

Summary of External Join Algorithms

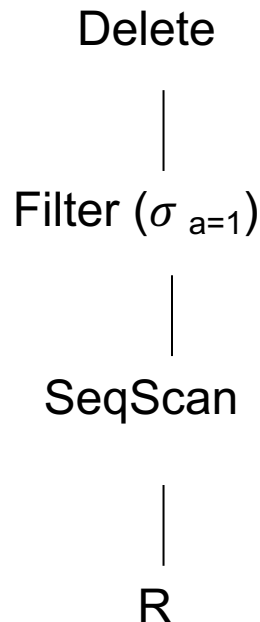
- Block Nested Loop: $B(S) + B(R) \cdot B(S) / (M-1)$
- Clustered index Join: $B(R) + T(R)B(S)/V(S,a)$
Unclustered index join: $B(R) + T(R)T(S)/V(S,a)$
- Partitioned Hash: $3B(R) + 3B(S)$;
 - $\min(B(R), B(S)) \leq M^2$
- Merge Join: $3B(R) + 3B(S)$
 - $B(R) + B(S) \leq M^2$

Before We Go Into Query Plan Costs... How do Updates Work? (Insert/Delete)

Example Using Delete

delete from R where a=1;

Query plan



In SimpleDB, the Delete Operator calls `BufferPool.deleteTuple()`

Why not call `HeapFile.deleteTuple()` directly?

Because there could also be indexes.
Need some entity that will decide all the structures from where tuple needs to be deleted

BufferPool then calls `HeapFile.deleteTuple()`

Pushing Updates to Disk

- When **inserting a tuple**, HeapFile inserts it on a page but does not write the page to disk
- When **deleting a tuple**, HeapFile deletes tuple from a page but does not write the page to disk
- The buffer manager worries when to write pages to disk (and when to read them from disk)
- When need to **add new page** to file, HeapFile adds page to file on disk and then reads it through buffer manager

Back to Query Optimization

Supplier(sid, sname, scity, sstate)

Supply(sid, pno, quantity)

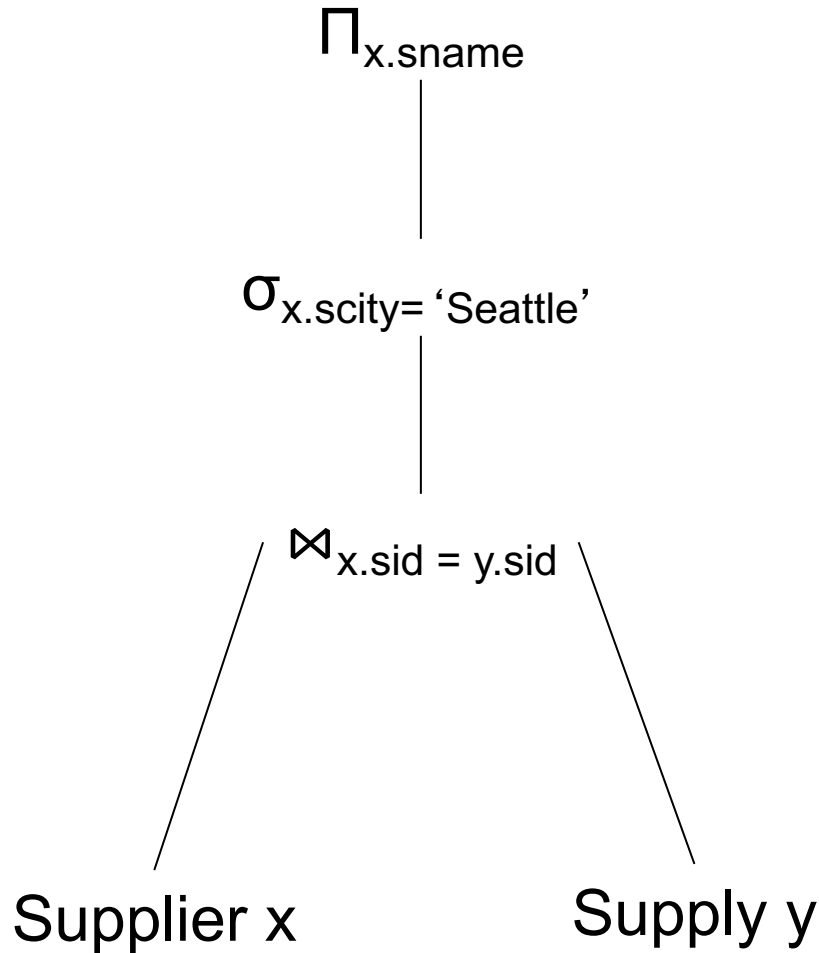
Example Optimization

```
SELECT x.name  
FROM.  Supplier x, Supply y  
WHERE x.sid = y.sid  
       and x.scity = 'Seattle'
```

