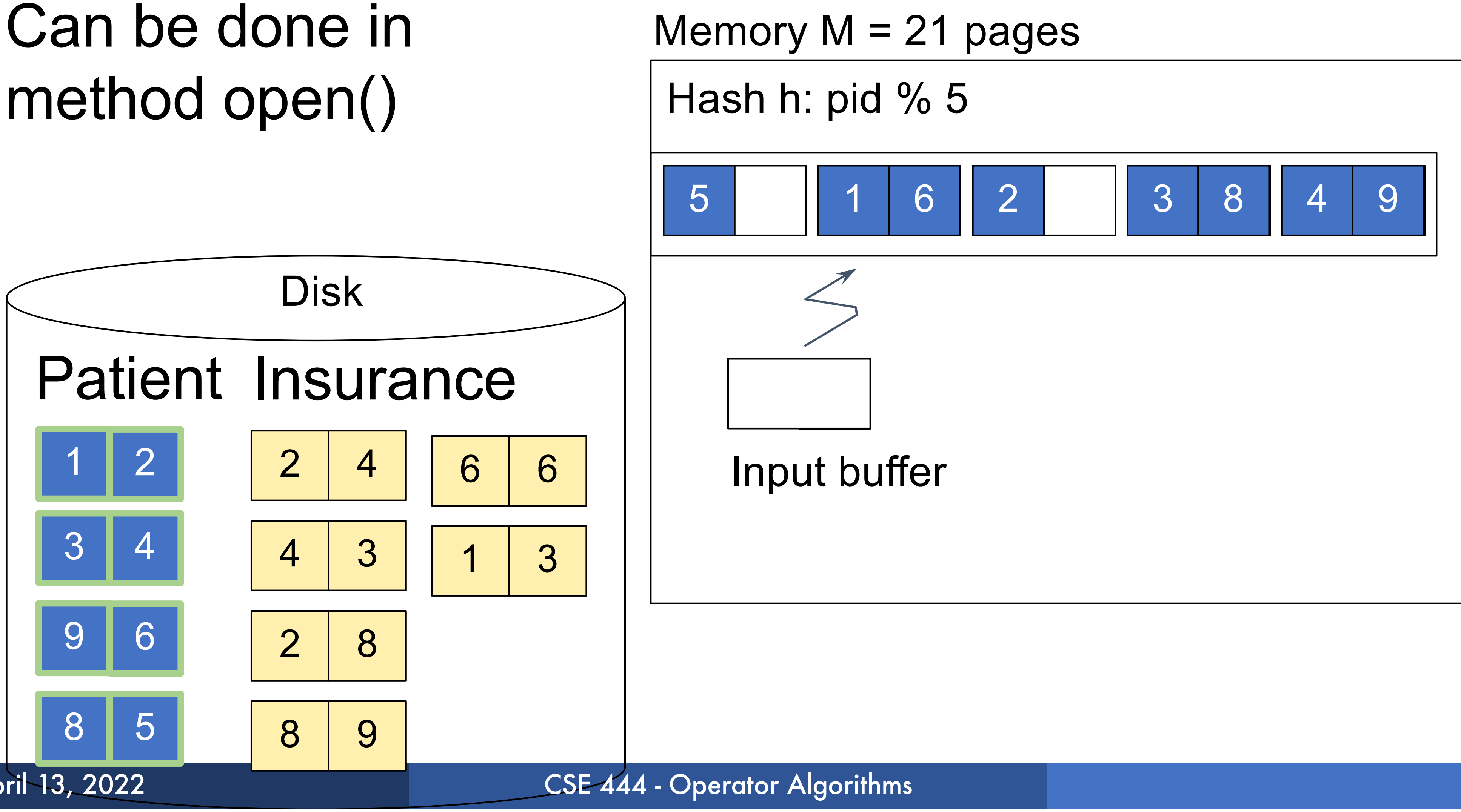
Hash Join Example



Hash Join Example

Step 1: Scan Patient and build hash table in memory

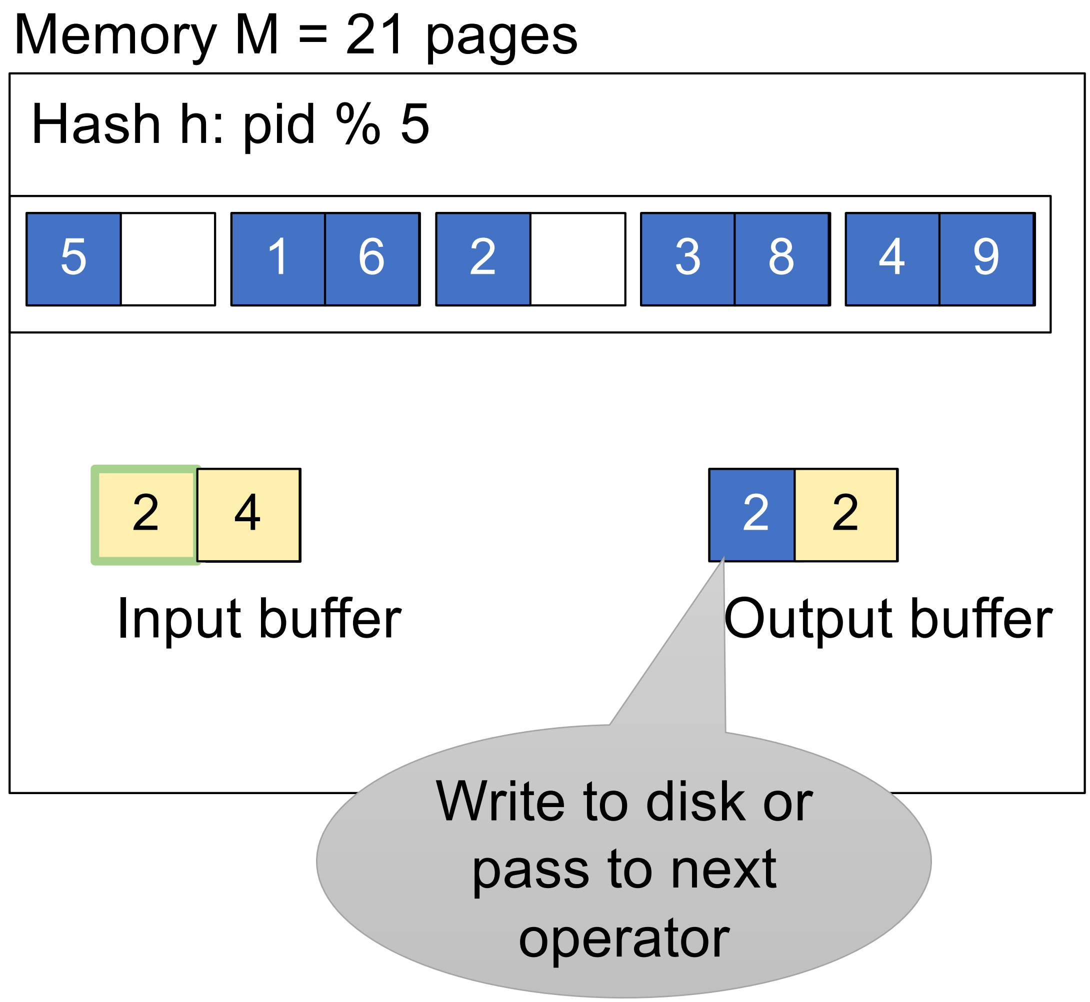
Can be done in method open()

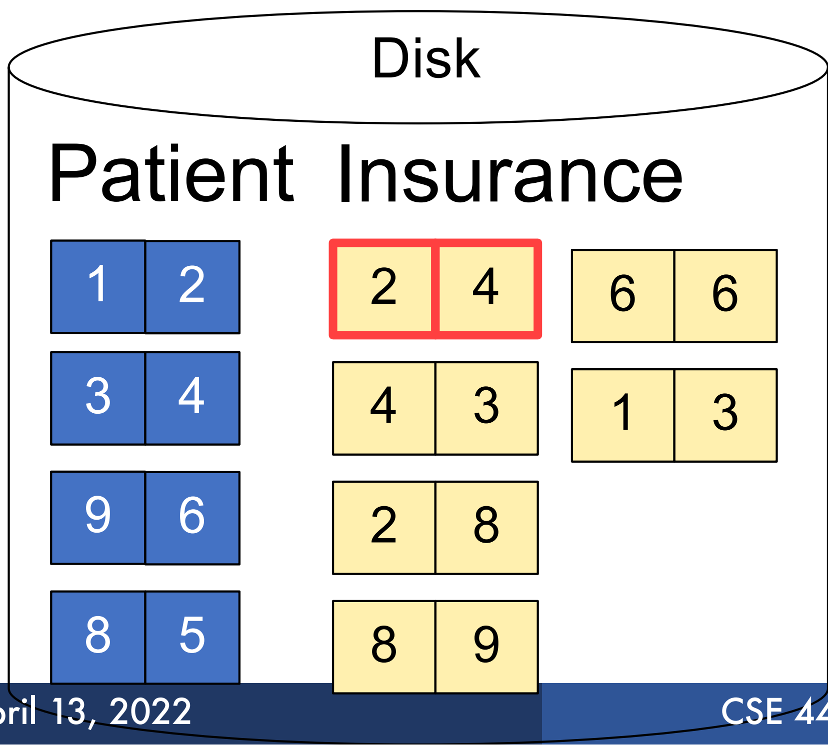


Hash Join Example

Step 2: Scan Insurance and probe into hash table

Done during calls to next()





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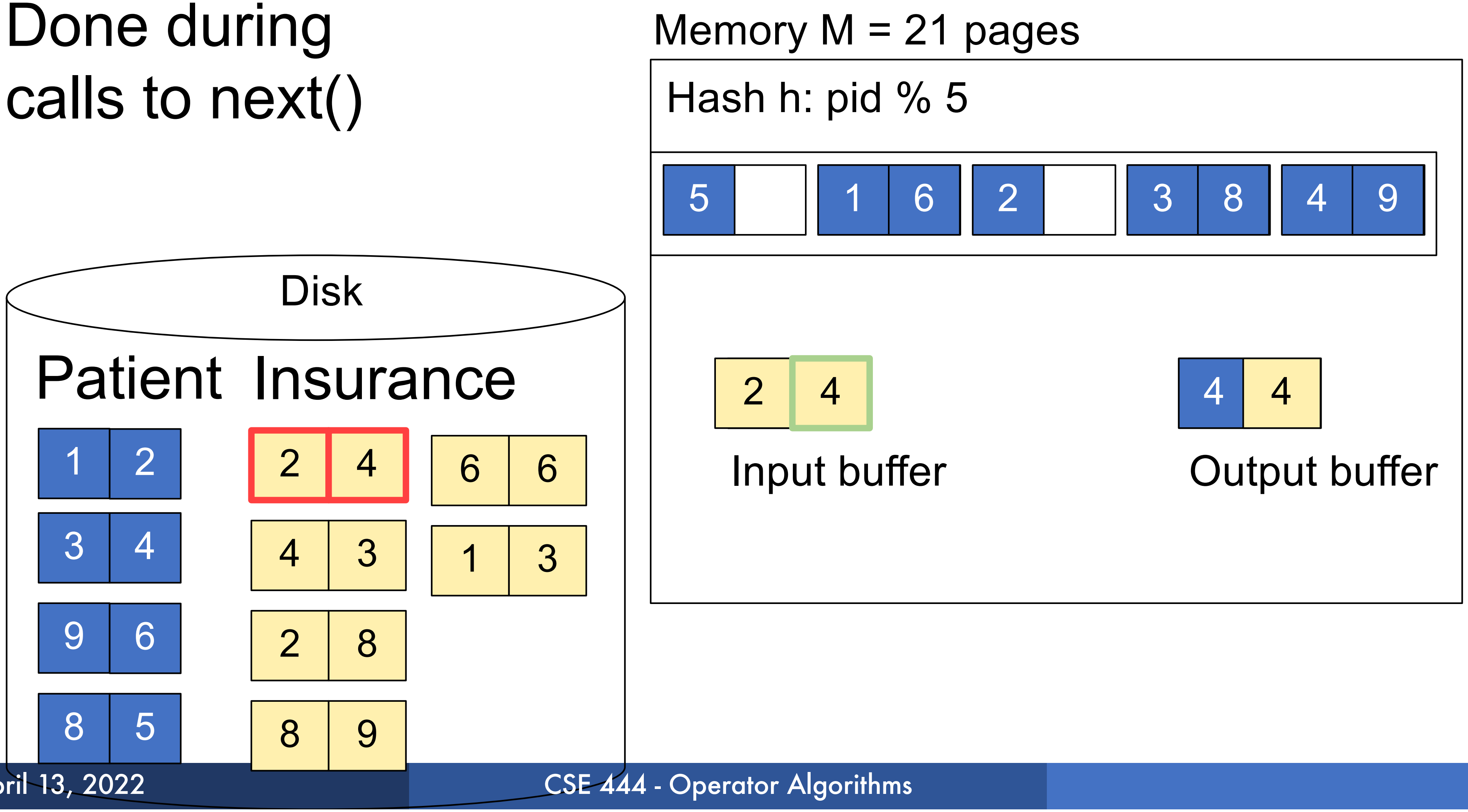
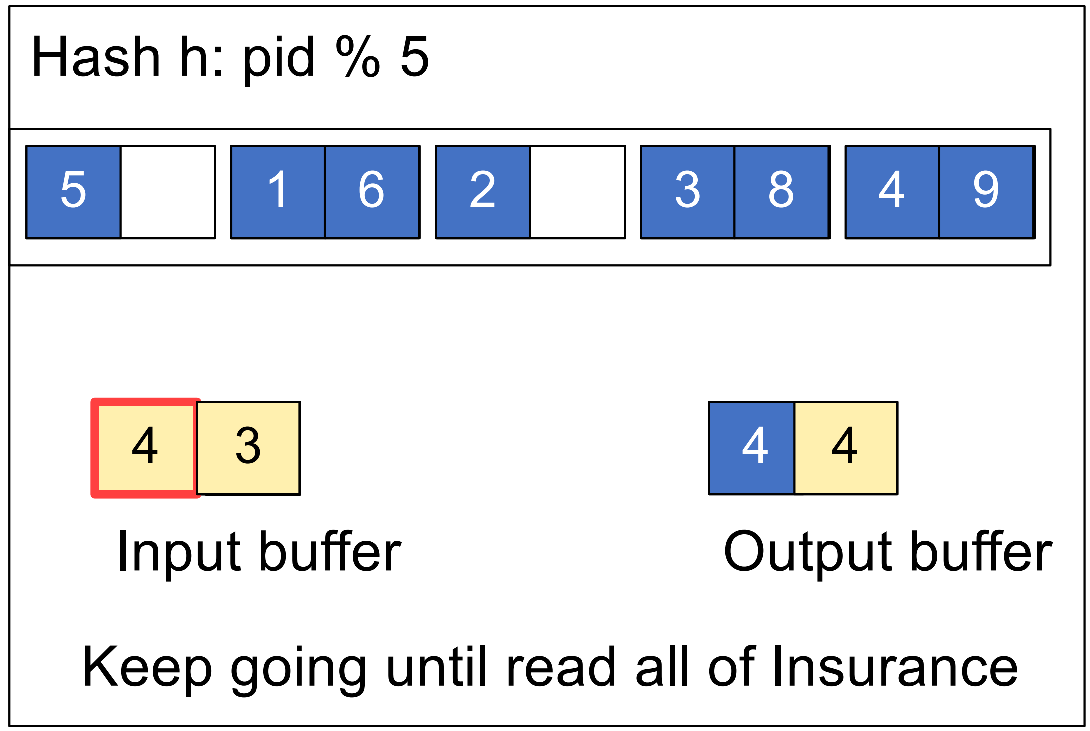


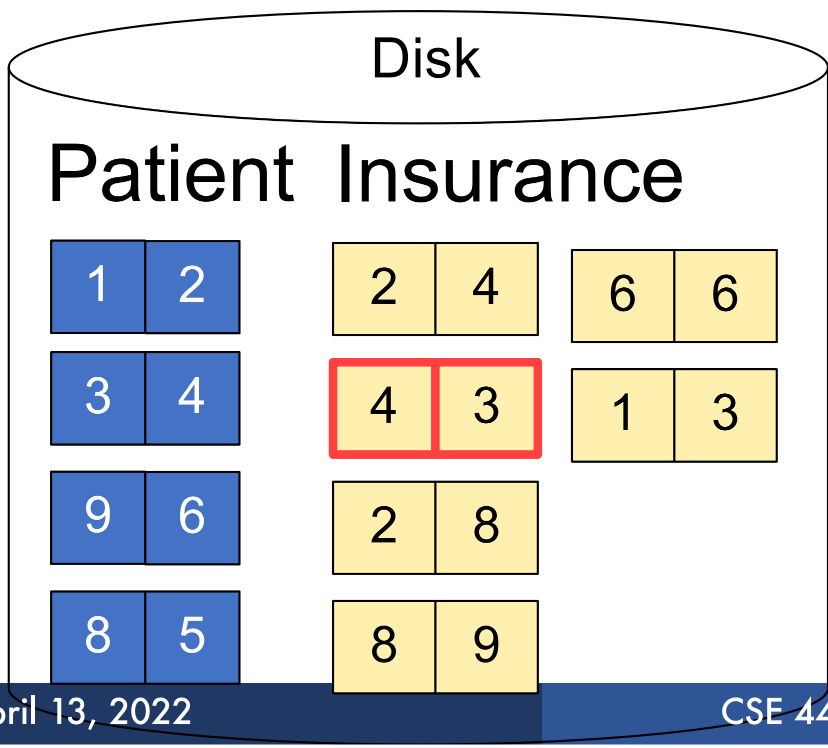
Hash Join Example

Step 2: Scan Insurance and probe into hash table

Done during calls to next()

Memory M = 21 pages





Cost: B(R) + B(S)

Discussion

- Hash-join is the workhorse of database systems
- The hash table is built on the heap, not in BP;
  hence it is not organized in pages,
  but pages are still convenient to measure its size
- Hash-join works great when:
  - The inner table fits in main memory
  - The hash function is good (never write your own!)
  - The data has no skew (discuss in class…)

Nested Loop Joins

- Tuple-based nested loop $R \bowtie S$
- R is the outer relation, S is the inner relation

```
for each tuple t1 in R do
   for each tuple t2 in S do
      if t1 and t2 join then output (t1,t2)
```

What is the Cost?

