

# Database System Internals

## Query Optimization (part 3)

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# Selinger Optimizer History

- 1960's: first database systems
  - Use tree and graph data models
- 1970: Ted Codd proposes relational model
  - E.F. Codd. A relational model of data for large shared data banks. Communications of the ACM, 1970
- 1974: System R from IBM Research
  - One of first systems to implement relational model
- 1979: Seminal query optimizer paper by P. Selinger et. al.
  - Invented cost-based query optimization
  - Dynamic programming algorithm for join order computation

# References

- P. Selinger, M. Astrahan, D. Chamberlin, R. Lorie, and T. Price. Access Path Selection in a Relational Database Management System. Proceedings of ACM SIGMOD, **1979**. Pages 22-34.

# Selinger Algorithm

Selinger enumeration algorithm considers

- Different logical and physical plans *at the same time*
- Cost of a plan is IO + CPU
- Concept of *interesting order* during plan enumeration
  - A *sorted order* as that requested by ORDER BY or GROUP BY
  - Or order on attributes that appear in equi-join predicates
    - Because they may enable cheaper sort-merge joins later

# More about the Selinger Algorithm

- Step 1: Enumerate all access paths for a single relation
  - File scan or index scan
  - Keep the cheapest for each *interesting order*
- Step 2: Consider all ways to join two relations
  - Use result from step 1 as the outer relation
  - Consider every other possible relation as inner relation
  - Estimate cost when using sort-merge or nested-loop join
  - Keep the cheapest for each *interesting order*
- Steps 3 and later: Repeat for three relations, etc.

# Example From Selinger Paper

**EMP**

NAME	DNO	JOB	SAL
SMITH	50	12	8500
JONES	50	5	15000
DOE	51	5	9500

**DEPT**

DNO	DNAME	LOC
50	MFG	DENVER
51	BILLING	BOULDER
52	SHIPPING	DENVER

**JOB**

JOB	TITLE
5	CLERK
6	TYPIST
8	SALES
12	MECHANIC

```
SELECT  NAME, TITLE, SAL, DNAME
FROM    EMP, DEPT, JOB
WHERE   TITLE = 'CLERK'
AND     LOC = 'DENVER'
AND     EMP.DNO = DEPT.DNO
AND     EMP.JOB = JOB.JOB
```

“Retrieve the name, salary, job title, and department name of employees who are clerks and work for departments in Denver.”