Supplier(sid, sname, scity, sstate)

Supply(sid, pno, quantity)

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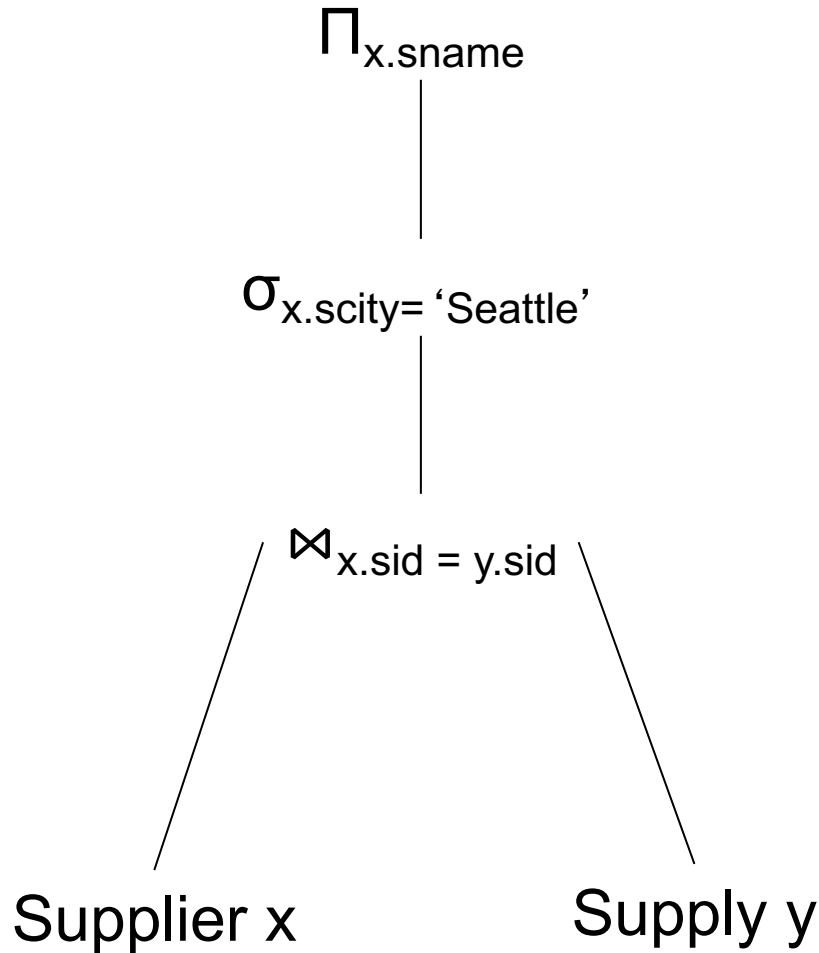