Nested Loop Joins

- Tuple-based nested loop $R \bowtie S$
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for each tuple t1 in R do
   for each tuple t2 in S do
      if t1 and t2 join then output (t1,t2)
```

What is the Cost?

- Cost: B(R) + T(R) B(S)
- Multiple-pass since S is read many times

Page-at-a-time Refinement

```
for each page of tuples r in R do
  for each page of tuples s in S do
    for all pairs of tuples t1 in r, t2 in s
      if t1 and t2 join then output (t1,t2)
```

What is the Cost?

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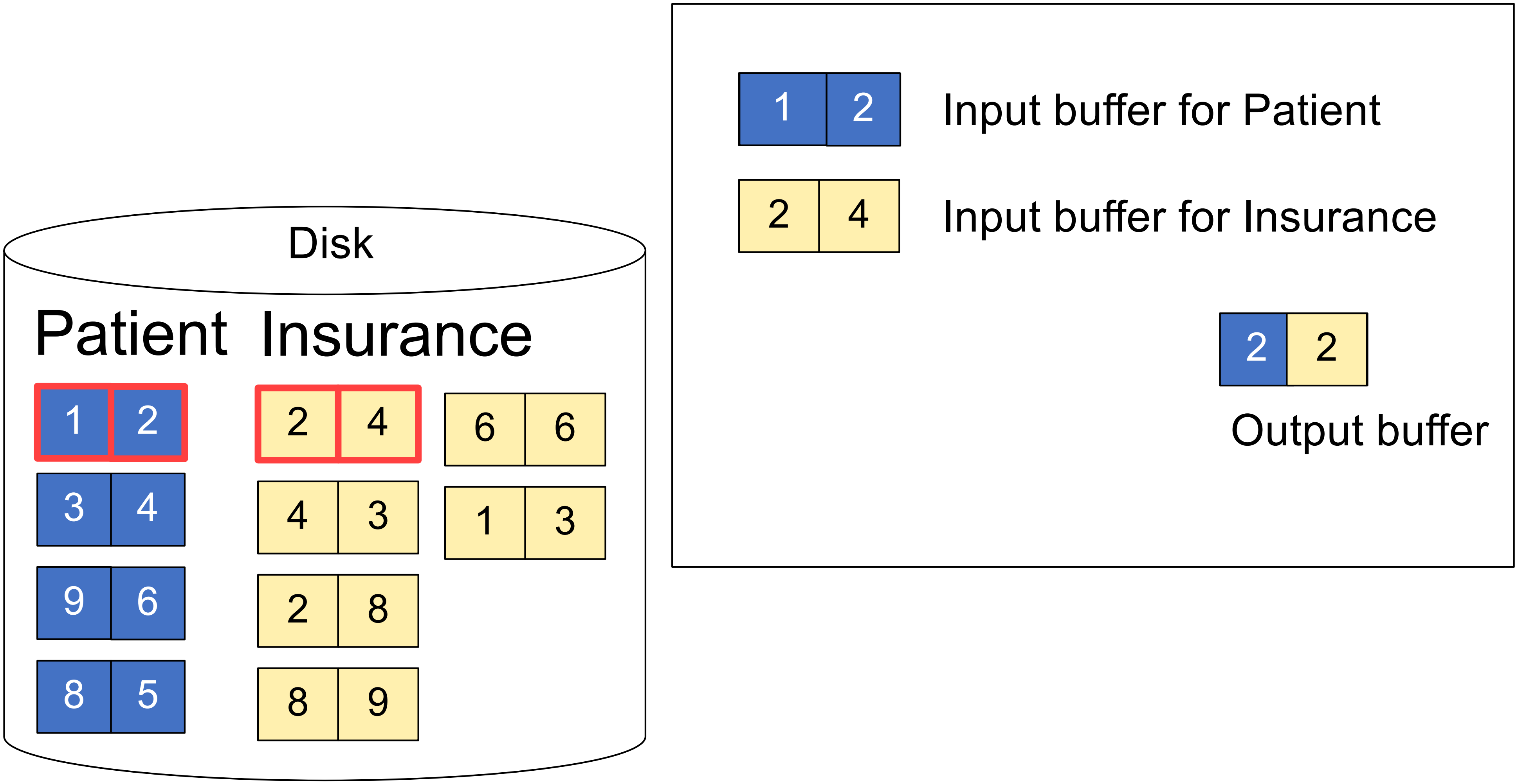
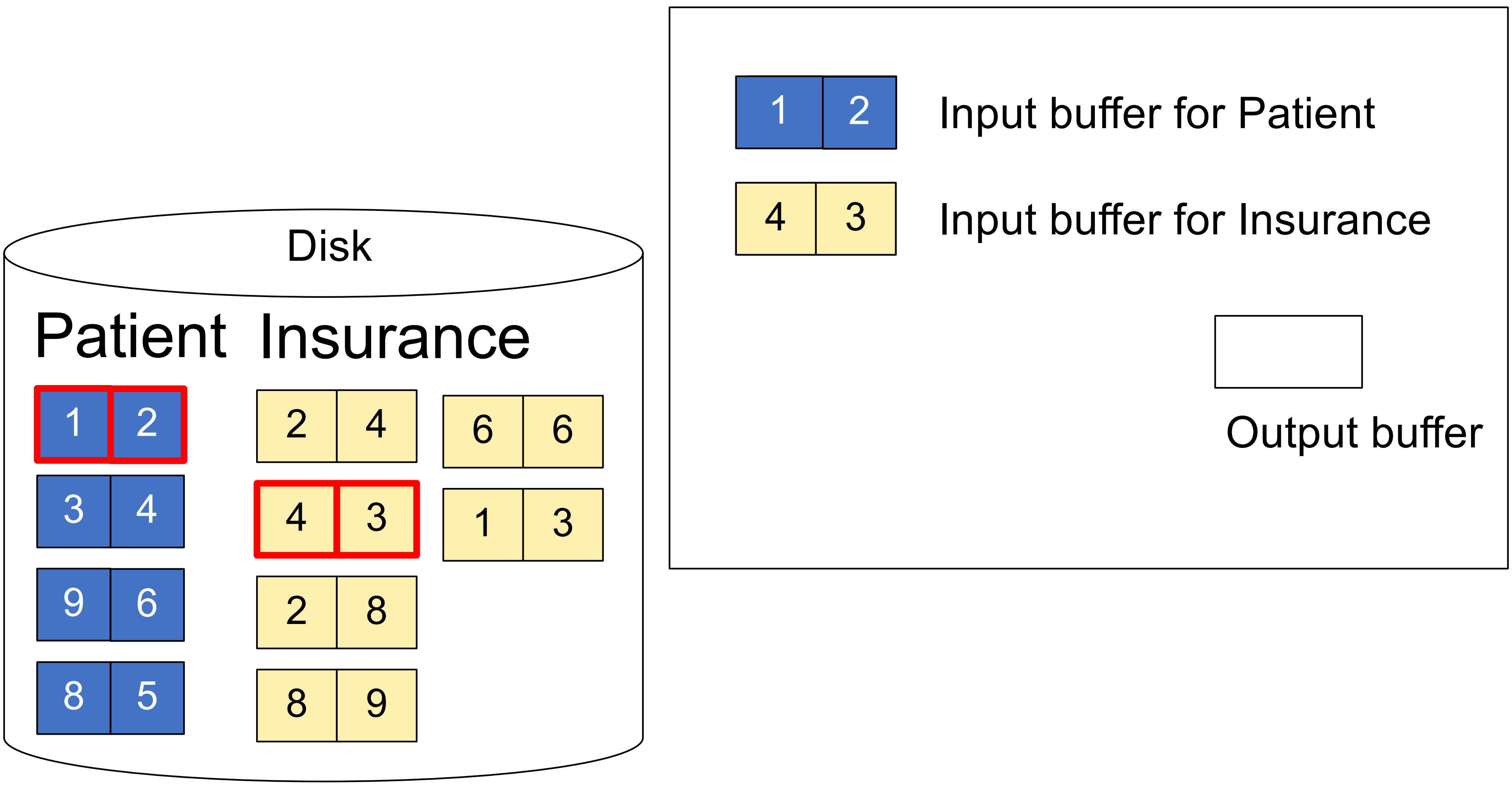
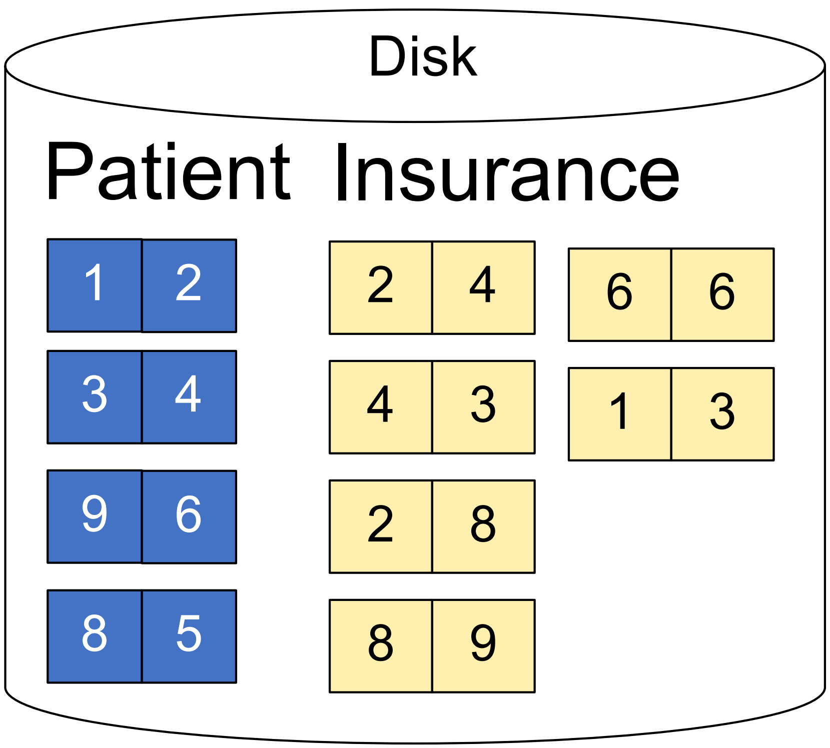
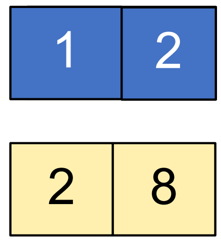


Page-at-a-time Refinement



Page-at-a-time Refinement

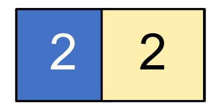




Input buffer for Patient

Input buffer for Insurance

Keep going until read all of Insurance



Output buffer

Then repeat for next page of Patient… until end of Patient

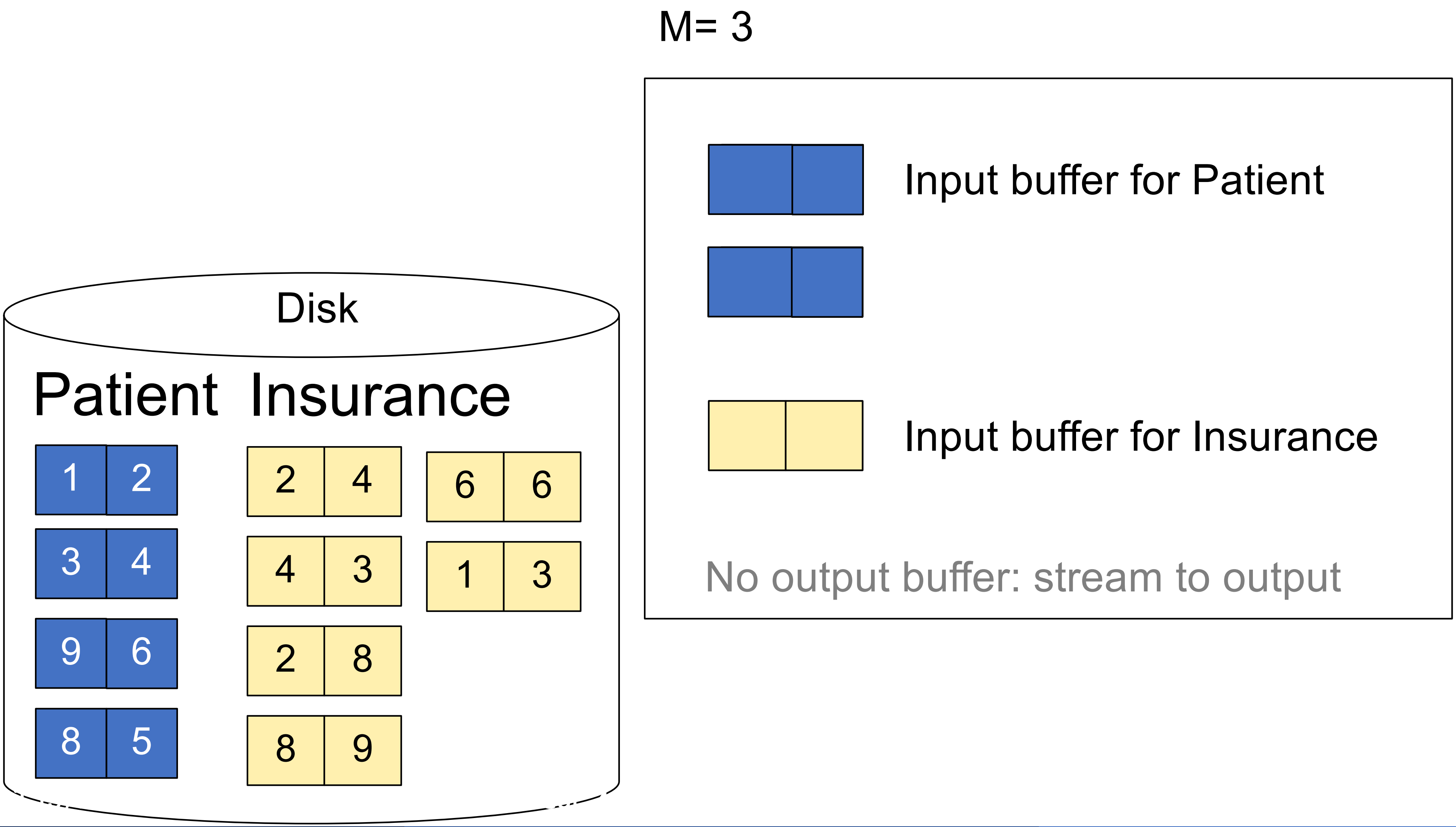
Cost: B(R) + B(R)B(S)

Block-Memory Refinement