Figure 1. JOIN example

# Step1: Access Path Selection for Single Relations

- Eligible Predicates: Local Predicates Only
- “Interesting” Orderings: DNO, JOB

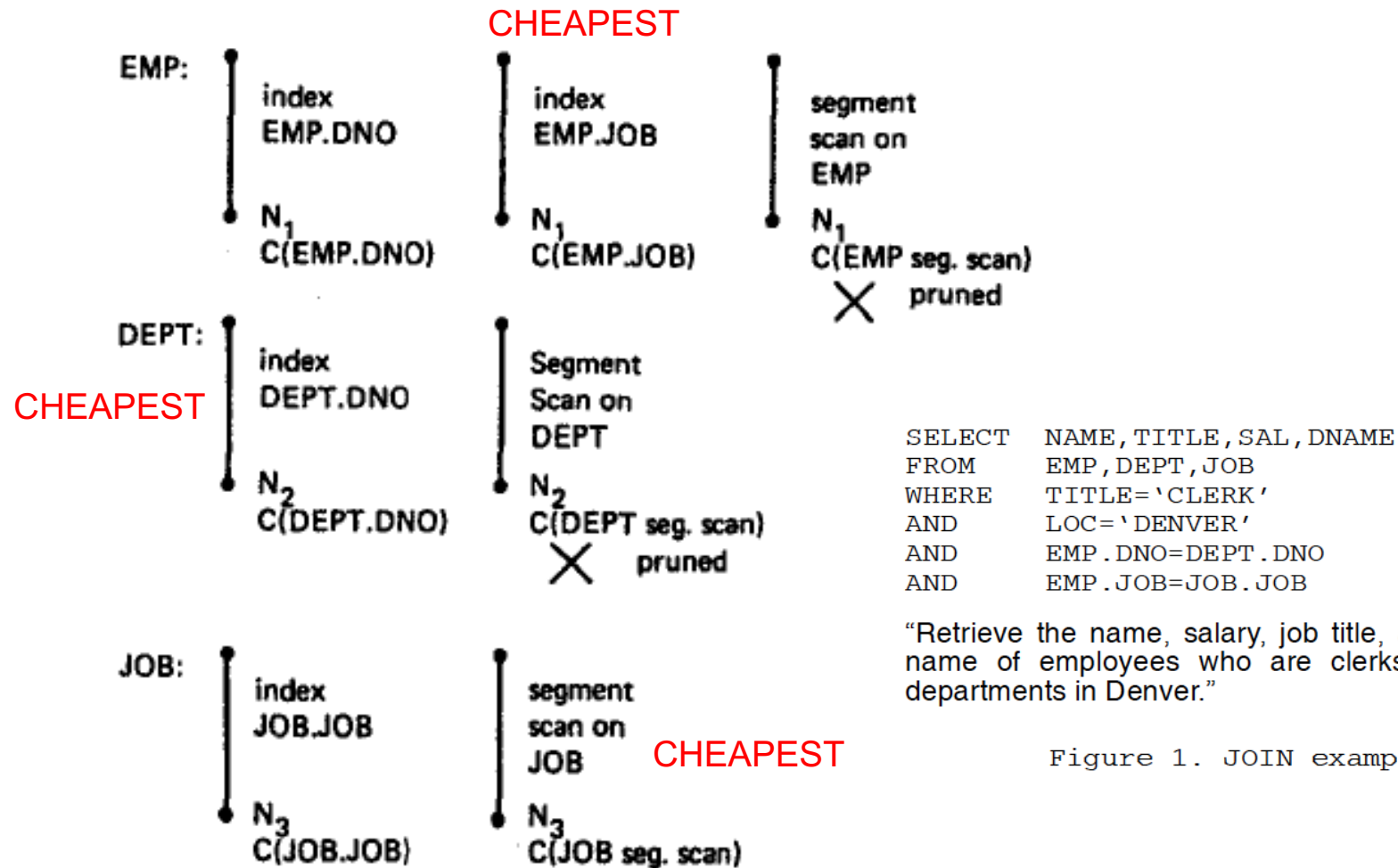
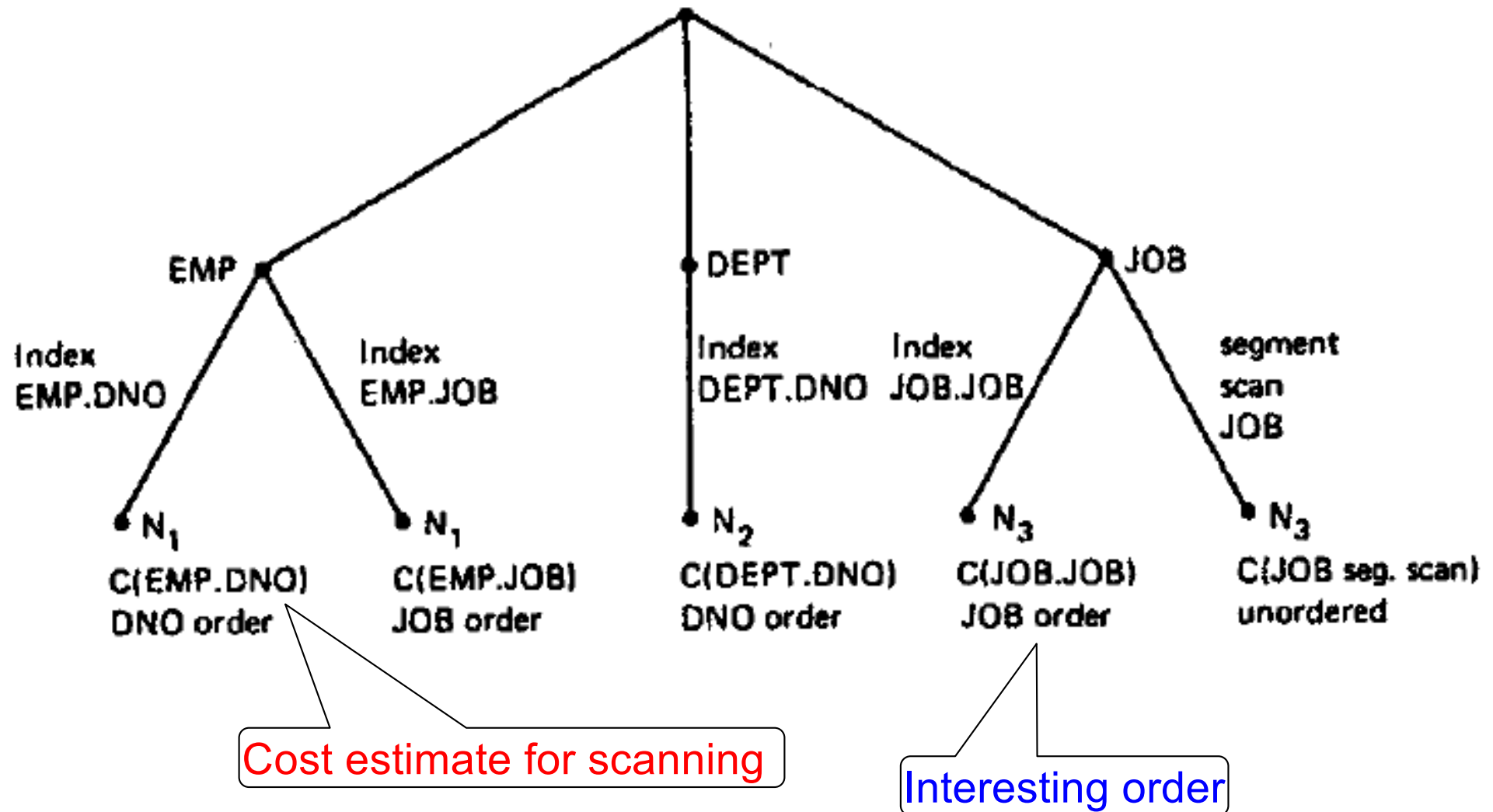