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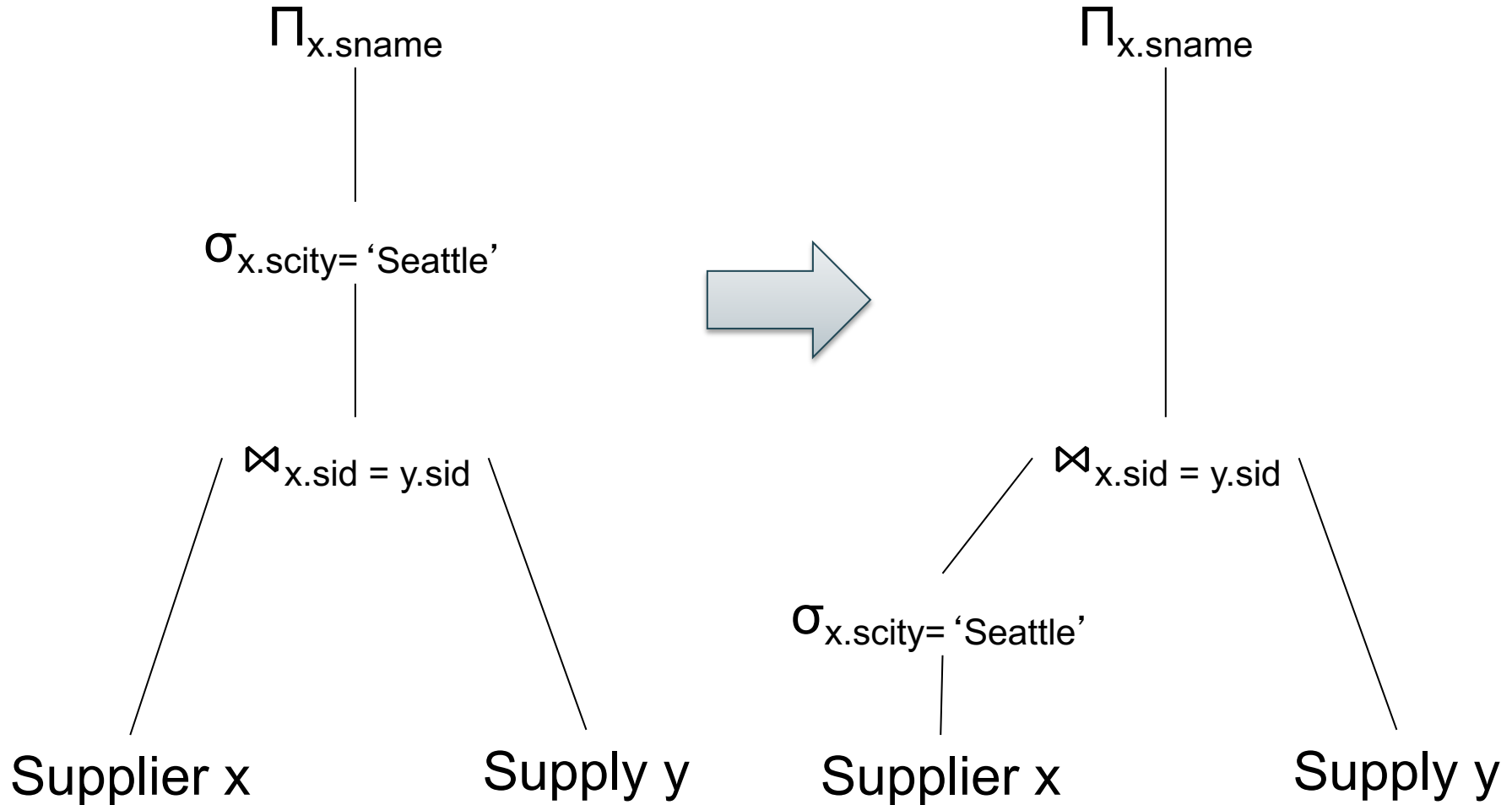
Push Selections Down