```
for each group of M-1 pages r in R do
   for each page of tuples s in S do
     for all pairs of tuples t1 in r, t2 in s
         if t1 and t2 join then output (t1,t2)
```

What is the Cost?

Block Memory Refinement



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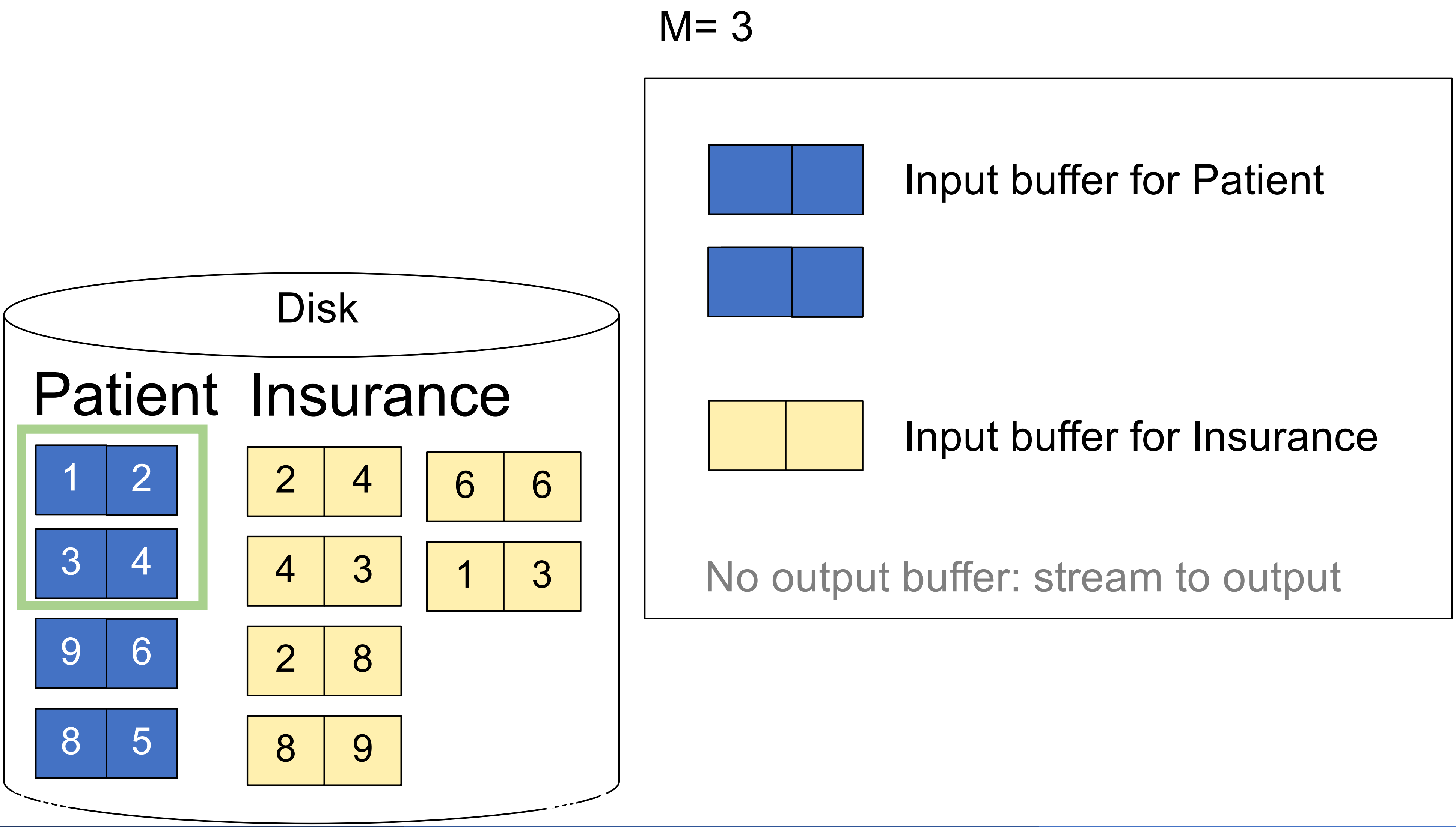

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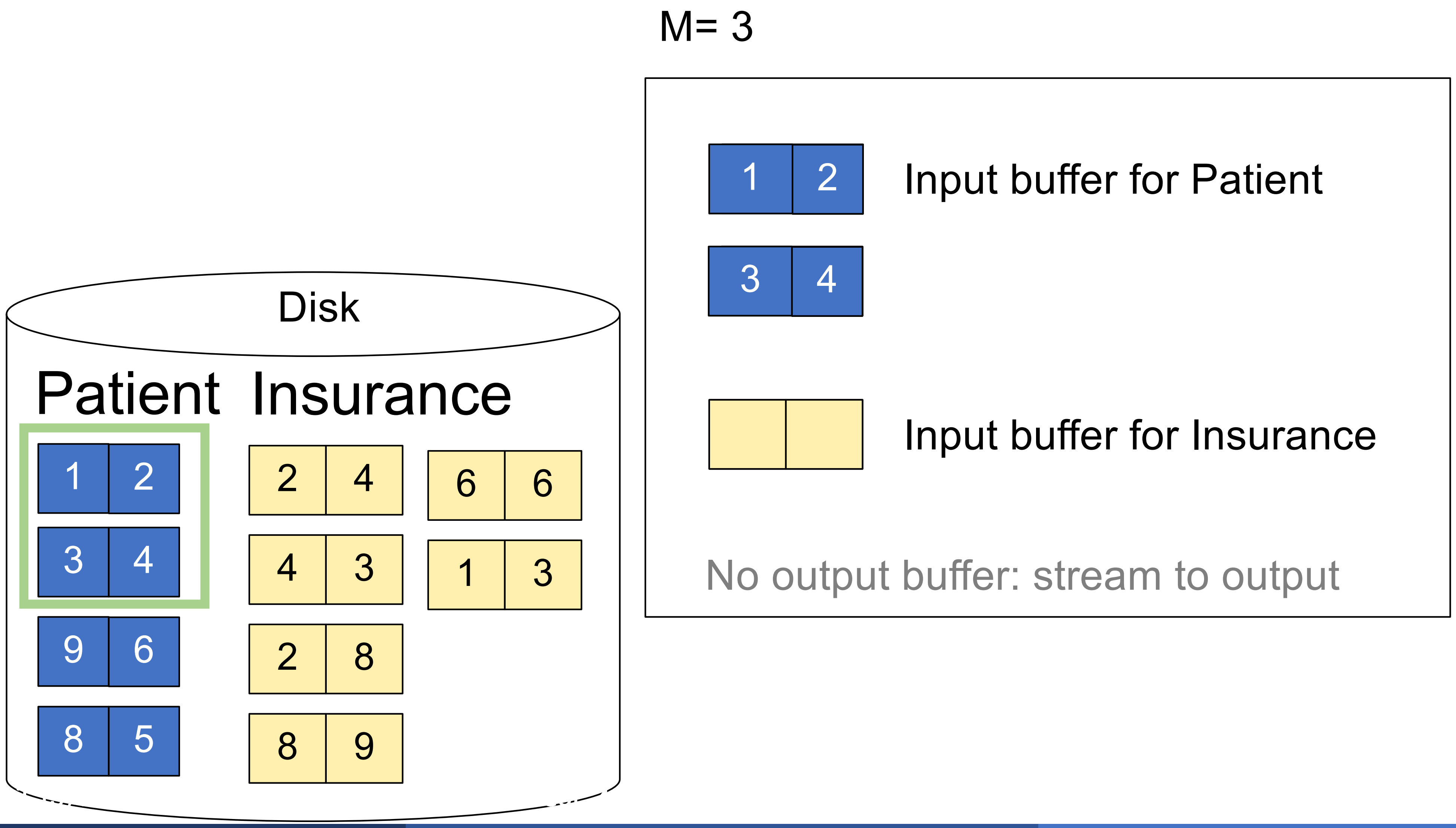

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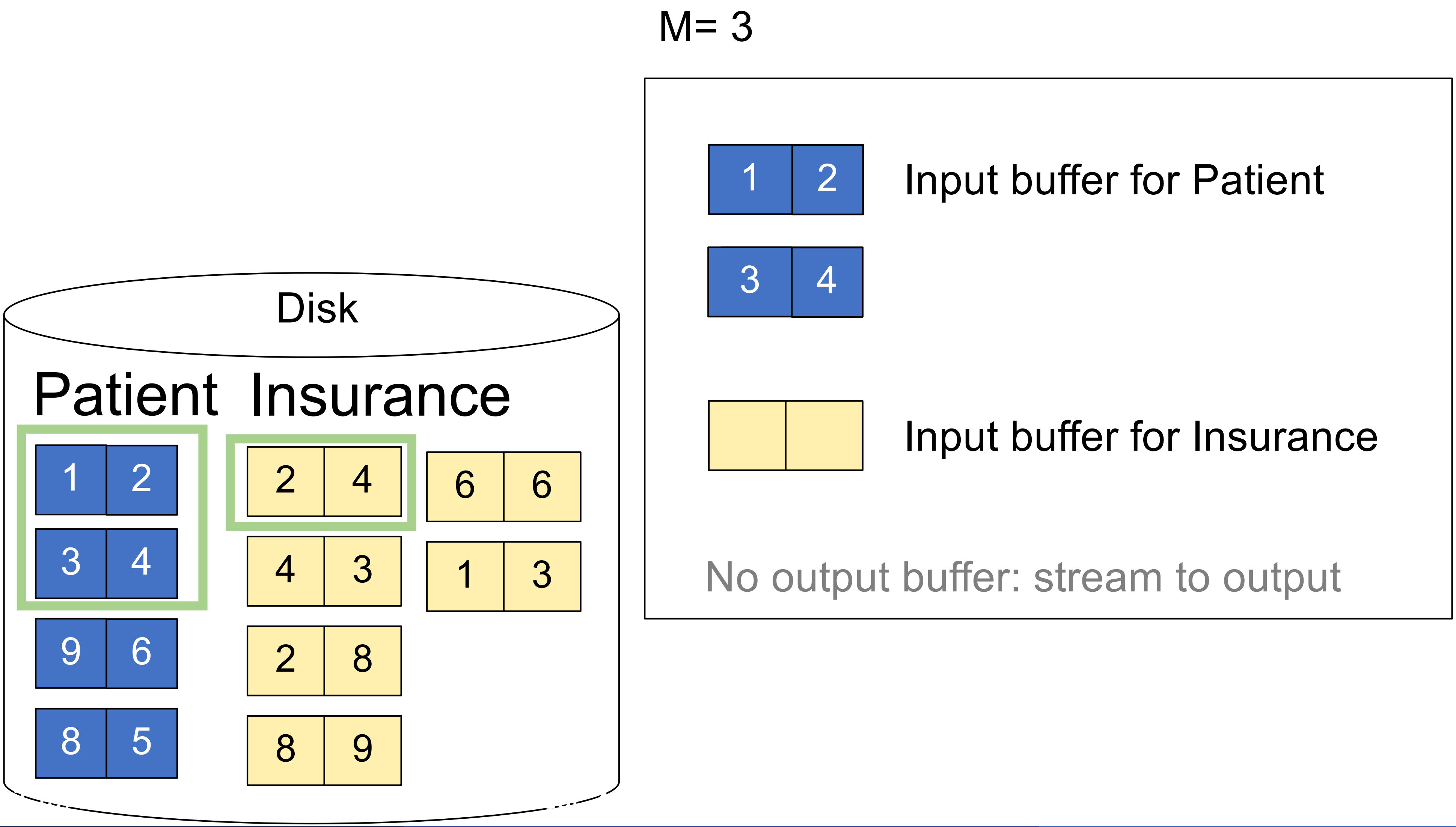
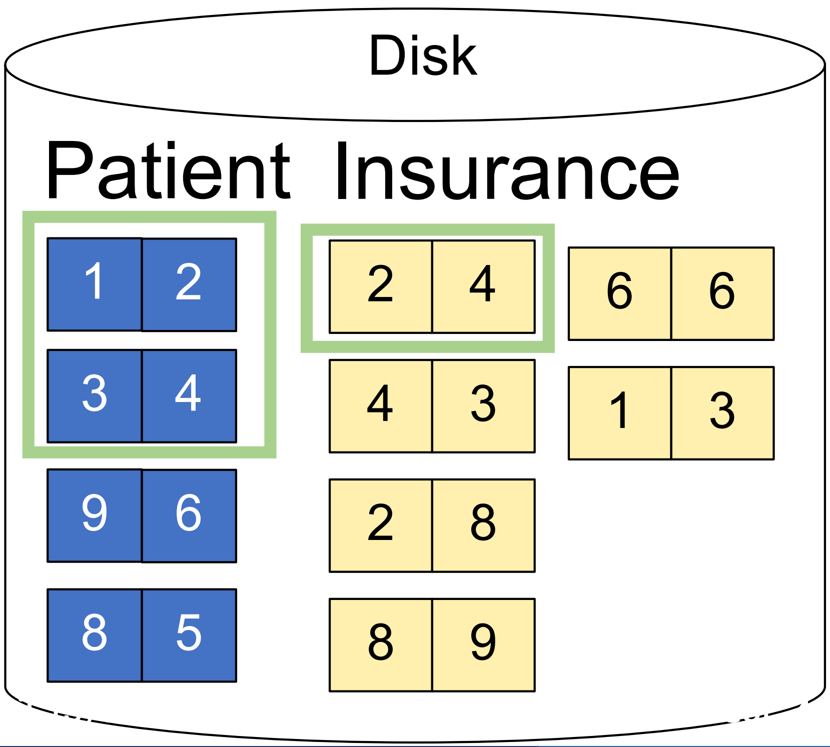
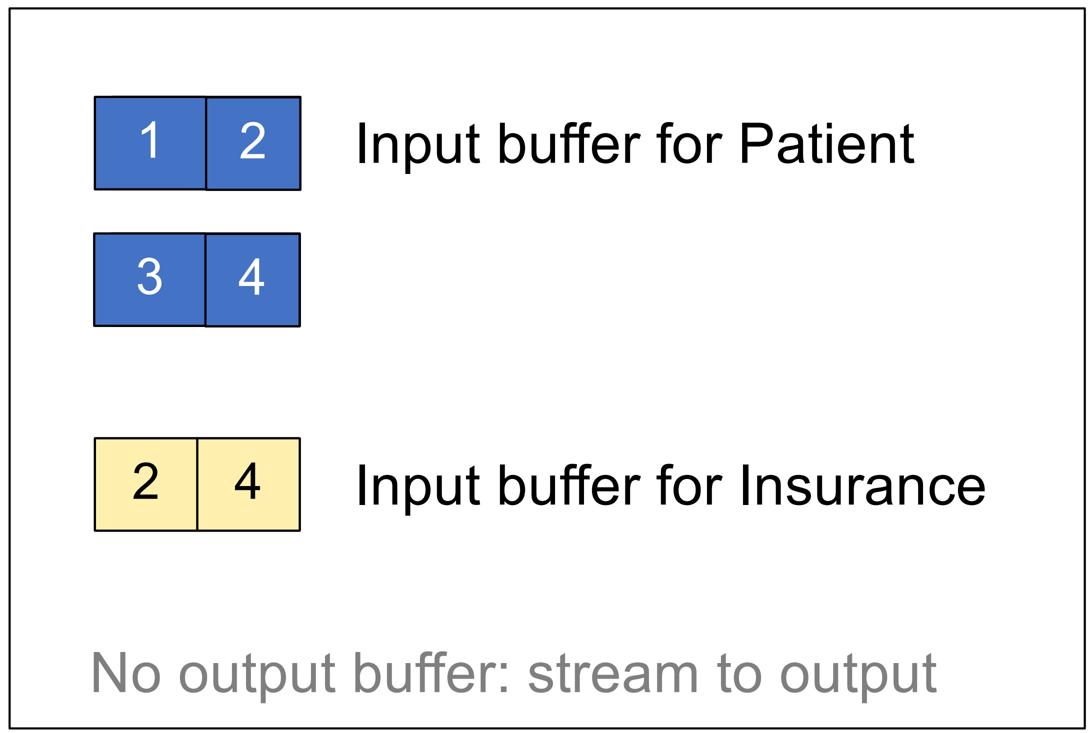


Block Memory Refinement

M= 3





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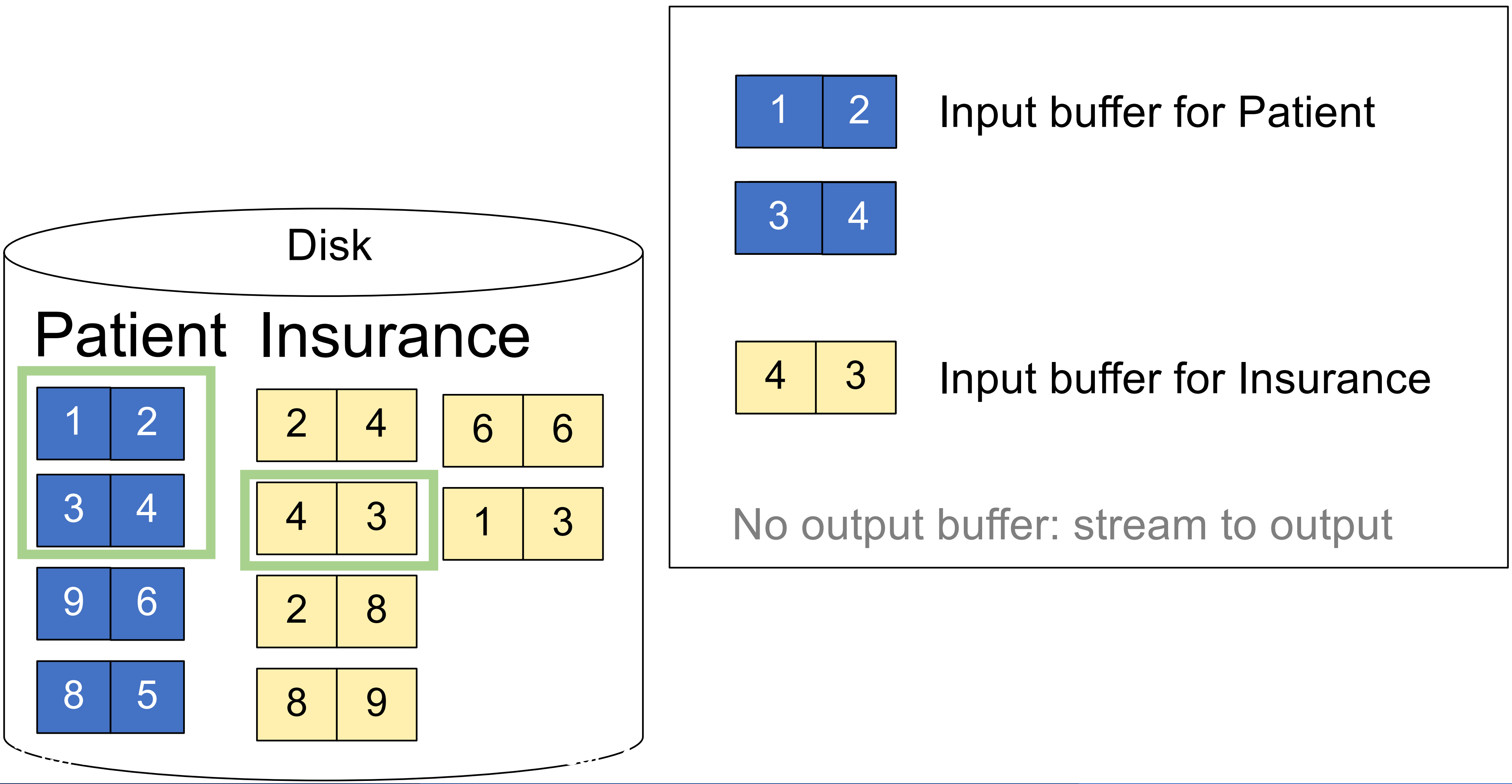

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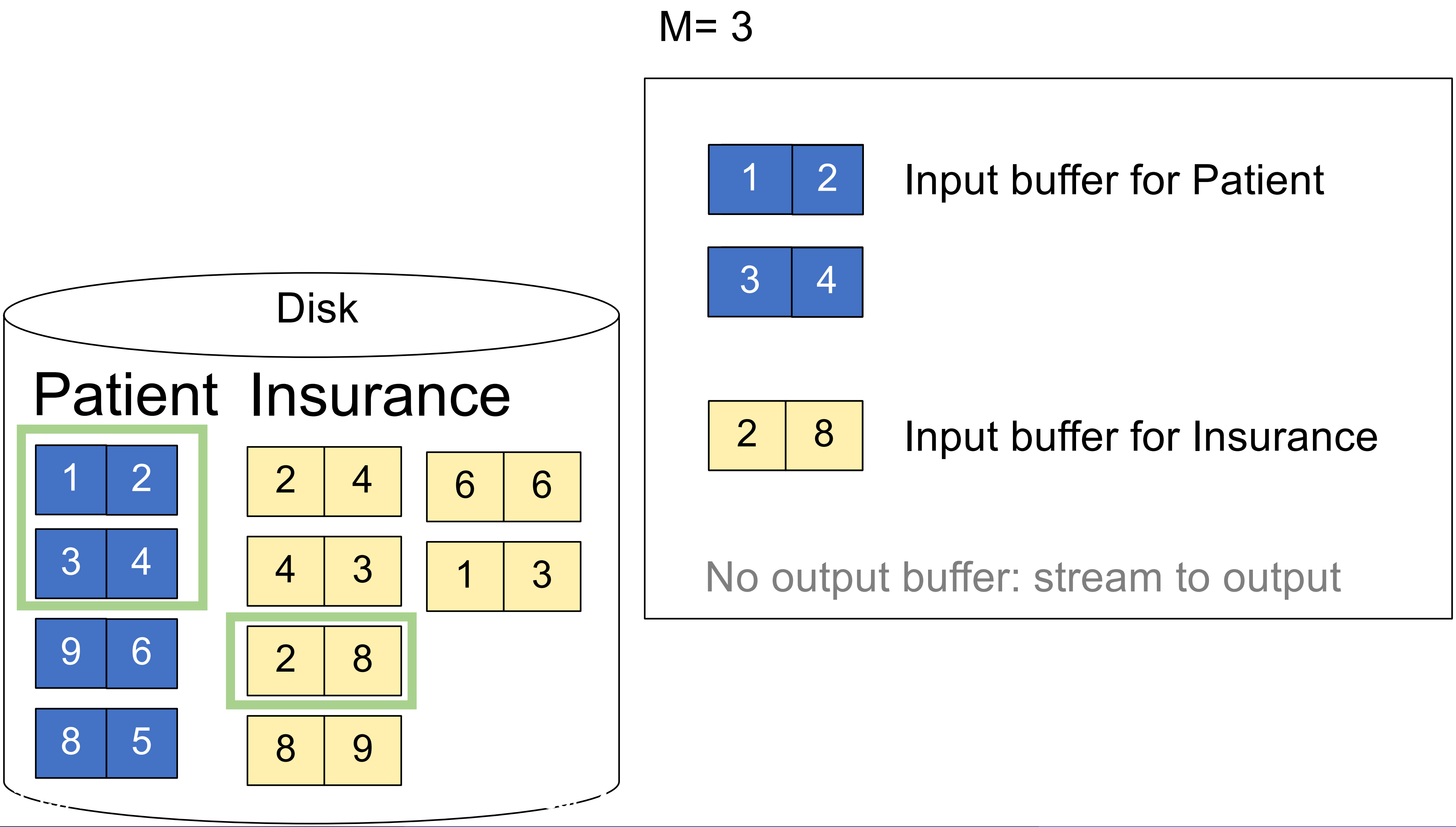

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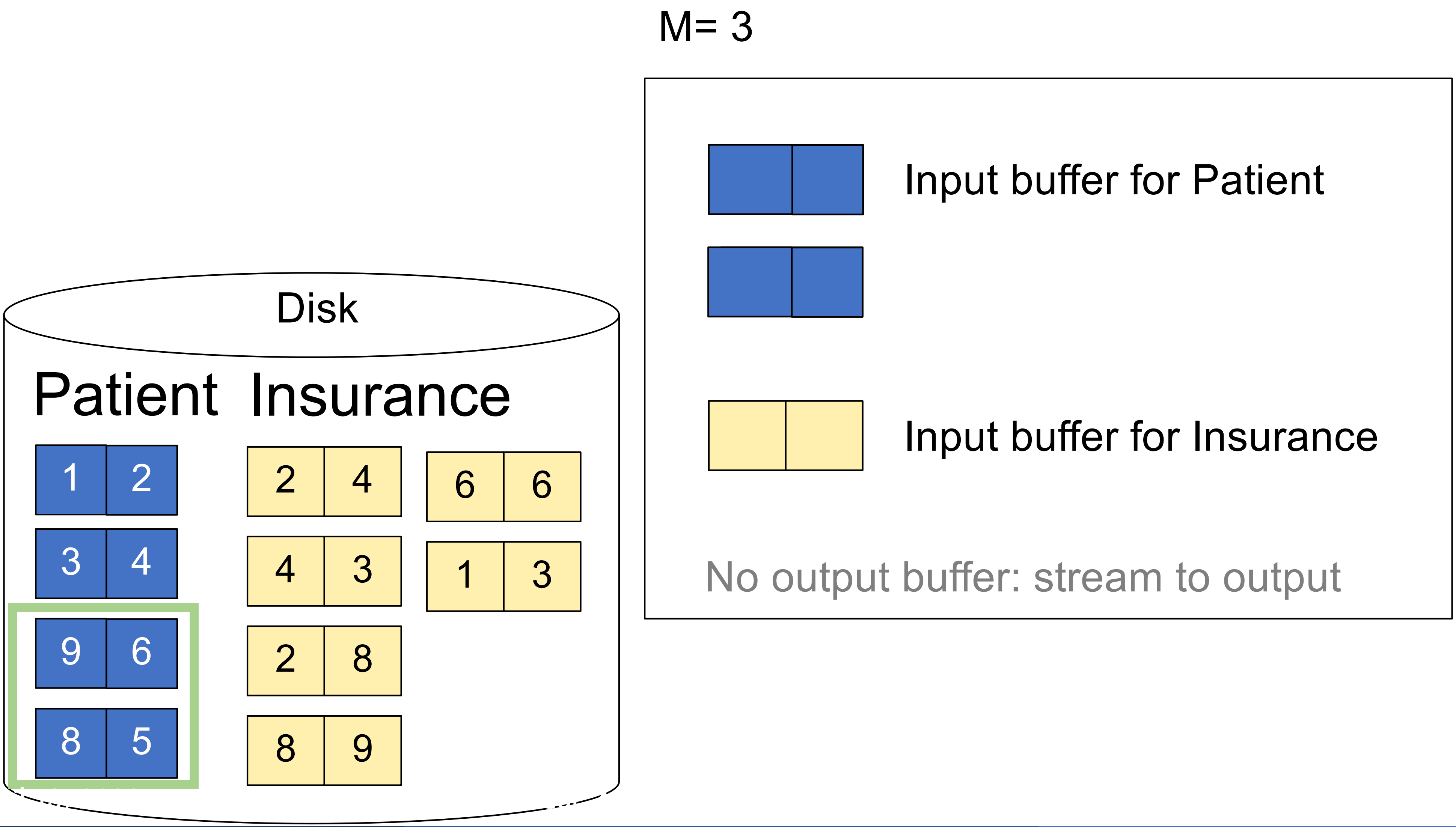

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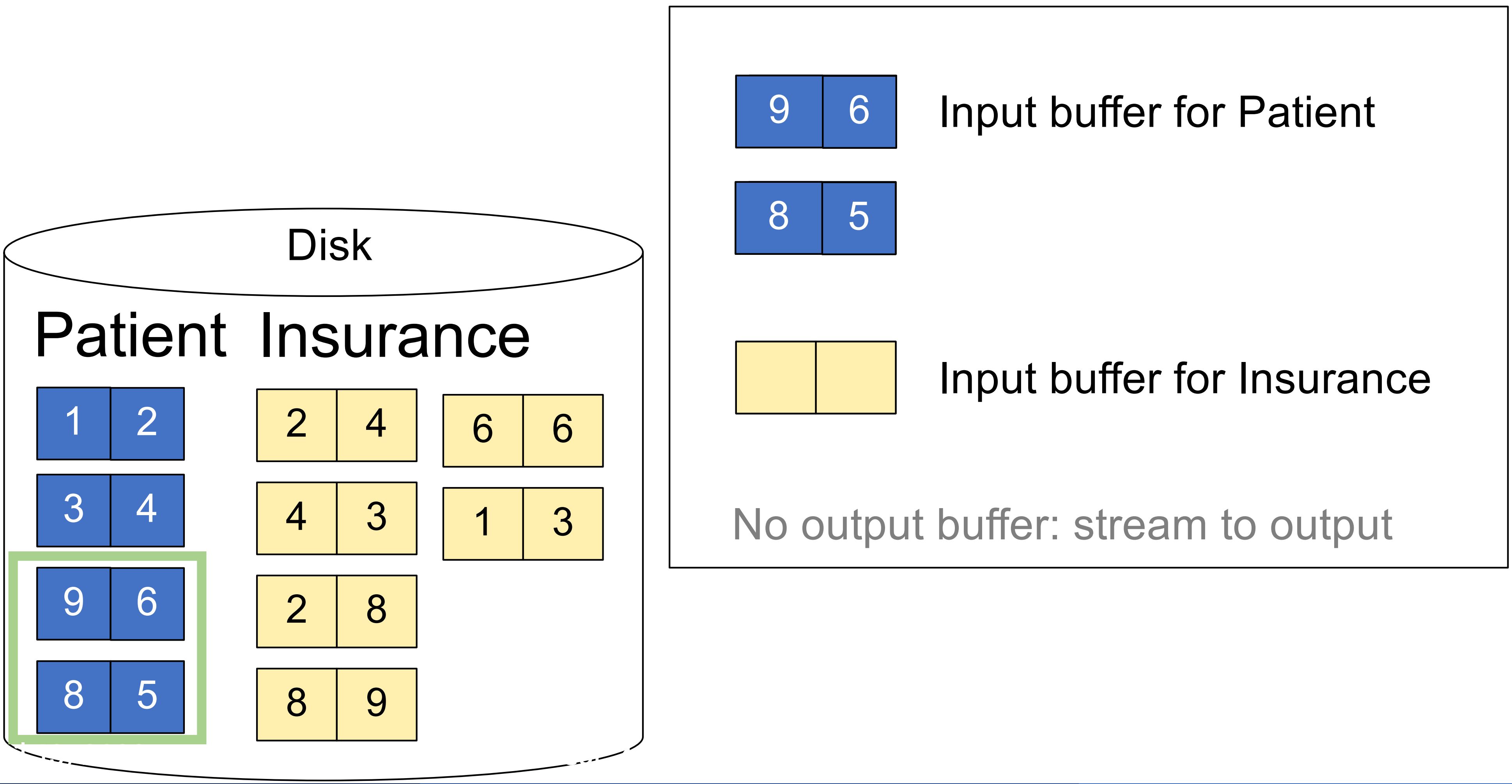

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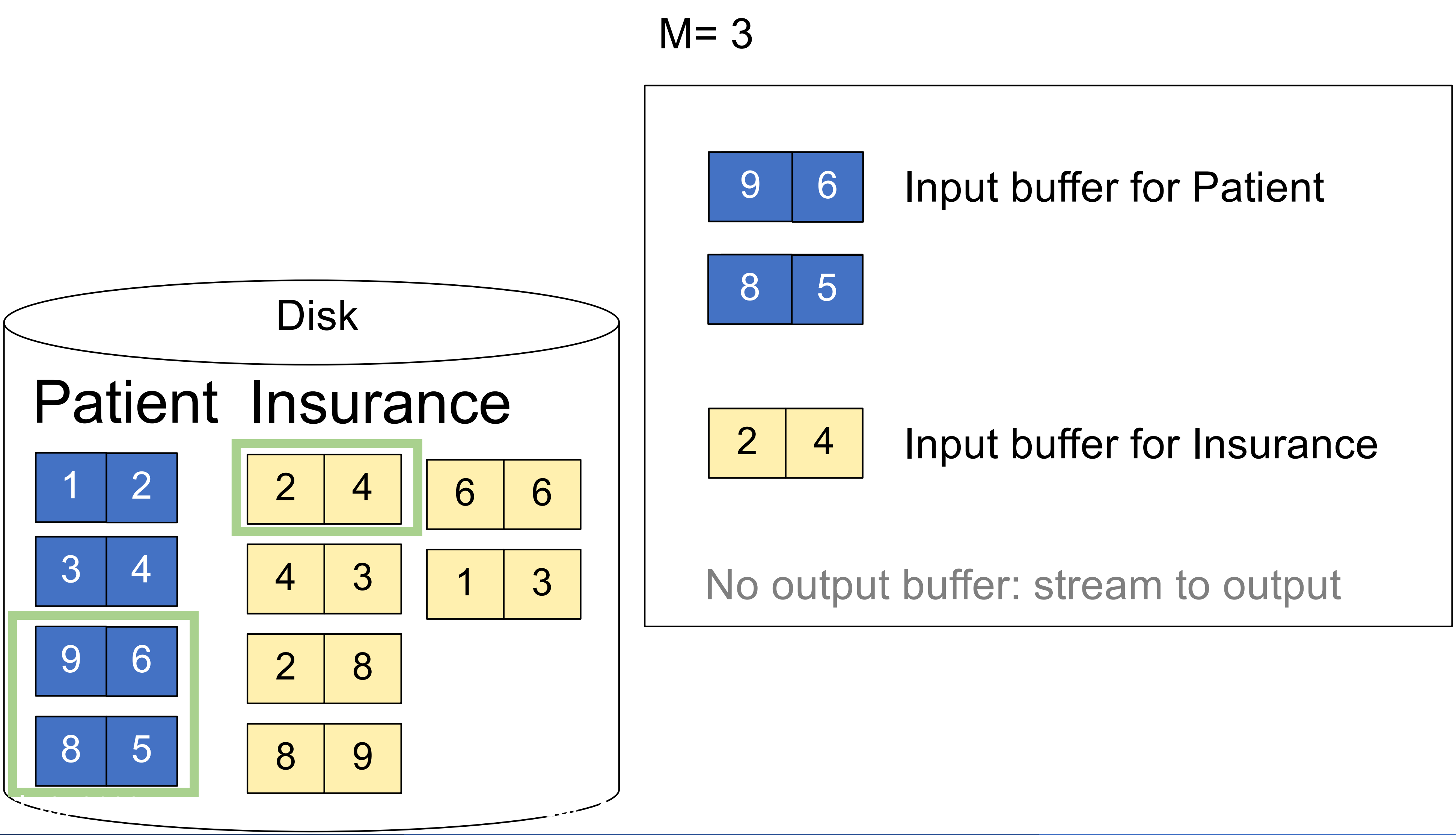

Block Memory Refinement

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What is the Cost

Block Memory Refinement

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```

- Cost: $B(R) + B(R)B(S)/(M-1)$

What is the Cost

Discussion

$R \bowtie S$: R=outer table, S=inner table

- Tuple-based nested loop join is never used

- Page-at-a-time nested loop join:
  - Usually combined with index access to inner table
  - Efficient when the outer table is small

- Block memory refinement nested loop:
  - Usually builds a hash table on the outer table
  - Efficient when the outer table is small

Sort-Merge Join

Sort-merge join: R ⋈ S

- Scan R and sort in main memory
- Scan S and sort in main memory
- Merge R and S

Sort-Merge Join

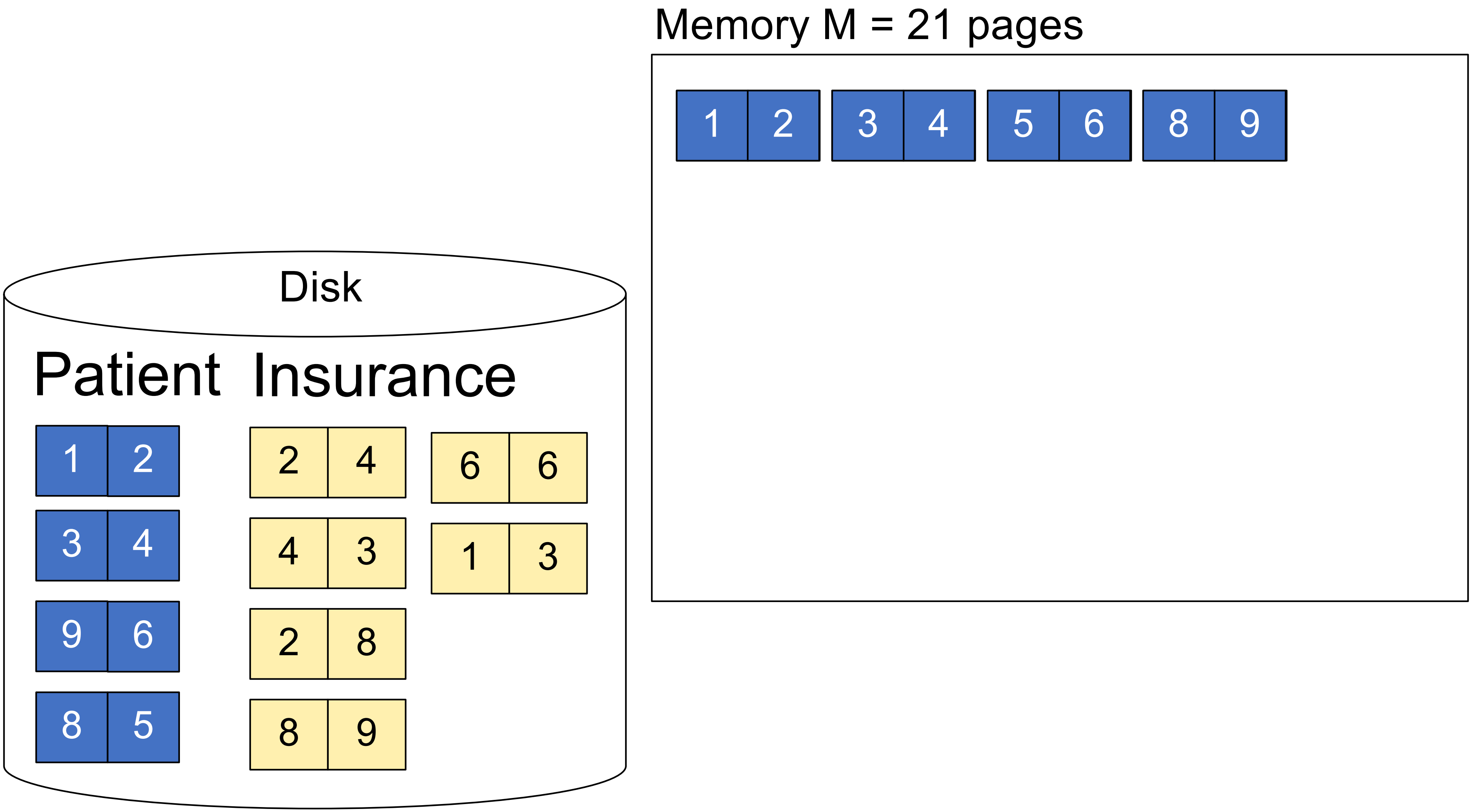
Sort-merge join: R ⋈ S

- Scan R and sort in main memory
- Scan S and sort in main memory
- Merge R and S

- Cost: B(R) + B(S)
- One pass algorithm when B(S) + B(R) <= M
- Typically, this is NOT a one pass algorithm,
  - We'll see the multi-pass version next lecture

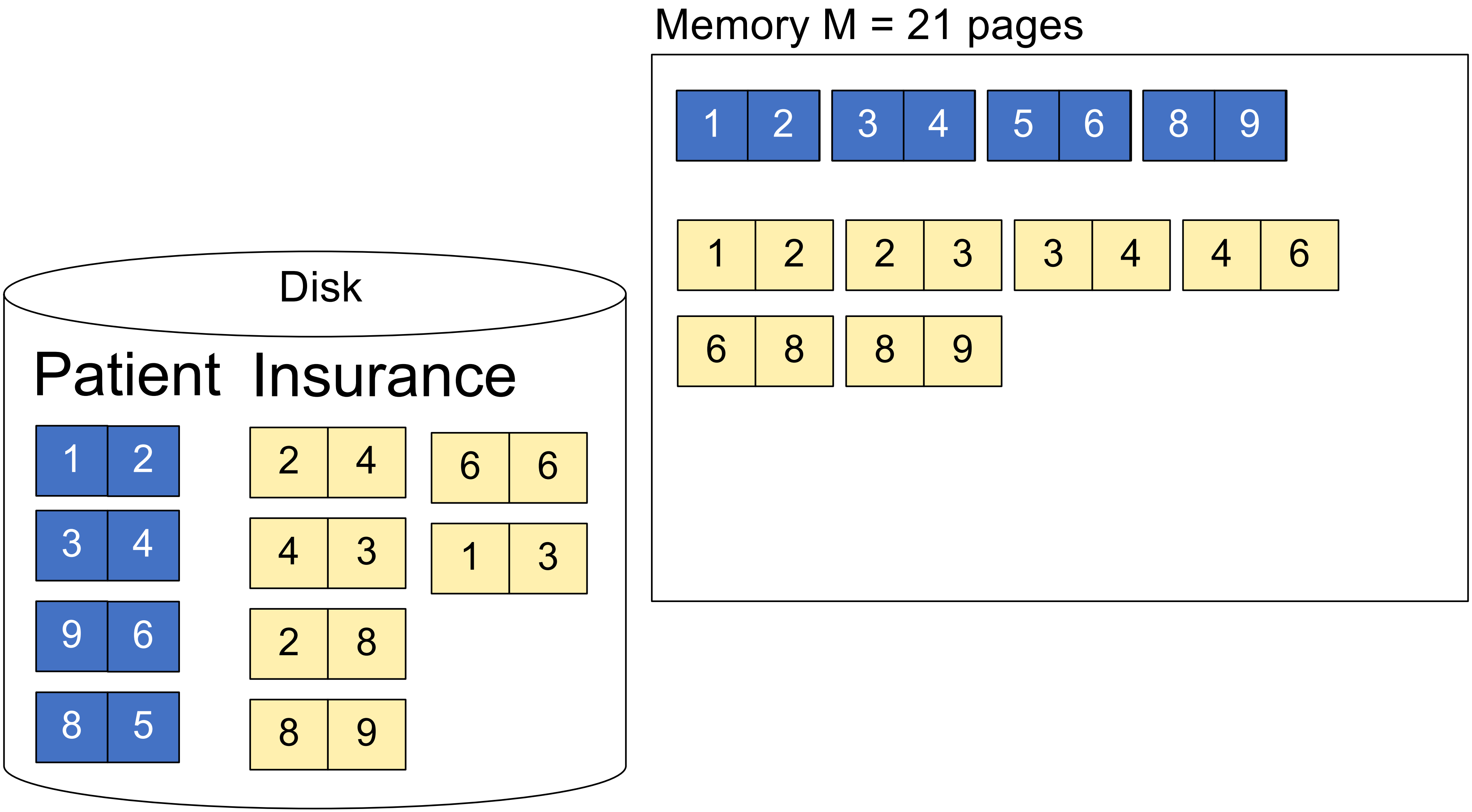
Sort-Merge Join Example

Step 1: Scan Patient and sort in memory



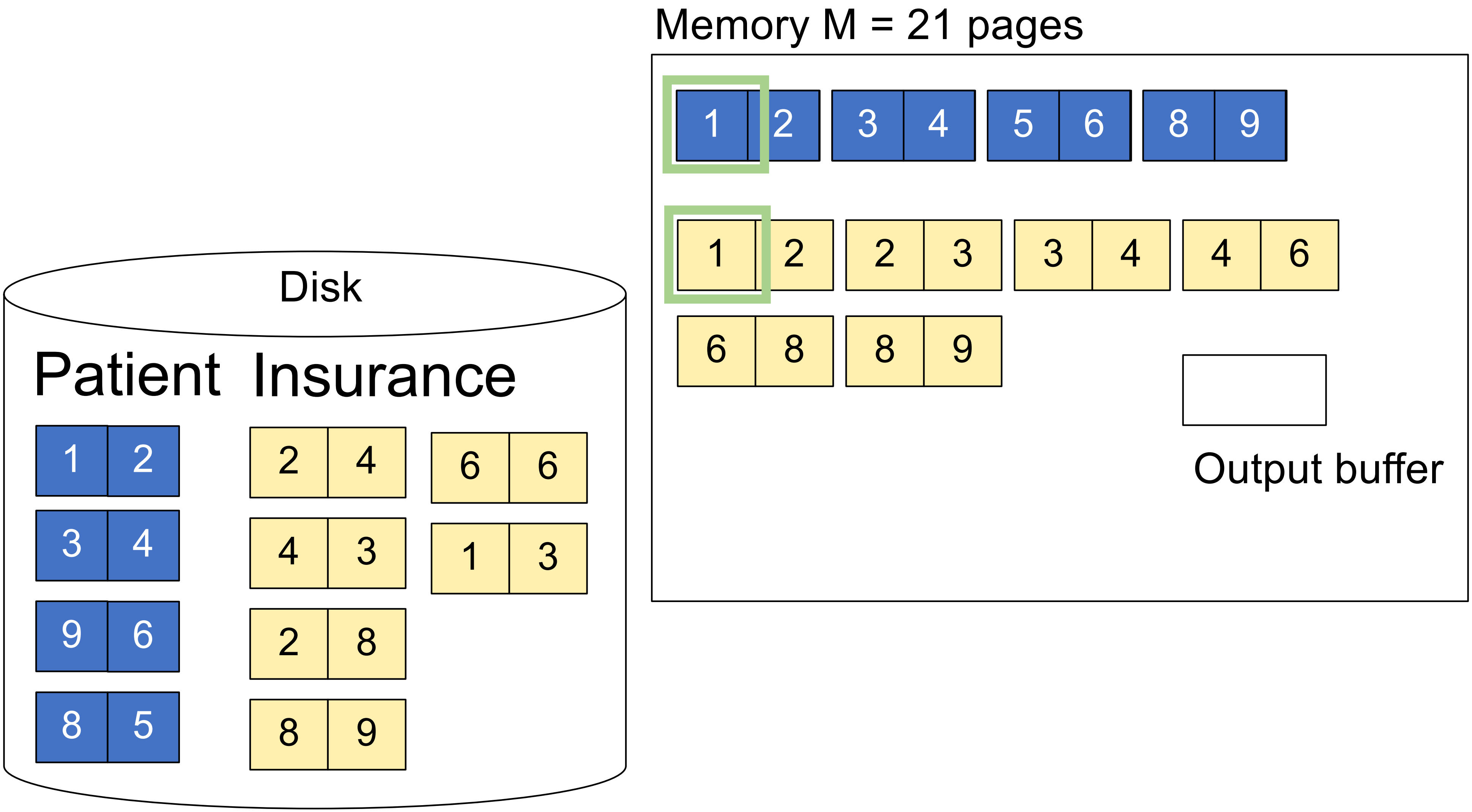
Sort-Merge Join Example

Step 2: Scan Insurance and sort in memory



Sort-Merge Join Example

Step 3: Merge Patient and Insurance



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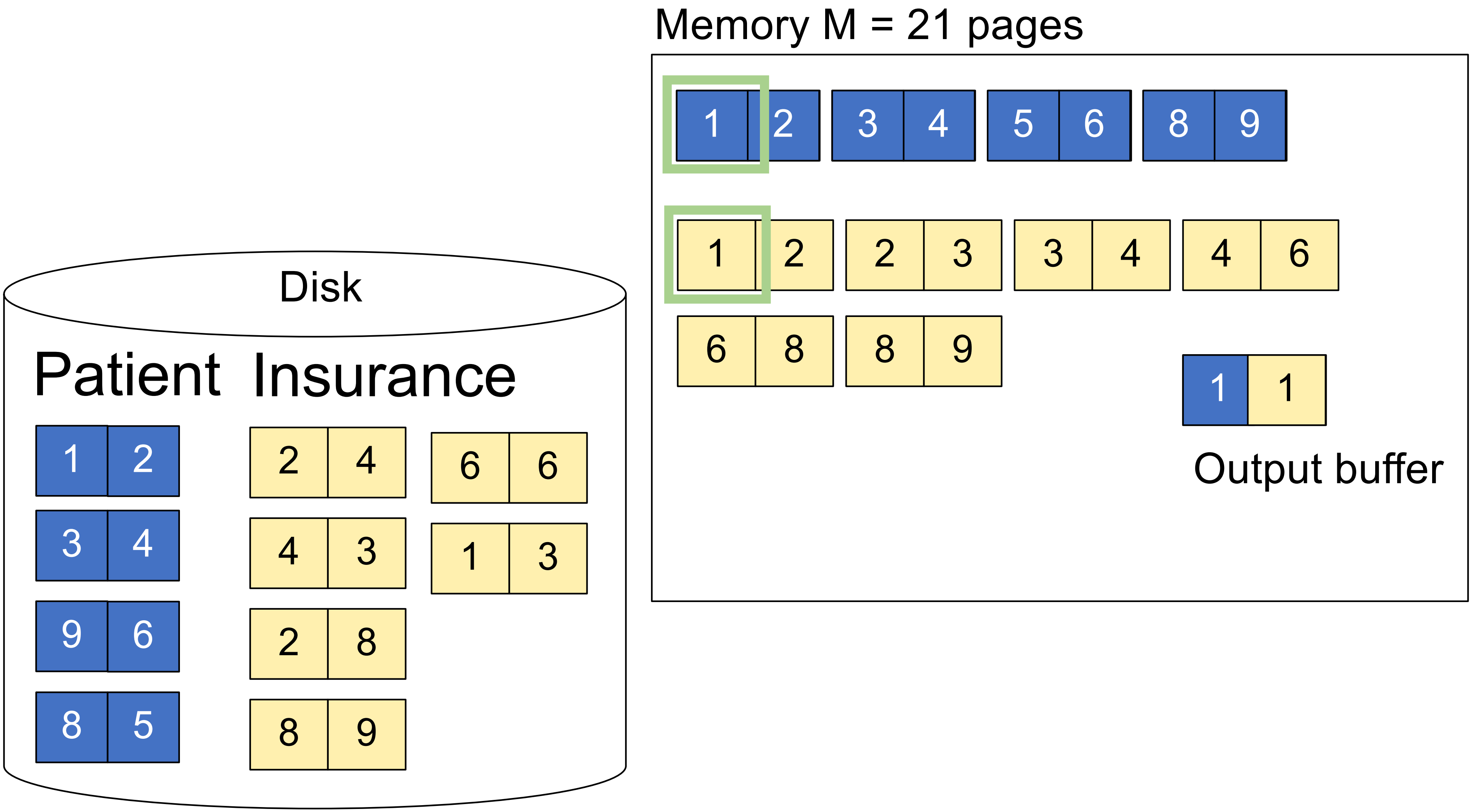

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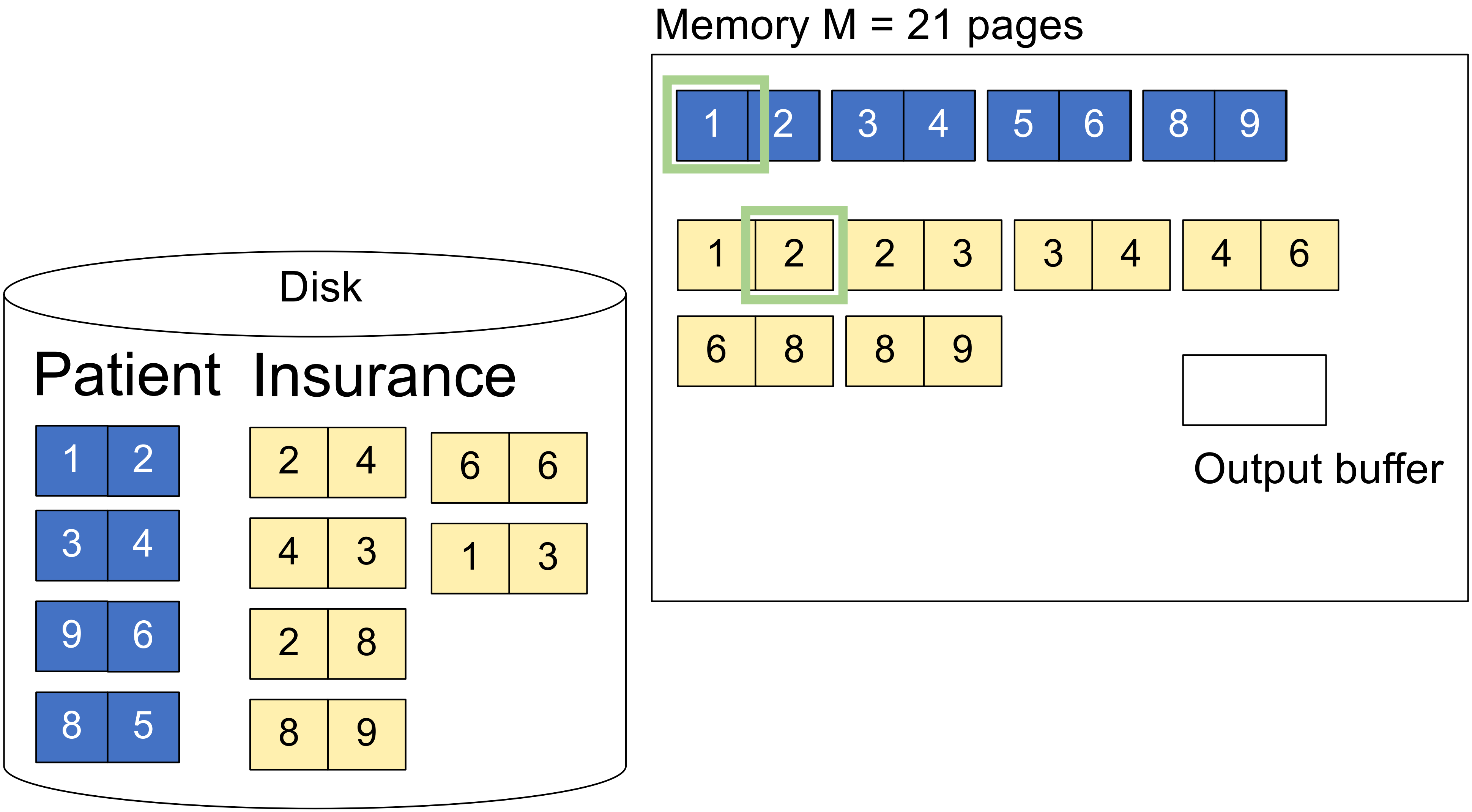

Sort-Merge Join Example

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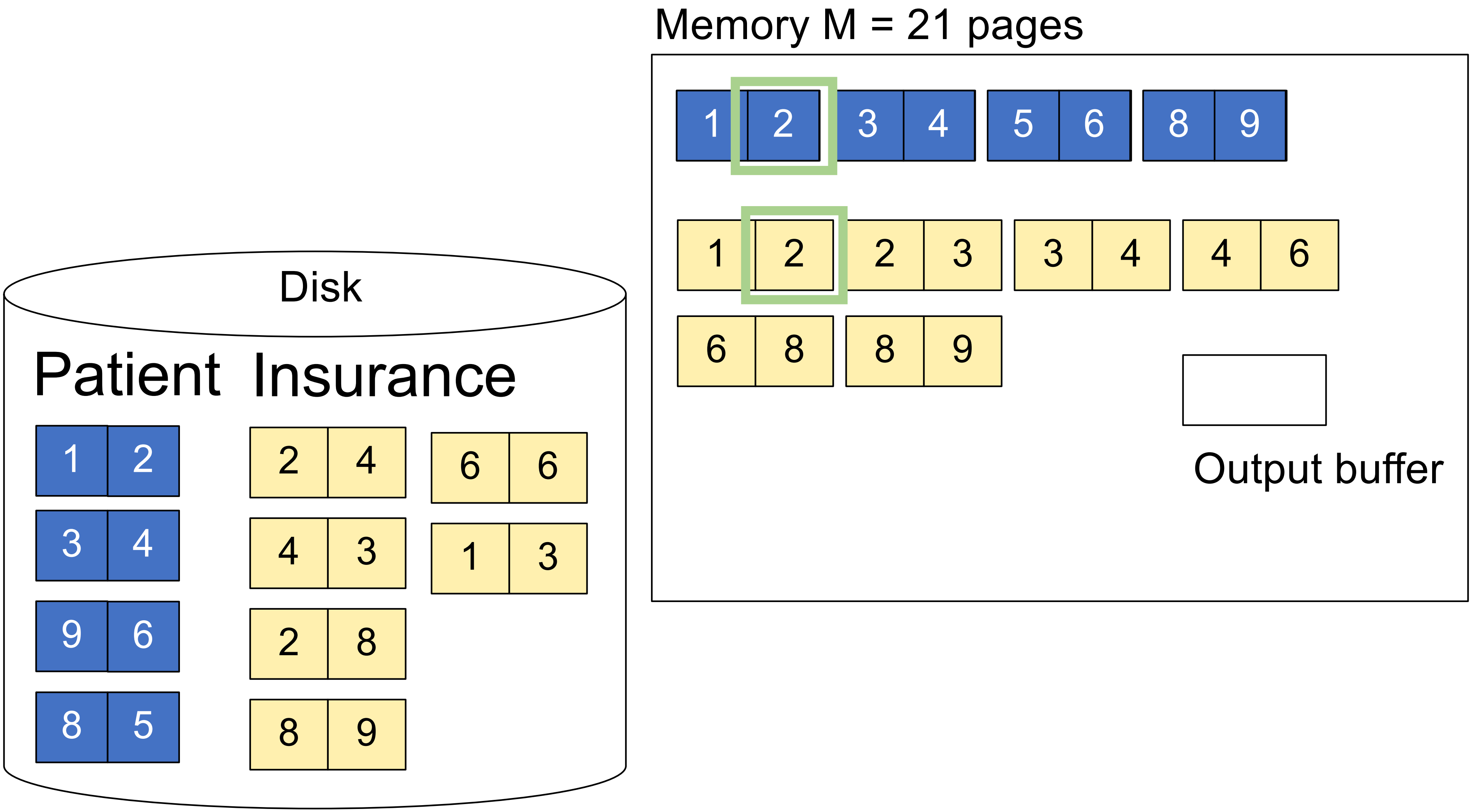

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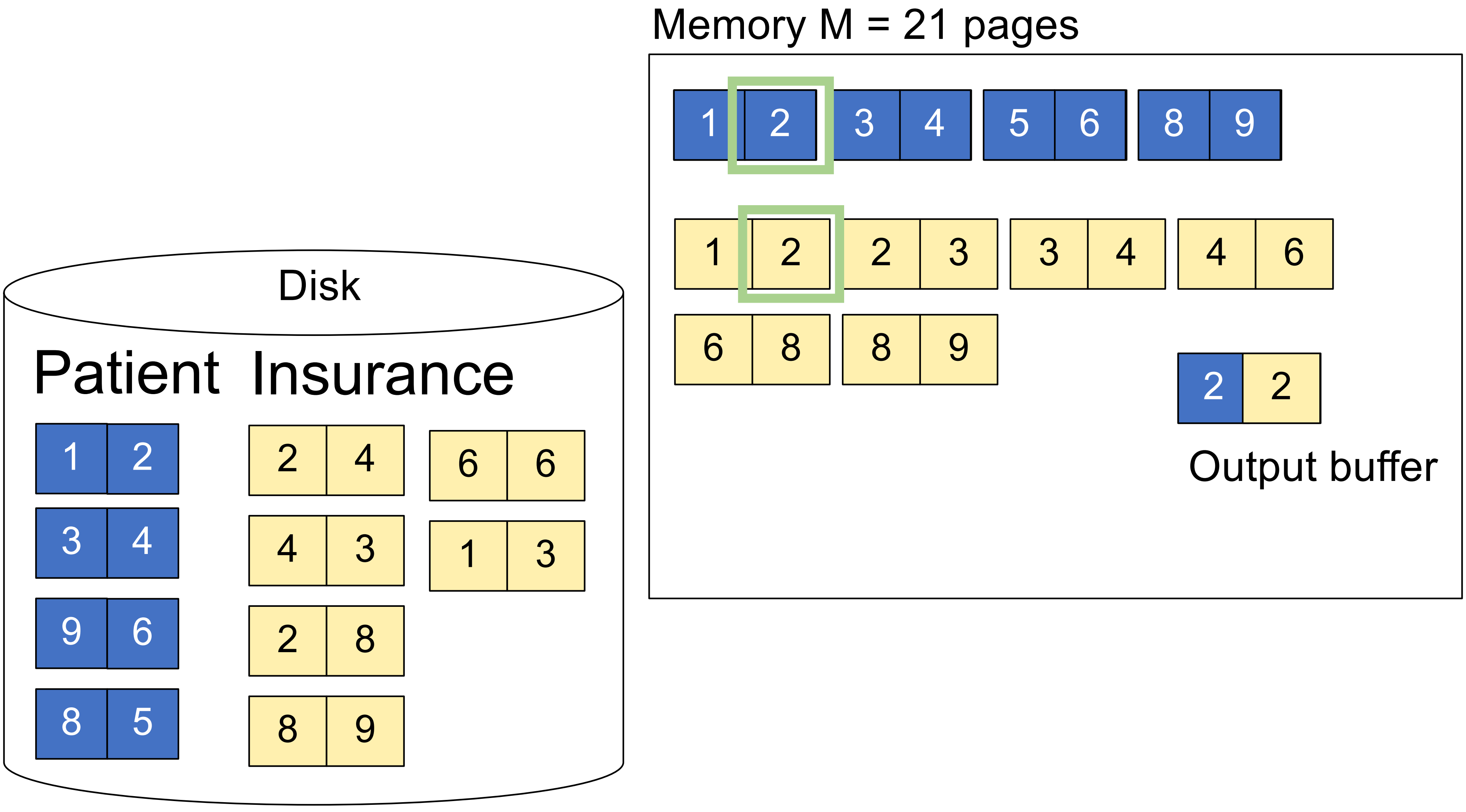

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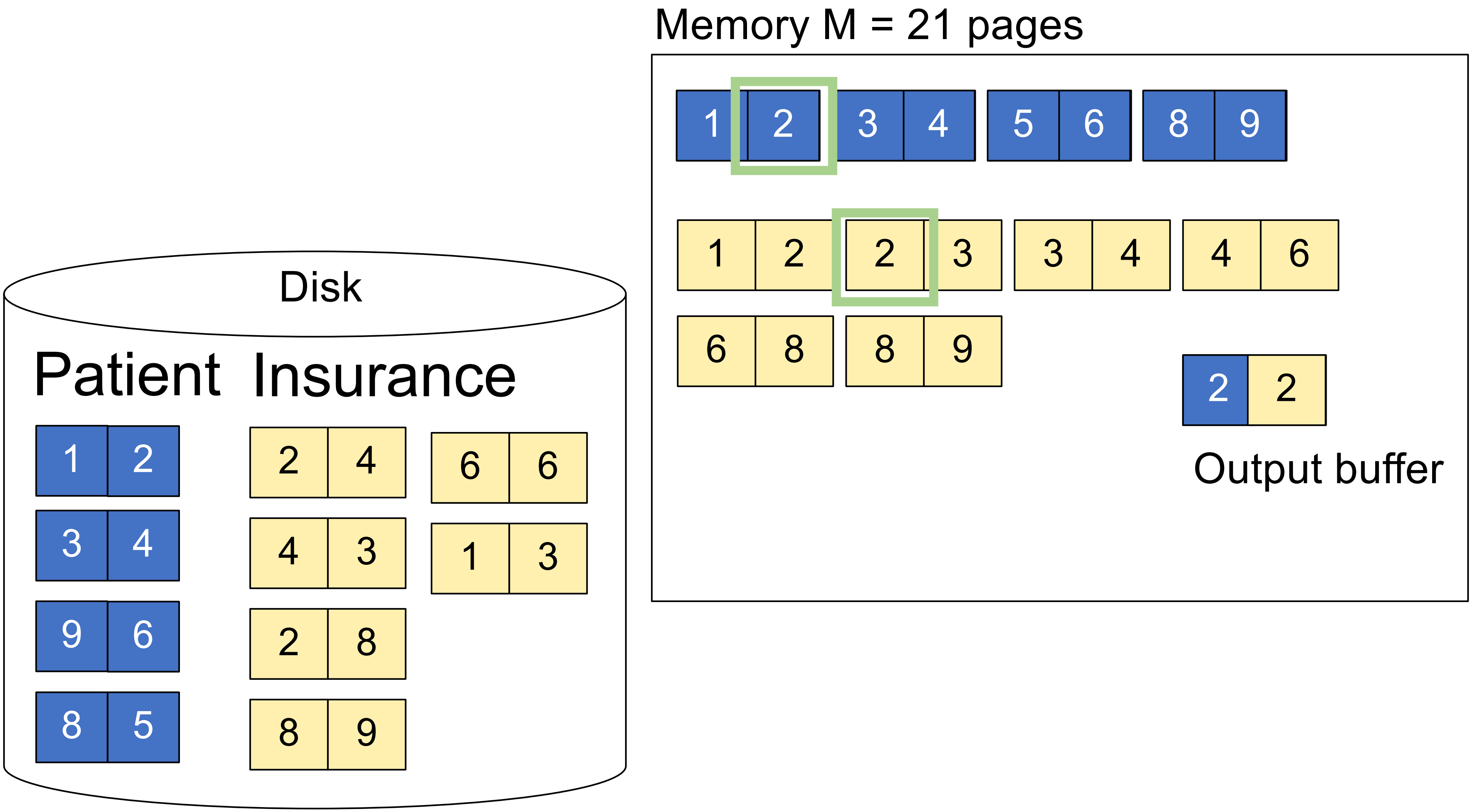

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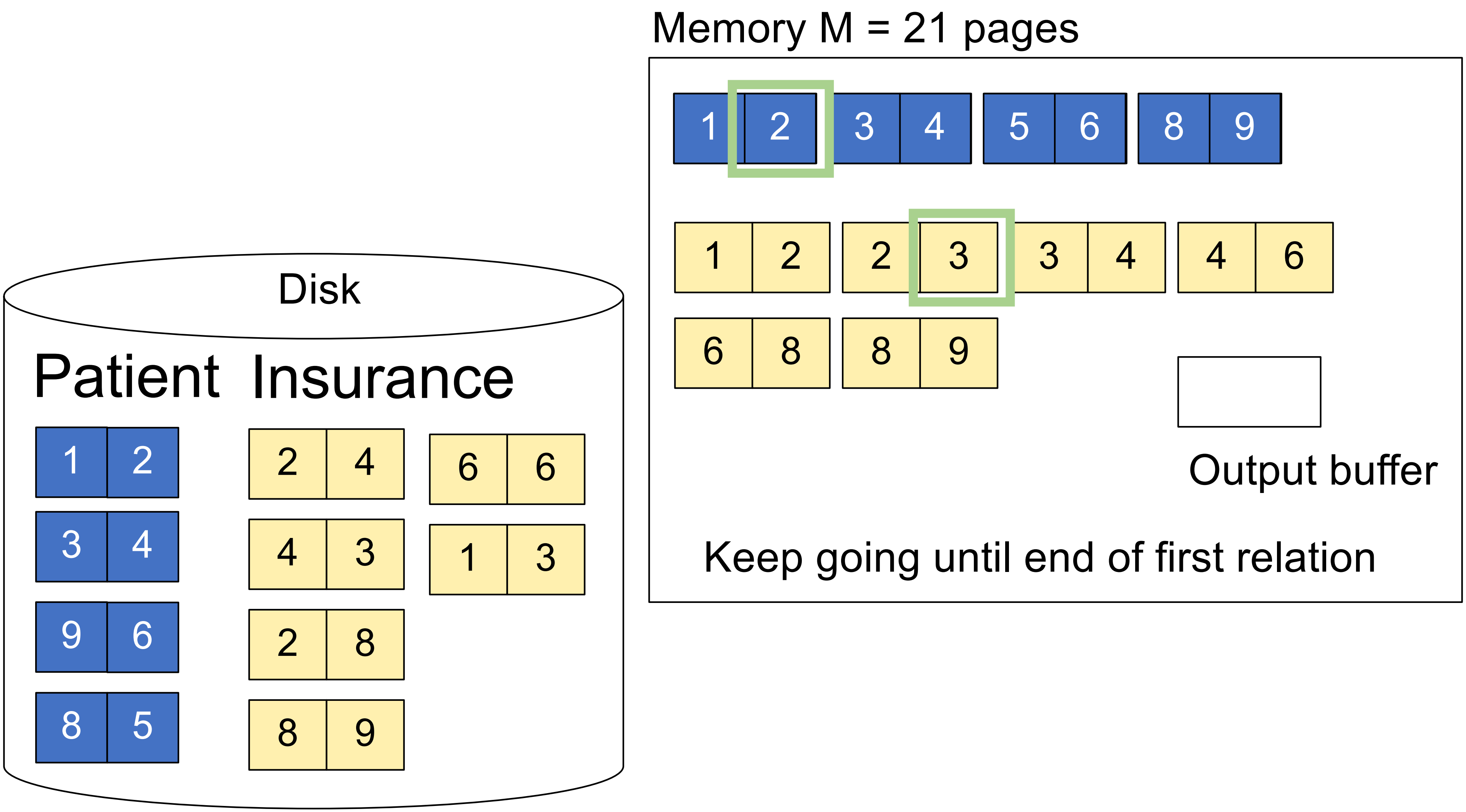

Outline

- **Join operator algorithms**
  - One-pass algorithms (Sec. 15.2 and 15.3)
  - Index-based algorithms (Sec 15.6)
  - Two-pass algorithms (Sec 15.4 and 15.5)