Figure 1. JOIN example

```
SELECT NAME, TITLE, SAL, DNAME
FROM EMP, DEPT, JOB
WHERE TITLE='CLERK' AND LOC='DENVER' AND EMP.DNO=DEPT.DNO AND EMP.JOB=JOB.JOB
```

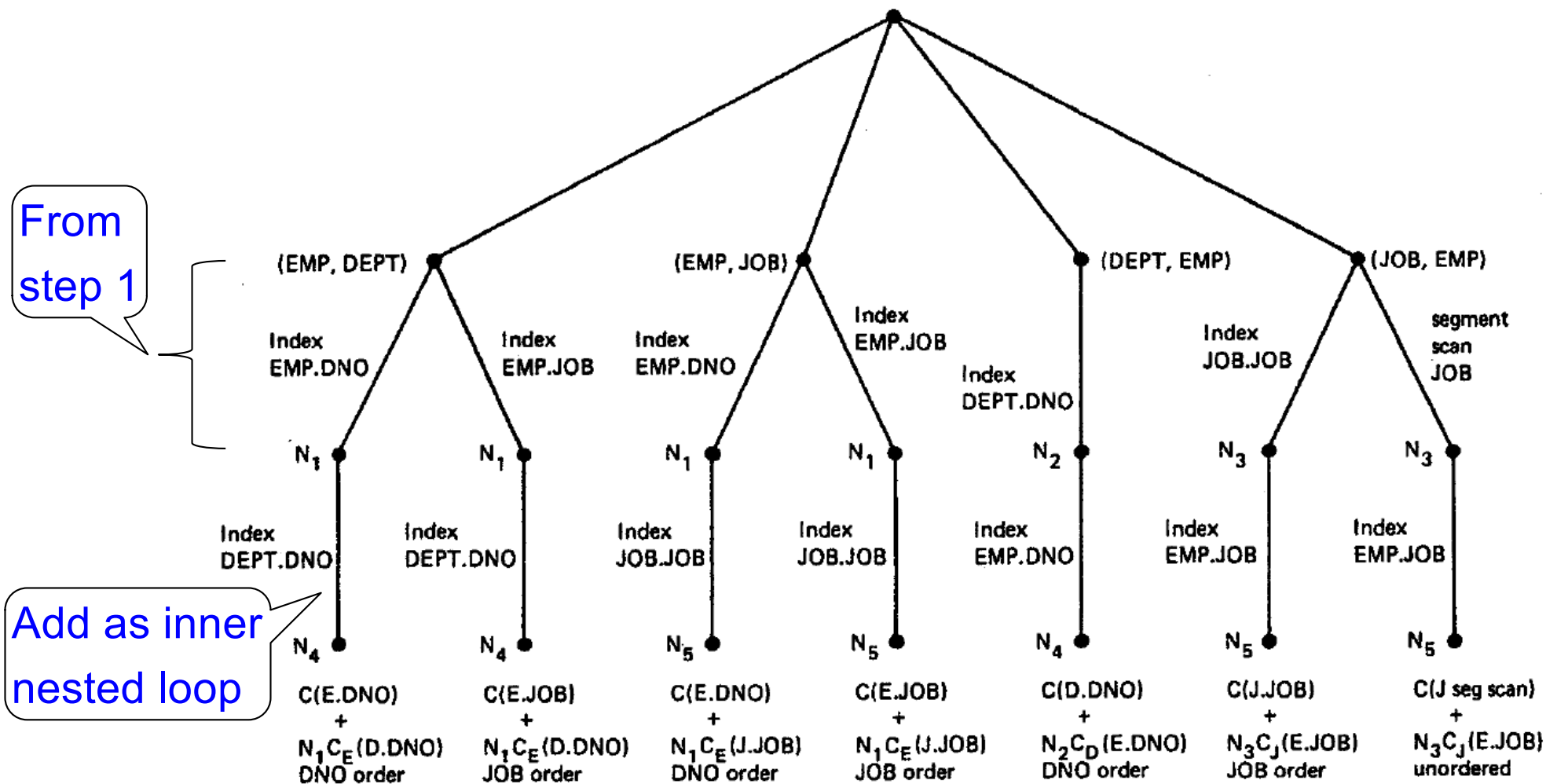
# Step1: Resulting Plan Search Tree for Single Relations