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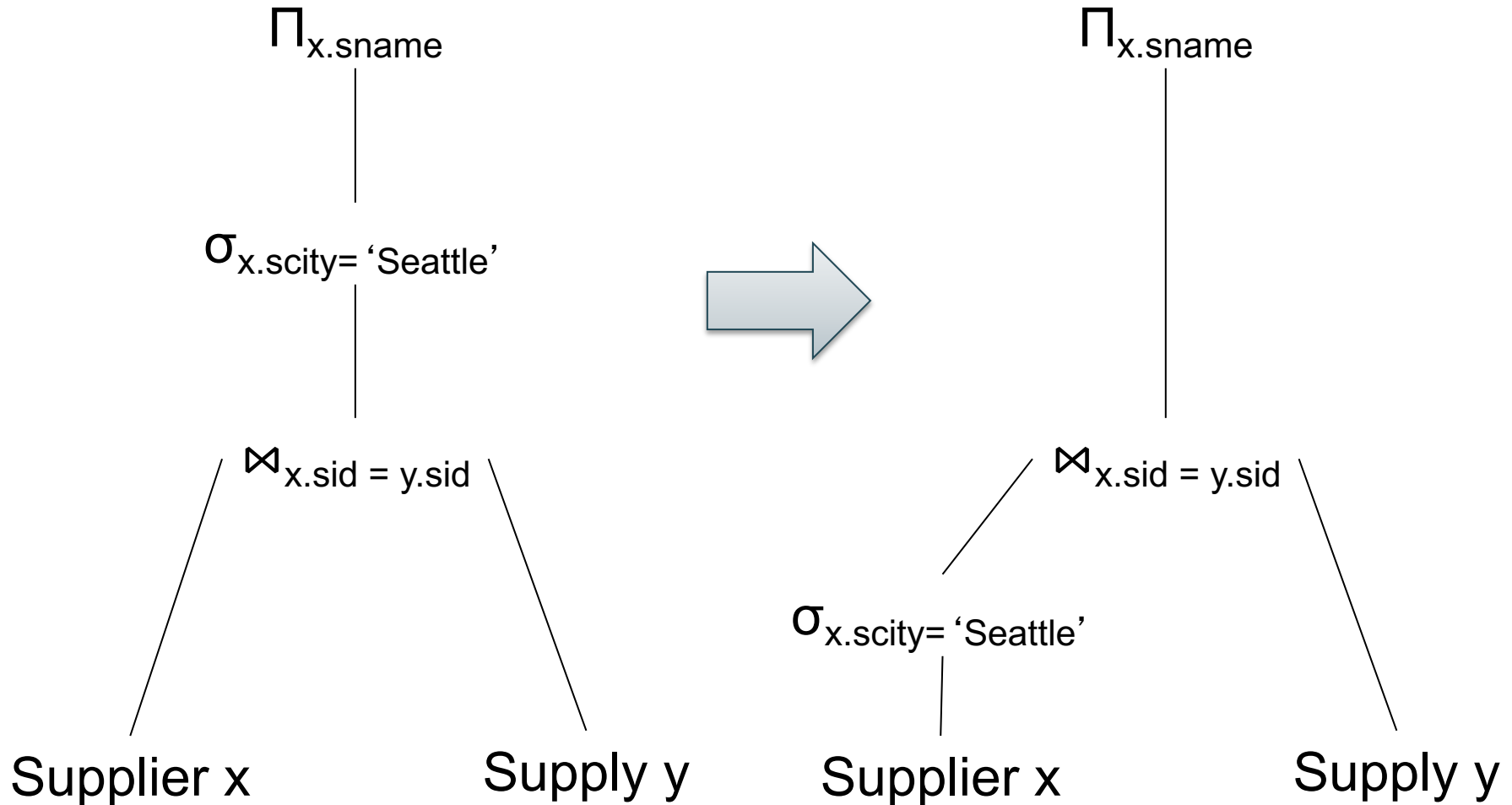
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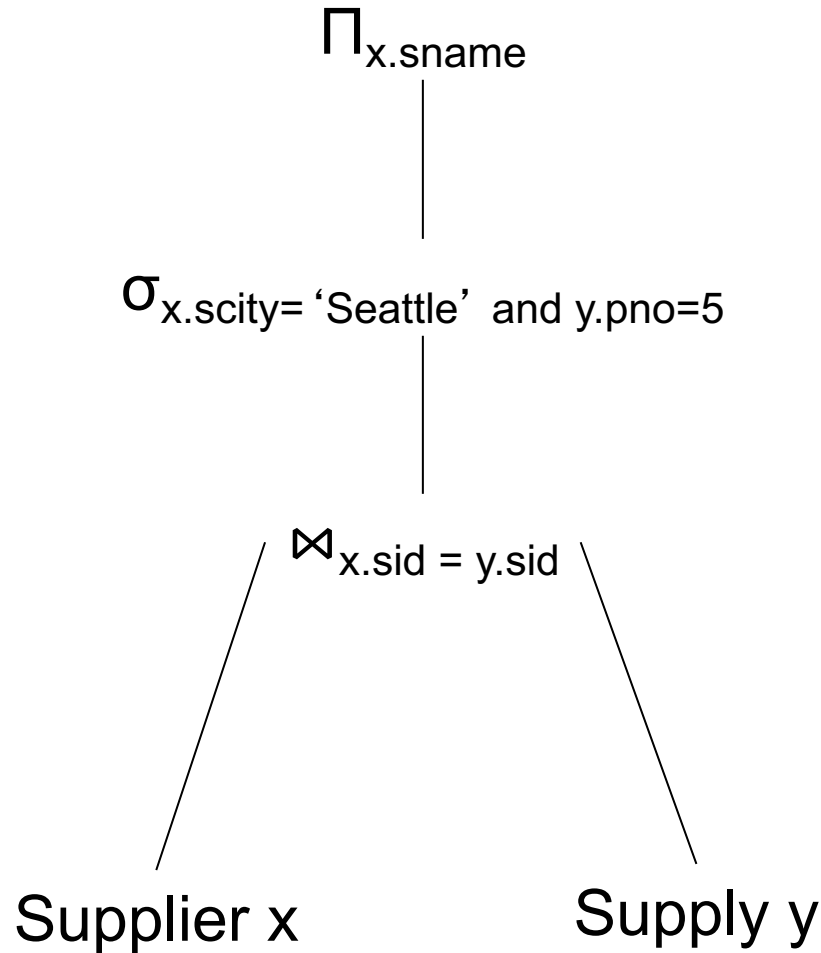


$$\sigma_C(R \bowtie S) = \sigma_C(R) \bowtie S \quad \text{when } C \text{ refers only to } R$$