Index Based Selection

Selection on equality: $\sigma_{a=v}(R)$

- $B(R)$= size of R in blocks
- $T(R)$ = number of tuples in R
- $V(R, a)$ = # of distinct values of attribute a

Note: we ignore I/O cost for index pages

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What is the cost in each case?

- Clustered index on a:
- Unclustered index on a:

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Index Based Selection

- Example:

  B(R) = 2000
  T(R) = 100,000
  V(R, a) = 20

  cost of $\sigma_{a=v}(R)$ = ?

- Table scan:
- Index based selection:

Index Based Selection

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B(R) = 2000
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- Index based selection:
  - If index is clustered: B(R)/V(R,a) = 100 I/Os
  - If index is unclustered: T(R)/V(R,a) = 5,000 I/Os

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Lesson: Don't build unclustered indexes when V(R,a) is small !

Index Based Selection

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Lesson: Don't build unclustered indexes when V(R,a) is small !

Index Nested Loop Join

$R \bowtie S$

- Assume S has an index on the join attribute
- Iterate over R, for each tuple fetch corresponding tuple(s) from S

- Previous nested loop join: cost
  - $B(R) + T(R)*B(S)$
- **Index Nested Loop Join Cost**:
  - If index on S is clustered: $B(R) + T(R)B(S)/V(S,a)$
  - If index on S is unclustered: $B(R) + T(R)T(S)/V(S,a)$

Outline

- **Join operator algorithms**
  - One-pass algorithms (Sec. 15.2 and 15.3)
  - Index-based algorithms (Sec 15.6)