**SELECT** NAME, TITLE, SAL, DNAME  
**FROM** EMP, DEPT, JOB  
**WHERE** TITLE='CLERK' AND LOC='DENVER' AND EMP.DNO=DEPT.DNO AND EMP.JOB=JOB.JOB



## Step2: Pairs of Relations (nested loop joins)

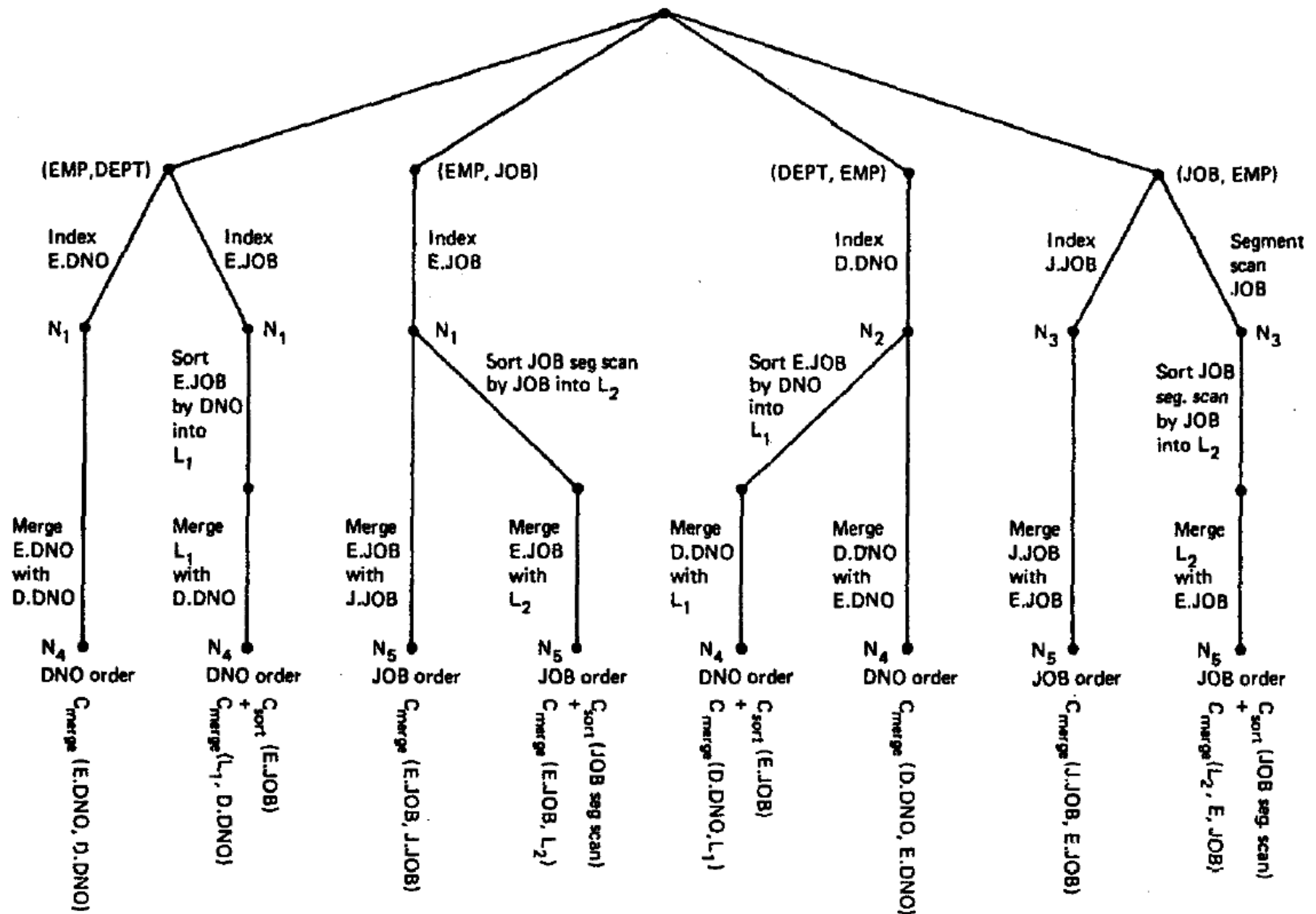


**SELECT** NAME, TITLE, SAL, DNAME

**FROM** EMP, DEPT, JOB

**WHERE** TITLE='CLERK' AND LOC='DENVER' AND EMP.DNO=DEPT.DNO AND EMP.JOB=JOB.JOB

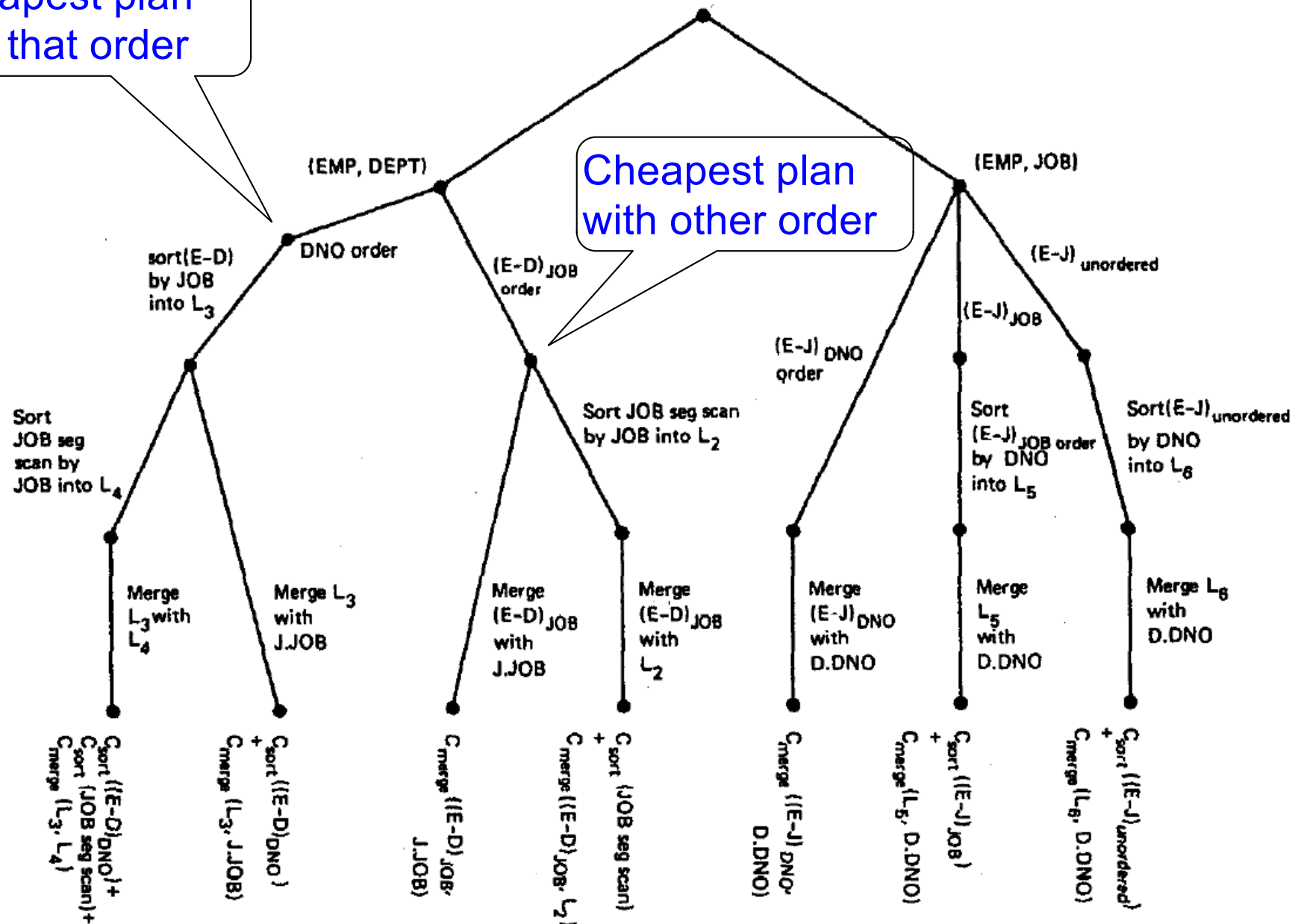
## Step2: Pairs of Relations (sort-merge joins)



# Step3:Add Third Relation (sort-merge join)

Cheapest plan with that order

Cheapest plan with other order



# Selinger Optimizer

## Problem:

- How to order a series of joins over N tables A,B,C,...

E.g.  $A.a = B.b$  AND  $A.c = D.d$  AND  $B.e = C.f$

- $N!$  ways to order joins; e.g. ABCD, ACBD, ....

- $$C_{N-1} = \frac{1}{N} \binom{2(N-1)}{N-1}$$

plans/ordering; e.g.