  - Two-pass algorithms (Sec 15.4 and 15.5)

Two-Pass Algorithms

- Fastest algorithm seen so far is one-pass hash join
  What if data does not fit in memory?
- Need to process it in multiple passes
- Two key techniques
  - Sorting
  - Hashing

Basic Terminology

- A run in a sequence is an increasing subsequence

- What are the runs?

  2, 4, 99, 103, 88, 77, 3, 79, 100, 2, 50

Basic Terminology

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- What are the runs?

2, 4, 99, 103, | 88, | 77, | 3, 79, 100, | 2, 50

External Merge-Sort: Step 1

Phase one: load M blocks in memory, sort, send to disk, repeat

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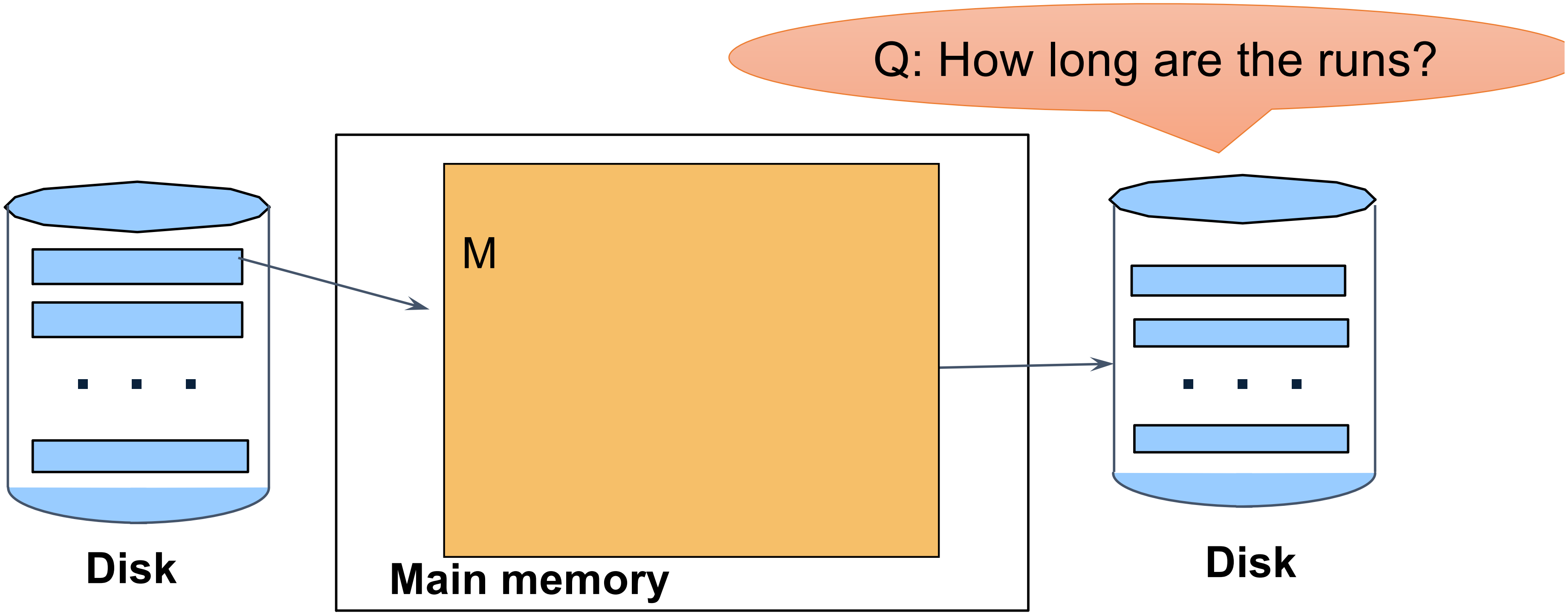
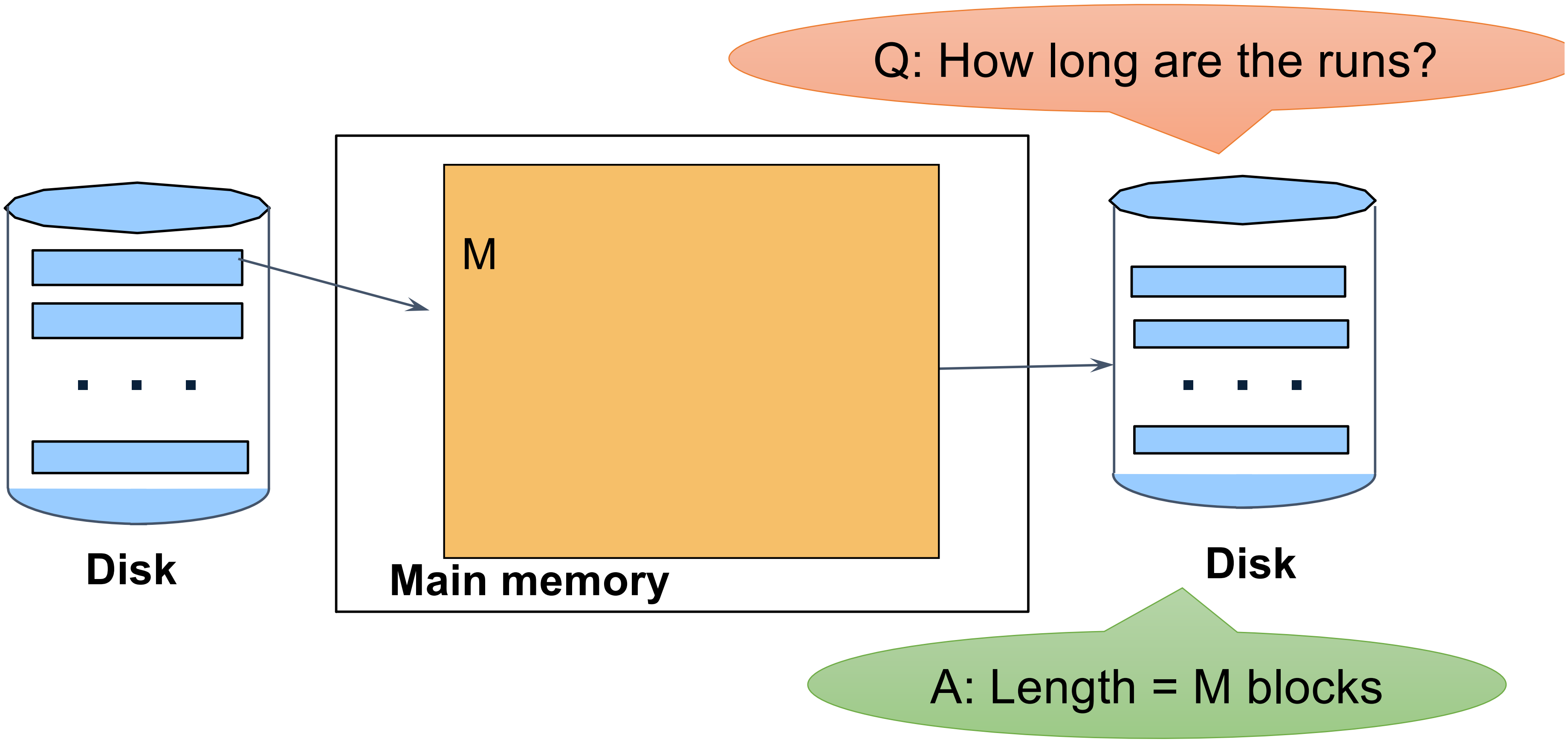


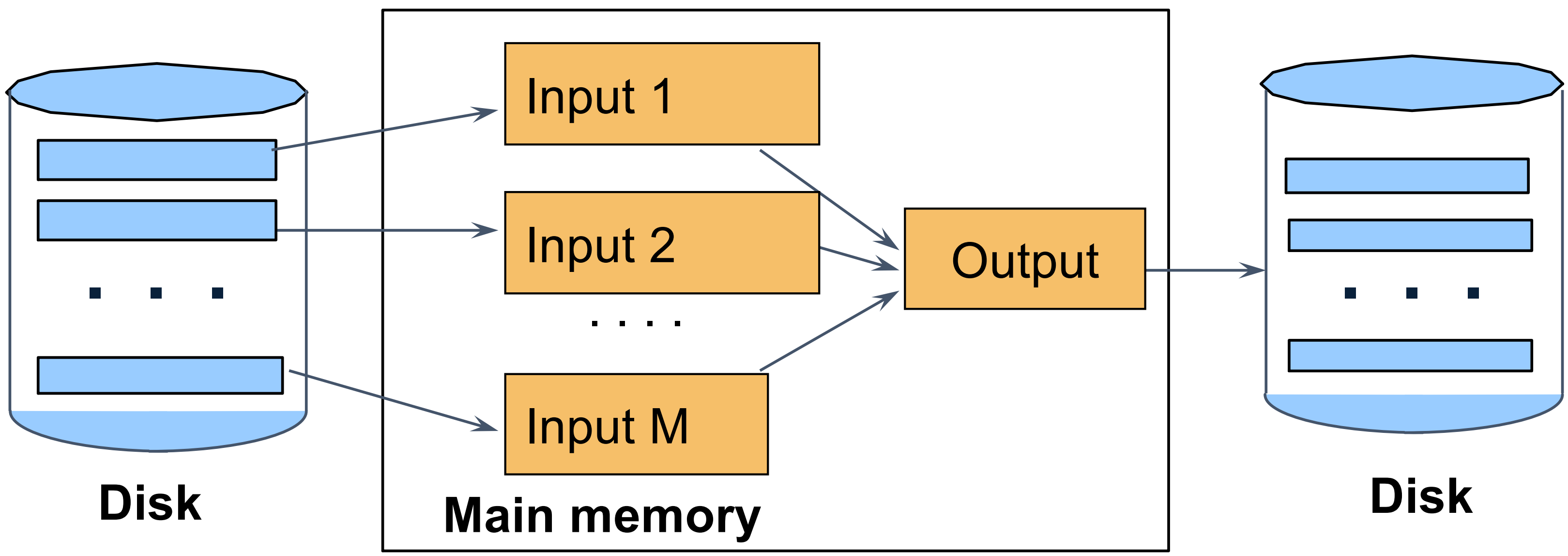
External Merge-Sort: Step 1

Phase one: load M blocks in memory, sort, send to disk, repeat



Phase two: merge M runs into a bigger run

- Merge M – 1 runs into a new run
- Result: runs of length M (M – 1) ≈ M^2



Example

- Merging three runs to produce a longer run:

0, 14, 33, 88, 92, 192, 322
2, 4, 7, 43, 78, 103, 523
1, 6, 9, 12, 33, 52, 88, 320

Output:
0

Example

- Merging three runs to produce a longer run:

0, **14, 33, 88, 92, 192, 322**
2, 4, 7, 43, 78, 103, 523
1, 6, 9, 12, 33, 52, 88, 320

Output:
0, ?

Example

- Merging three runs to produce a longer run:

0, **14, 33, 88, 92, 192, 322**
2, 4, 7, 43, 78, 103, 523
1, **6, 9, 12, 33, 52, 88, 320**

Output:
0, 1, ?

Example

- Merging three runs to produce a longer run:

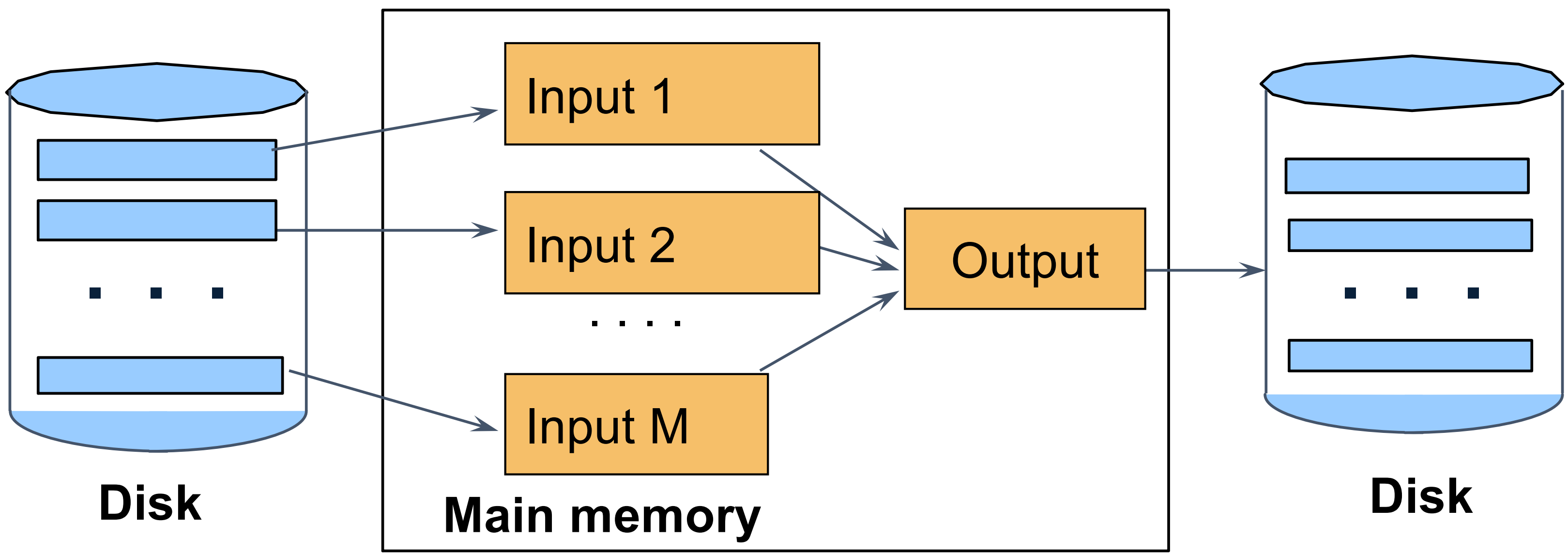
0, **14**, **33, 88, 92, 192, 322**