$((AB)C)D, ((AB)(CD))$

- Multiple implementations (hash, nested loops)
- Naïve approach does not scale
  - E.g.  $N = 20$ , #join orders  $20! = 2.4 \times 10^{18}$ ; many more plans

# Selinger Optimizer

- Only **left-deep plan**:  $((AB)C)D$  – eliminate  $C_{N-1}$ .
  - In SimpleDB, we consider all linear plans, not only left-deep.
- Push down selections
- Don't consider cartesian products
- Dynamic programming algorithm

# Next Example Acks

Implement variant of Selinger optimizer in SimpleDB

Designed to help you understand how this would work in SimpleDB

Many following slides from Sam Madden at MIT

# SimpleDBs Optimizer

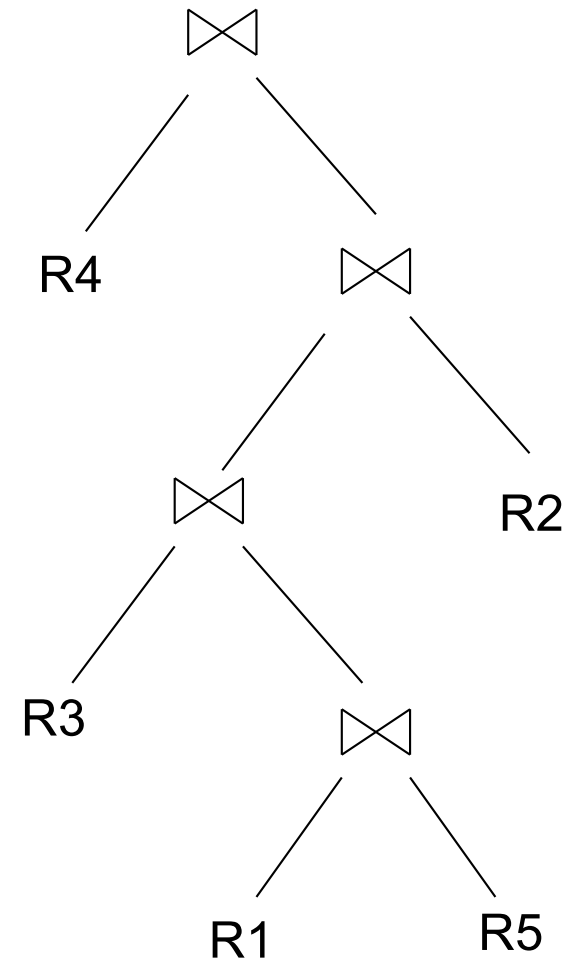
Exists within JoinOptimizer.java

In all the beginning labs, there is no optimization!

The relevant parts of JoinOptimizer are empty

One major difference in SimpleDB compared to Selinger optimizer:

We consider **linear trees**, not left-deep only



# Dynamic Programming

OrderJoins(...):

R = set of relations to join

For d = 1 to N: /\* where N = |R| \*/

For S in {all size-d subsets of R}:

**optjoin**(S) = (S - a) join a,

where a is the single relation that minimizes:

cost(**optjoin**(S - a)) +  
min.cost to join (S - a) with a +  
min.access cost for a

SimpleDB Lab5:  
you implement **orderJoins**

Use: **enumerateSubsets**

Use:  
**computeCostAndCardOfSubplan**

Note: **optjoin**(S-a) is cached from previous iterations



# Example

- **orderJoins(A, B, C, D)**
- Assume all joins are Nested Loop

Subplan S	optJoin(S)	Cost(OptJoin(S))
A		

# Example

- **orderJoins(A, B, C, D)**
- Assume all joins are NL
- $d = 1$ 
  - A = best way to access A (sequential scan, predicate-pushdown on index, etc)
  - B = best way to access B
  - C = best way to access C
  - D = best way to access D
- Total number of steps:  
**choose(N, 1)**

Subplan S	optJoin(S)	Cost(OptJoin(S))
A	Index scan	100
B	Seq. scan	50
C	Seq scan	120
D	B+tree scan	400

# Example

- **orderJoins(A, B, C, D)**
- $d = 2$ 
  - $\{A, B\} = AB$  or  $BA$   
use previously computed  
best way to access A and B

Subplan S	optJoin(S)	Cost(OptJoin(S))
A	Index scan	100
B	Seq. scan	50
...		

# Example

- **orderJoins(A, B, C, D)**
- $d = 2$ 
  - $\{A, B\} = AB$  or  $BA$   
use previously computed  
best way to access A and B

Subplan S	optJoin(S)	Cost(OptJoin(S))
A	Index scan	100
B	Seq. scan	50
...		
{A, B}	BA	156

# Example

- **orderJoins(A, B, C, D)**
- $d = 2$ 
  - $\{A, B\} = AB$  or  $BA$   
use previously computed  
best way to access A and B
  - $\{B, C\} = BC$  or  $CB$

Subplan S	optJoin(S)	Cost(OptJoin(S))
A	Index scan	100
B	Seq. scan	50
...		
{A, B}	BA	156
{B, C}	BC	98

# Example

## ▪ **orderJoins(A, B, C, D)**

### ▪ $d = 2$

- $\{A, B\} = AB$  or  $BA$   
use previously computed  
best way to access A and B
- $\{B, C\} = BC$  or  $CB$

Subplan S	optJoin(S)	Cost(OptJoin(S))
A	Index scan	100
B	Seq. scan	50
...		
$\{A, B\}$	BA	156
$\{B, C\}$	BC	98

# Example

## ▪ **orderJoins(A, B, C, D)**

### ▪ $d = 2$

- $\{A, B\} = AB$  or  $BA$   
use previously computed  
best way to access A and B
- $\{B, C\} = BC$  or  $CB$
- $\{C, D\} = CD$  or  $DC$
- $\{A, C\} = AC$  or  $CA$
- $\{B, D\} = BD$  or  $DB$
- $\{A, D\} = AD$  or  $DA$

Subplan S	optJoin(S)	Cost(OptJoin(S))
A	Index scan	100
B	Seq. scan	50
...		
$\{A, B\}$	BA	156
$\{B, C\}$	BC	98
.....		