2, 4, 7, **43**, **78, 103, 523**
1, 6, **9**, **12, 33, 52, 88, 320**

Output:
0, 1, 2, 4, 6, 7, ?

External Merge-Sort: Step 2

Phase two: merge M runs into a bigger run

- Merge M – 1 runs into a new run
- Result: runs of length M (M – 1) ≈ M^2



If approx. B <= M^2 then we are done

Cost of External Merge Sort

- Assumption: $B(R) <= M^2$
- Read+write+read = $3B(R)$

Discussion

- What does $B(R) <= M^2$ mean?
- How large can R be?

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- How large can R be?

- Example:
  - Page size = 32KB
  - Memory size 32GB: $M = 10^6$-pages

Discussion

- What does $B(R) <= M^2$ mean?
- How large can R be?

- Example:
  - Page size = 32KB
  - Memory size 32GB: $M = 10^6$ pages

- R can be as large as 10^{12} pages
  - 32×10^{15} Bytes = 32 PB

Merge-Join

Join R $\bowtie$ S

- How?....

Merge-Join

Join R $\bowtie$ S

- Step 1a: generate initial runs for R
- Step 1b: generate initial runs for S
- Step 2: merge and join
  - Either merge first and then join
  - Or merge & join at the same time

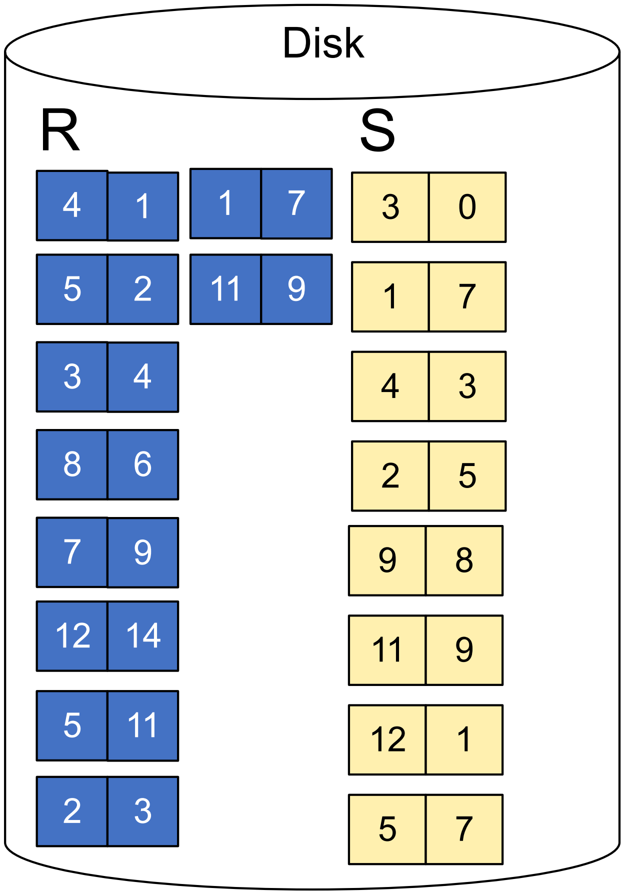
Merge-Join Example

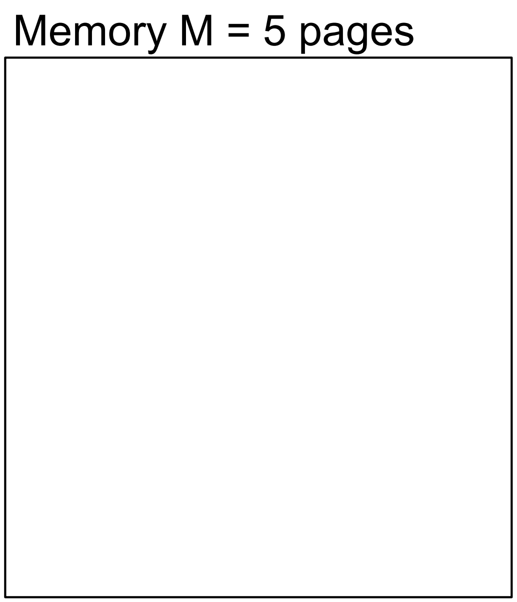
Setup: Want to join R and S

Relation R has 10 pages with 2 tuples per page

Relation S has 8 pages with 2 tuples per page

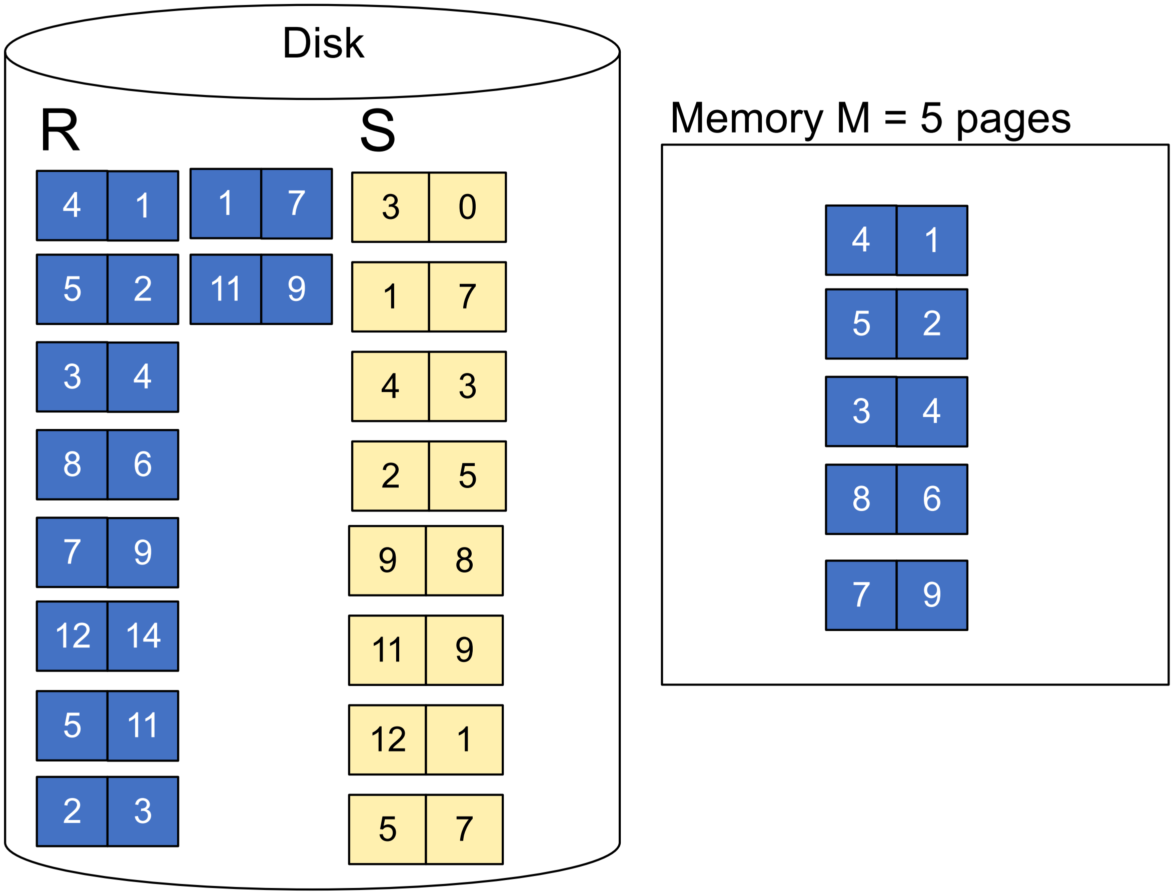
Values shown are values of join attribute for each given tuple





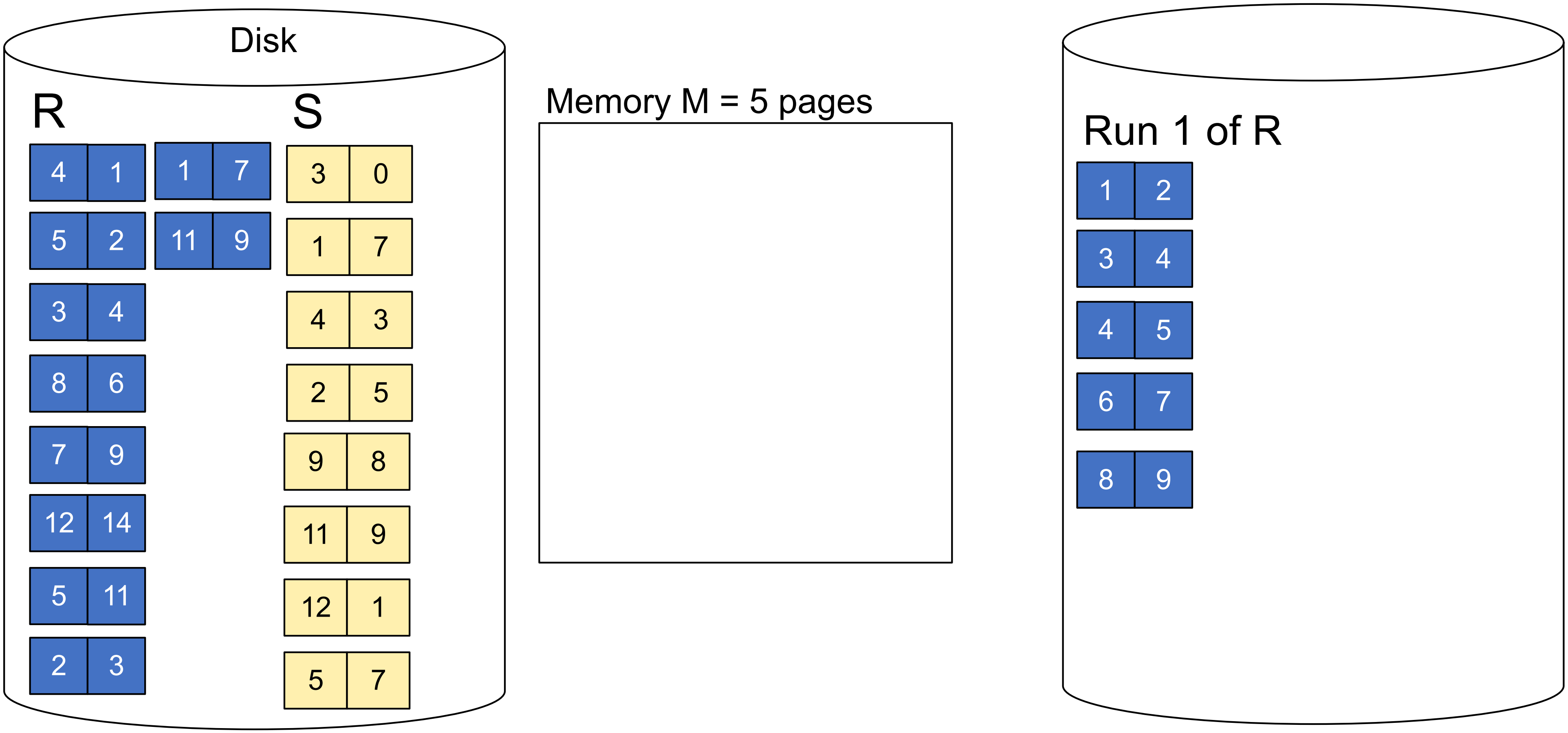
Merge-Join Example

Step 1: Read M pages of R and sort in memory



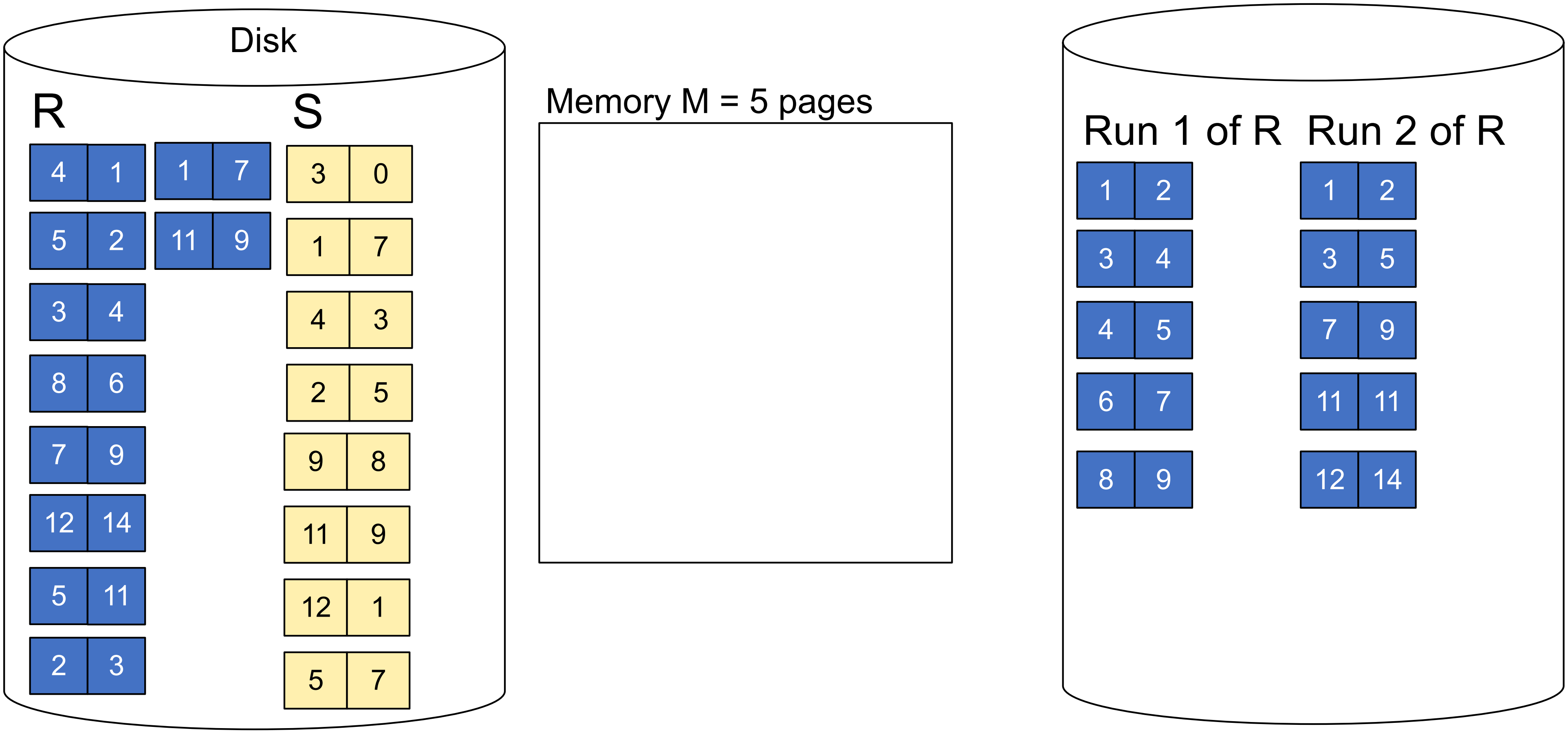
Merge-Join Example

Step 1: Read M pages of R and sort in memory, then write to disk