# Example

## ▪ **orderJoins(A, B, C, D)**

### ▪ $d = 2$

- $\{A, B\} = AB$  or  $BA$   
use previously computed  
best way to access A and B

- $\{B, C\} = BC$  or  $CB$
- $\{C, D\} = CD$  or  $DC$
- $\{A, C\} = AC$  or  $CA$
- $\{B, D\} = BD$  or  $DB$
- $\{A, D\} = AD$  or  $DA$

Subplan S	optJoin(S)	Cost(OptJoin(S))
A	Index scan	100
B	Seq. scan	50
...		
$\{A, B\}$	BA	156
$\{B, C\}$	BC	98
.....		

### ▪ Total number of steps: $\text{choose}(N, 2) \times 2$



# Example

- **orderJoins(A, B, C, D)**

- $d = 3$

- $\{A, B, C\} =$   
Remove A: compare  $A(\{B, C\})$  to  $(\{B, C\})A$

Subplan S	optJoin(S)	Cost(OptJoin(S))
A	Index scan	100
B	Seq. scan	50
....		
{A, B}	BA	156
{B, C}	BC	98
....		
{A, B, C}	BAC	500
.....		

# Example

▪ **orderJoins(A, B, C, D)**

▪  $d = 3$

- $\{A, B, C\} =$   
Remove A: compare  $A(\{B, C\})$  to  $(\{B, C\})A$

Subplan S	optJoin(S)	Cost(OptJoin(S))
A	Index scan	100
B	Seq. scan	50
....		
{A, B}	BA	156
{B, C}	BC	98
....		
{A, B, C}	BAC	500
.....		

optJoin(B,C)  
and its cost are  
already cached  
in table

# Example

## ▪ **orderJoins(A, B, C, D)**

▪  $d = 3$

•  $\{A, B, C\} =$

Remove A: compare A( **$\{B, C\}$** ) to  $(\{B, C\})A$   
Remove B: compare B( $\{A, C\}$ ) to  $(\{A, C\})B$   
Remove C: compare C( $\{A, B\}$ ) to  $(\{A, B\})C$

Subplan S	optJoin(S)	Cost(OptJoin(S))
A	Index scan	100
B	Seq. scan	50
....		
{A, B}	BA	156
<b>{B, C}</b>	BC	98
....		
{A, B, C}	BAC	500
.....		

optJoin(B,C)  
and its cost are  
already cached  
in table

# Example

## ▪ $\text{orderJoins}(A, B, C, D)$

▪  $d = 3$

•  $\{A, B, C\} =$

Remove A: compare  $A(\{B, C\})$  to  $(\{B, C\})A$   
Remove B: compare  $B(\{A, C\})$  to  $(\{A, C\})B$   
Remove C: compare  $C(\{A, B\})$  to  $(\{A, B\})C$

Subplan S	optJoin(S)	Cost(optJoin(S))
A	Index scan	100
B	Seq. scan	50
....		
{A, B}	BA	156
{B, C}	BC	98
....		
{A, B, C}	BAC	500
.....		

optJoin(B,C)  
and its cost are  
already cached  
in table

# Example

## ▪ **orderJoins(A, B, C, D)**

▪  $d = 3$

•  $\{A, B, C\} =$

Remove A: compare A( $\{B, C\}$ ) to  $(\{B, C\})A$   
 Remove B: compare B( $\{A, C\}$ ) to  $(\{A, C\})B$   
 Remove C: compare C( $\{A, B\}$ ) to  $(\{A, B\})C$

•  $\{A, B, D\} =$

Remove A: compare A( $\{B, D\}$ ) to  $(\{B, D\})A$

...

•  $\{A, C, D\} = \dots$

•  $\{B, C, D\} = \dots$

▪ Total number of steps:  $\text{choose}(N, 3) \times 3 \times 2$

Subplan S	optJoin(S)	Cost(OptJoin(S))
A	Index scan	100
B	Seq. scan	50
....		
{A, B}	BA	156
<b>{B, C}</b>	BC	98
....		
<b>{A, B, C}</b>	BAC	500
.....		

optJoin(B,C)  
and its cost are  
already cached  
in table

# Example

## ■ **orderJoins(A, B, C, D)**

### ■ $d = 4$

- $\{A, B, C, D\} =$

Subplan S	optJoin(S)	Cost(OptJoin(S))
A	Index scan	100
B	Seq. scan	50
{A, B}	BA	156
{B, C}	BC	98
{A, B, C}	BAC	500
<b>{B, C, D}</b>	DBC	150
.....		

Remove A: compare A(**{B,C,D}**) to ({B,C,D})A  
 Remove B: compare B({A,C,D}) to ({A,C,D})B  
 Remove C: compare C({A,B,D}) to ({A,B,D})C  
 Remove D: compare D({A,B,C}) to ({A,B,C})D

optJoin(B, C, D)  
and its cost are  
already cached  
in table

### ■ Total number of steps: $\text{choose}(N, 4) \times 4 \times 2$

# Interesting Orders

- Some query plans produce data in sorted order
  - E.g scan over a primary index, merge-join
  - Called *interesting order*
- Next operator may use this order
  - E.g. can be another merge-join
- For each subset of relations, compute multiple optimal plans, one for each interesting order
- Increases complexity by factor  $k+1$ , where  $k$ =number of interesting orders

# Why Left-Deep

Asymmetric, cost depends on the order

- Left: Outer relation      Right: Inner relation
- For nested-loop-join, we try to load the outer (typically smaller) relation in memory, then read the inner relation one page at a time
$$B(R) + B(R) * B(S) \text{ or } B(R) + B(R)/M * B(S)$$
- For index-join,  
we assume right (inner) relation has index



# Why Left-Deep

## ■ Advantages of left-deep trees?

1. Fits well with standard join algorithms (nested loop, one-pass), more efficient
2. One pass join: Uses smaller memory
  1.  $((R, S), T)$ , can reuse the space for  $R$  while joining  $(R, S)$  with  $T$
  2.  $(R, (S, T))$ : Need to hold  $R$ , compute  $(S, T)$ , then join with  $R$ , worse if more relations
3. Nested loop join, consider top-down iterator `next()`
  1.  $((R, S), T)$ , Reads the chunks of  $(R, S)$  once, reads stored base relation  $T$  multiple times
  2.  $(R, (S, T))$ : Reads the chunks of  $R$  once, reads computed relation  $(S, T)$  multiple times, either more time or more space

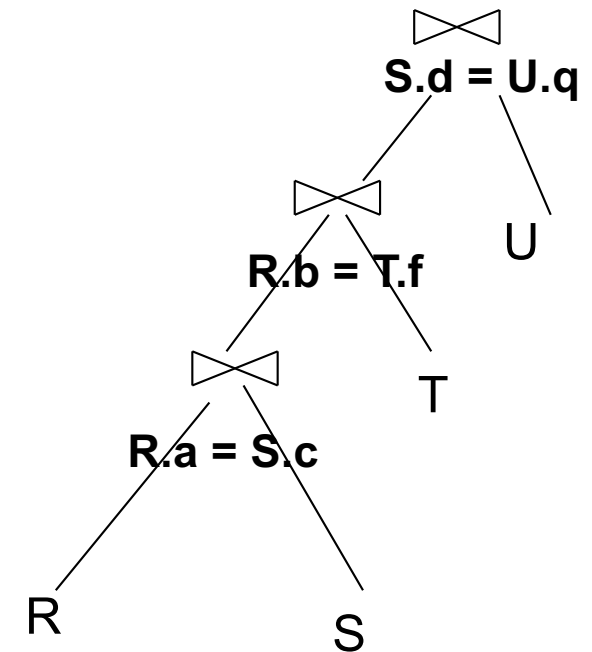
# Implementation in SimpleDB (lab5)

## 1. `JoinOptimizer.java` (and the classes used there)

## 2. Returns vector of “`LogicalJoinNode`”

Two base tables, two join attributes, predicate  
e.g.  $R(a, b), S(c, d), T(a, f), U(p, q)$   
 $(R, S, R.a, S.c, =)$

Recall that SimpleDB keeps all attributes of  
 $R, S$  after their join  $R.a, R.b, S.c, S.d$



## 3. Output vector looks like:

$\langle (R, S, R.a, S.c), (R, T, R.b, T.f), (S, U, S.d, U.q) \rangle$

# Implementation in SimpleDB (lab5)

Any advantage of returning pairs?

- Flexibility to consider all linear plans  
 $\langle (R, S, R.a, S.c), (R, T, R.b, T.f), (U, S, U.q, S.d) \rangle$

More Details:

- You mainly need to implement “`orderJoins(..)`”
- “`CostCard`” data structure stores a plan, its cost and cardinality: you would need to estimate them
- “`PlanCache`” stores the table in dyn. Prog:

Maps a set of LJJN to  
a vector of LJJN (best plan for the vector),  
its cost, and its cardinality

**LJJN = LogicalJoinNode**