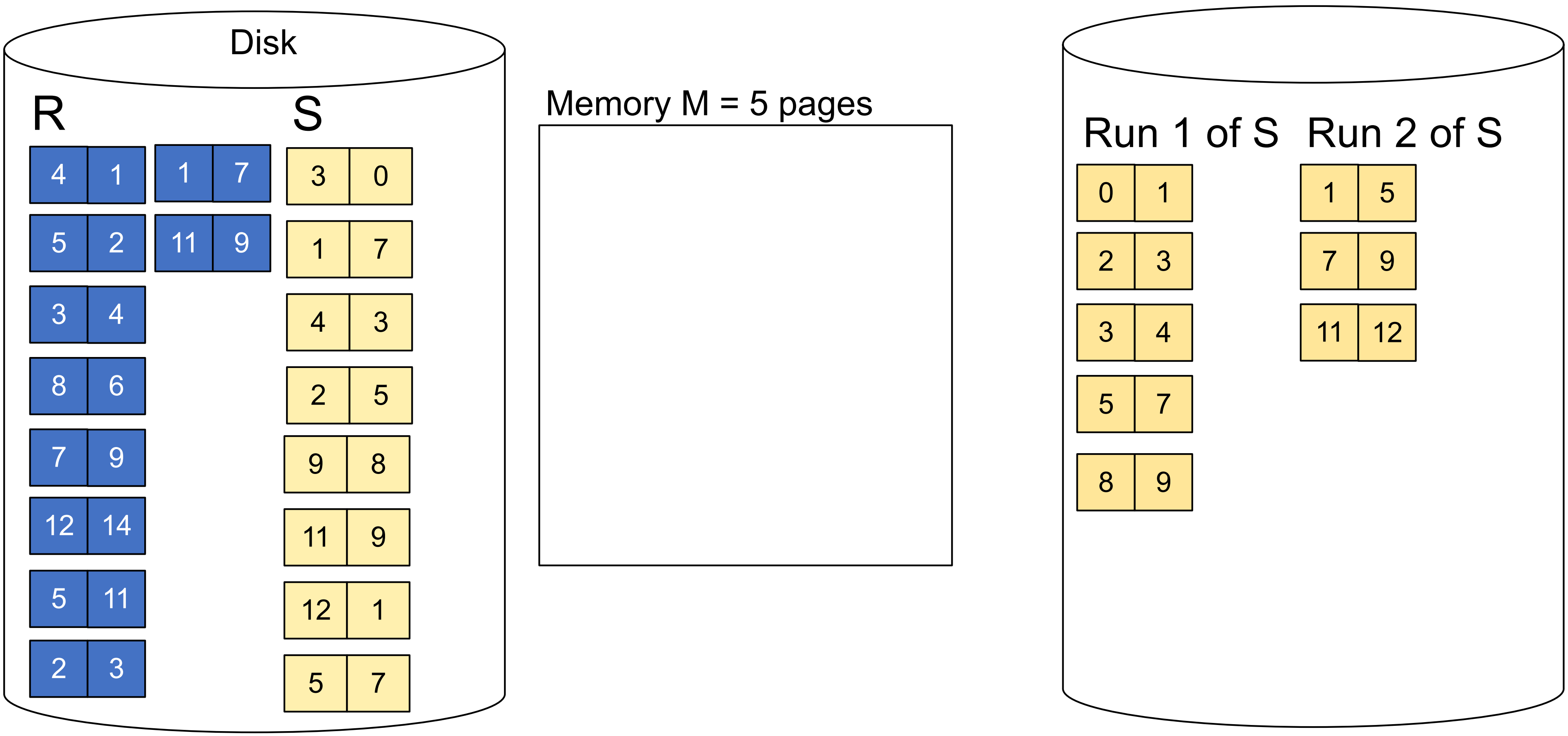
Merge-Join Example

Step 1: Repeat for next M pages until all R is processed



Merge-Join Example

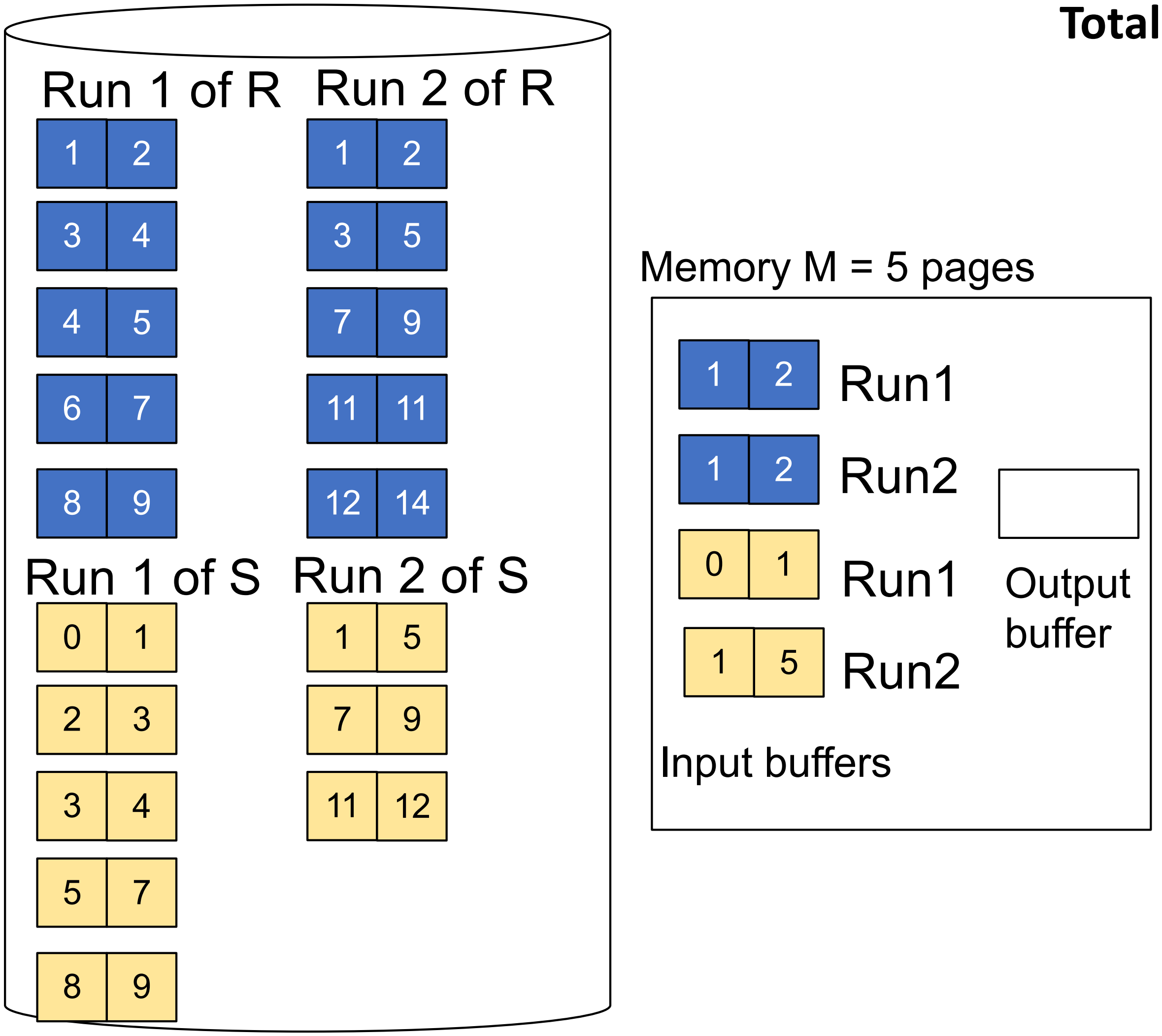
Step 1: Do the same with S



Merge-Join Example

Step 2: Join while merging sorted runs

Total cost: 3B(R) + 3B(S)

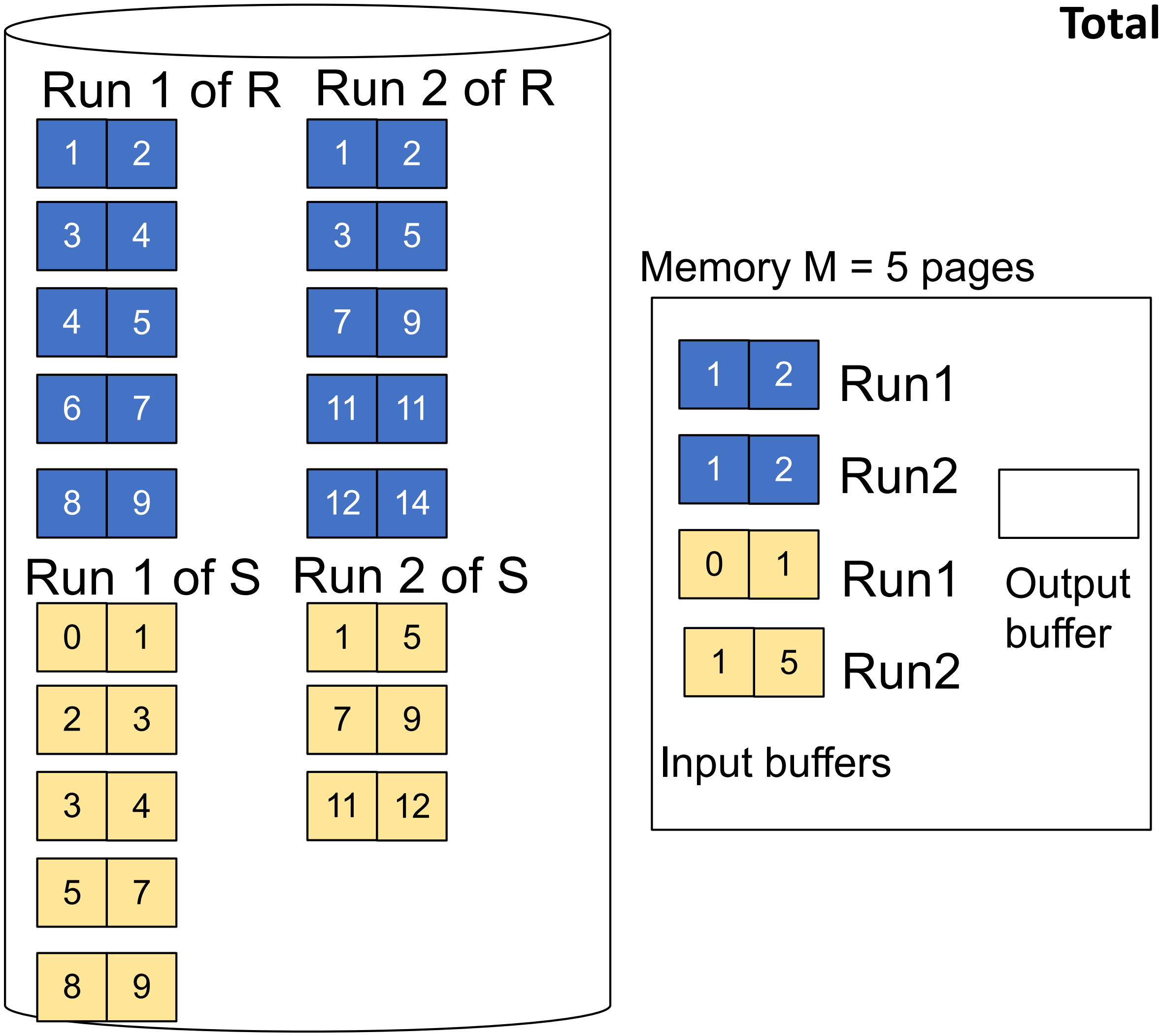


Step 2: Join while merging

Output tuples

Merge-Join Example

Step 2: Join while merging sorted runs



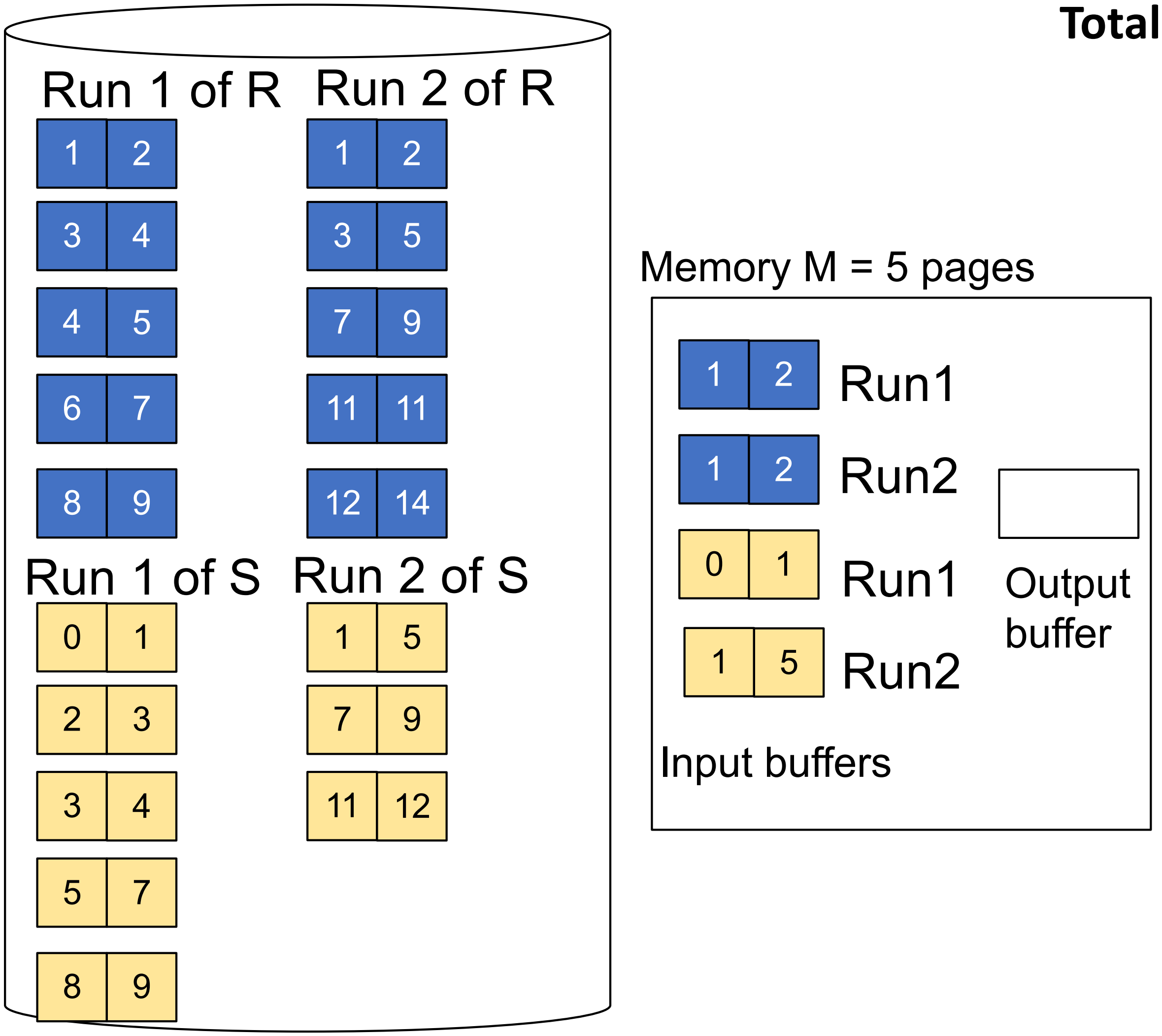
Total cost: 3B(R) + 3B(S)

Step 2: Join while merging
Output tuples

Merge-Join Example

Step 2: Join while merging sorted runs

Total cost: 3B(R) + 3B(S)

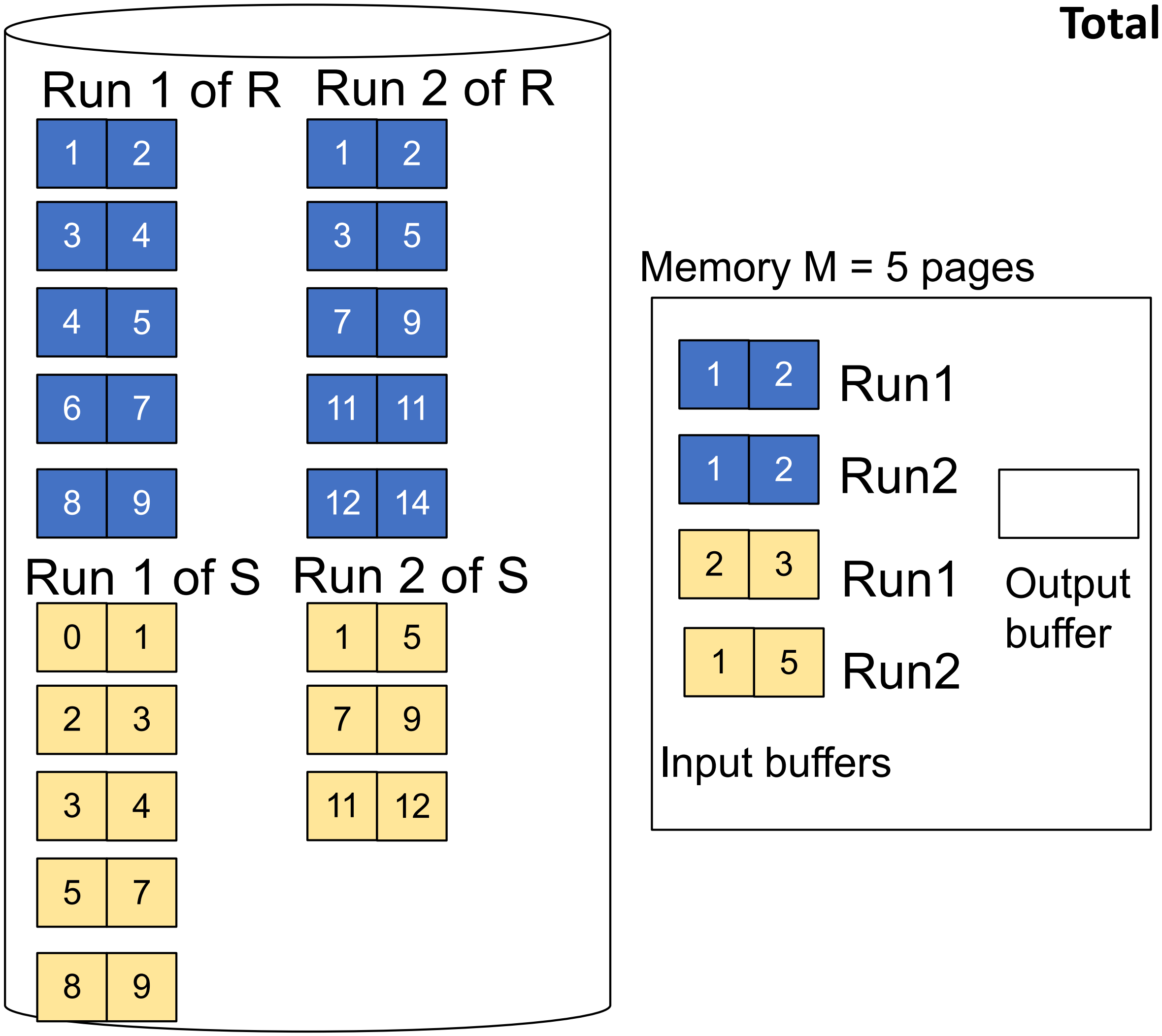


Step 2: Join while merging
Output tuples
(1,1)
(1,1)
(1,1)
(1,1)

Merge-Join Example

Step 2: Join while merging sorted runs

Total cost: 3B(R) + 3B(S)



Step 2: Join while merging

Output tuples

(1,1)

(1,1)

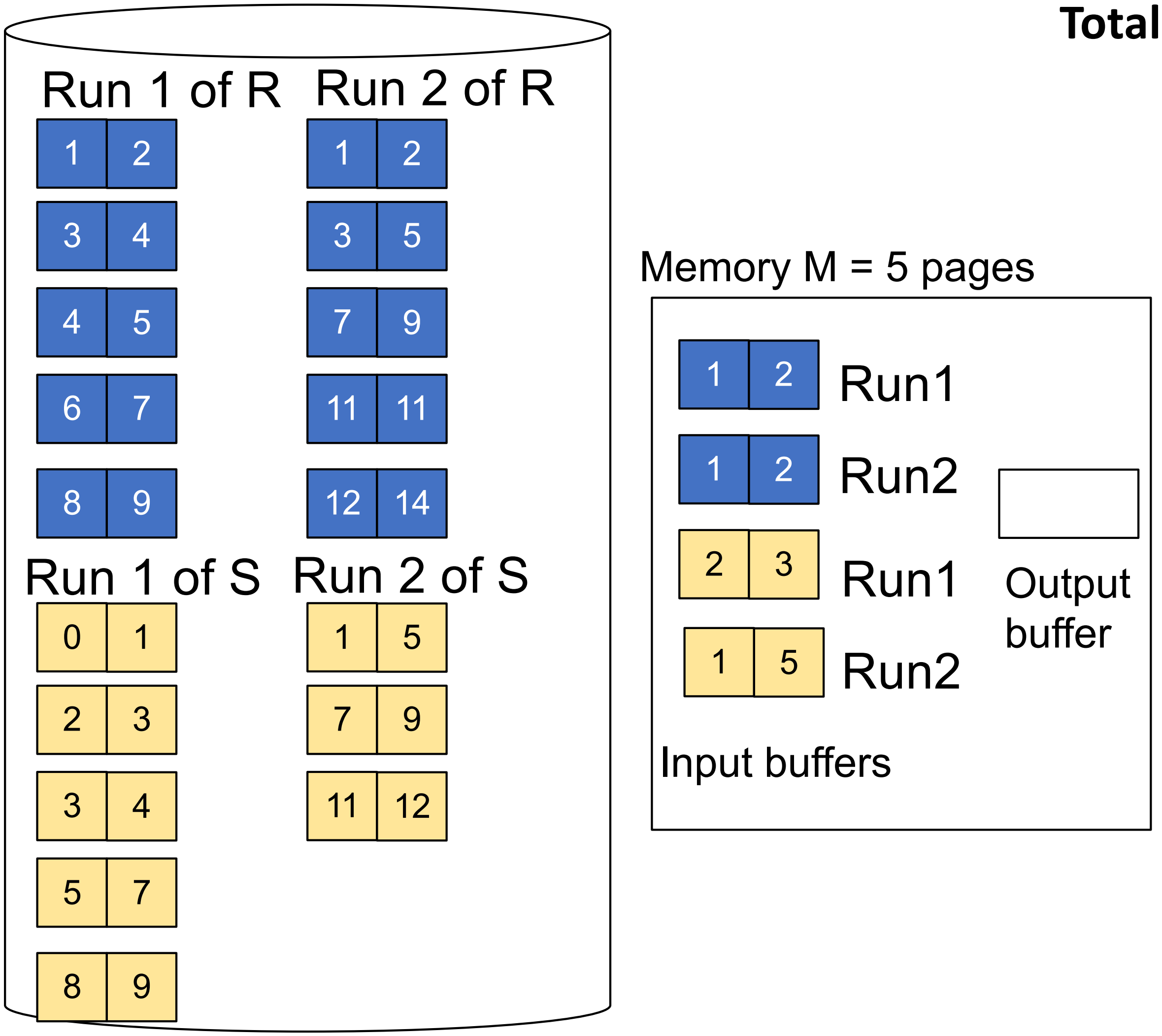
(1,1)

(1,1)

Merge-Join Example

Step 2: Join while merging sorted runs

Total cost: 3B(R) + 3B(S)



Step 2: Join while merging

Output tuples

(1,1)

(1,1)

(1,1)

(1,1)

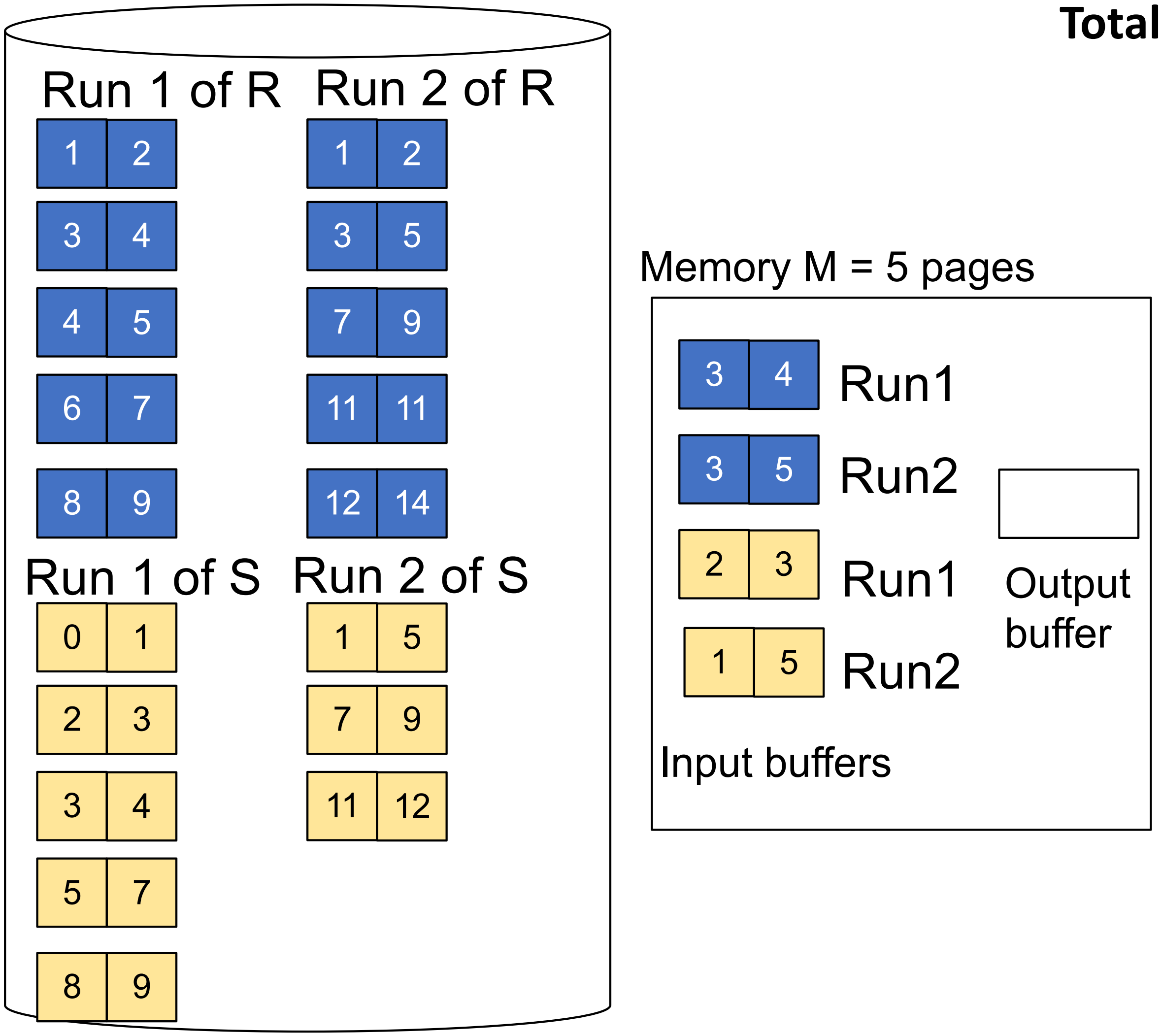
(2,2)

(2,2)

Merge-Join Example

Step 2: Join while merging sorted runs

Total cost: 3B(R) + 3B(S)



Step 2: Join while merging

Output tuples

(1,1)

(1,1)

(1,1)

(1,1)

(2,2)

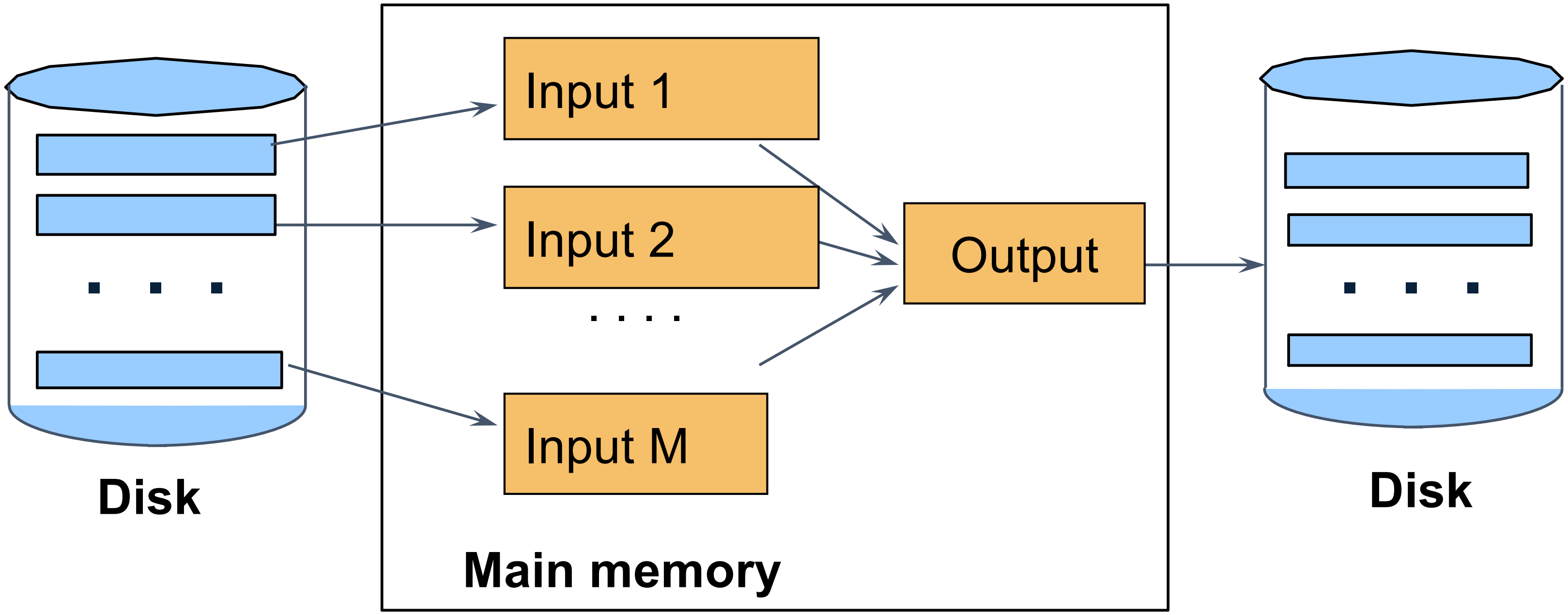
(2,2)

(3,3)

(3,3)

...

Merge-Join



$M_1 = B(R)/M$ runs for R
$M_2 = B(S)/M$ runs for S
Merge-join $M_1 + M_2$ runs;
need $M_1 + M_2 <= M$ to process all runs
i.e. $B(R) + B(S) <= M^2$