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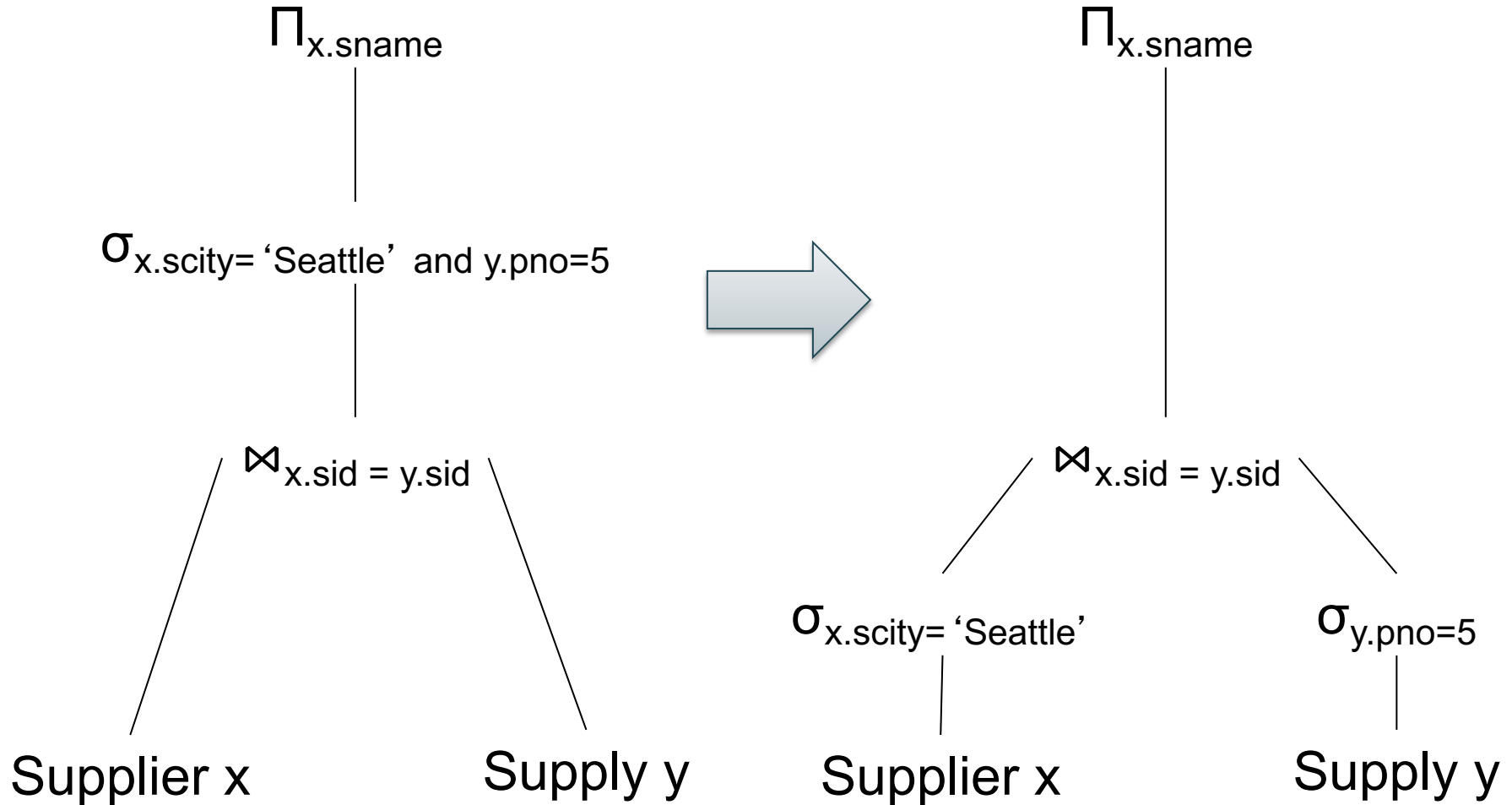
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Supplier(sid, sname, scity, sstate)

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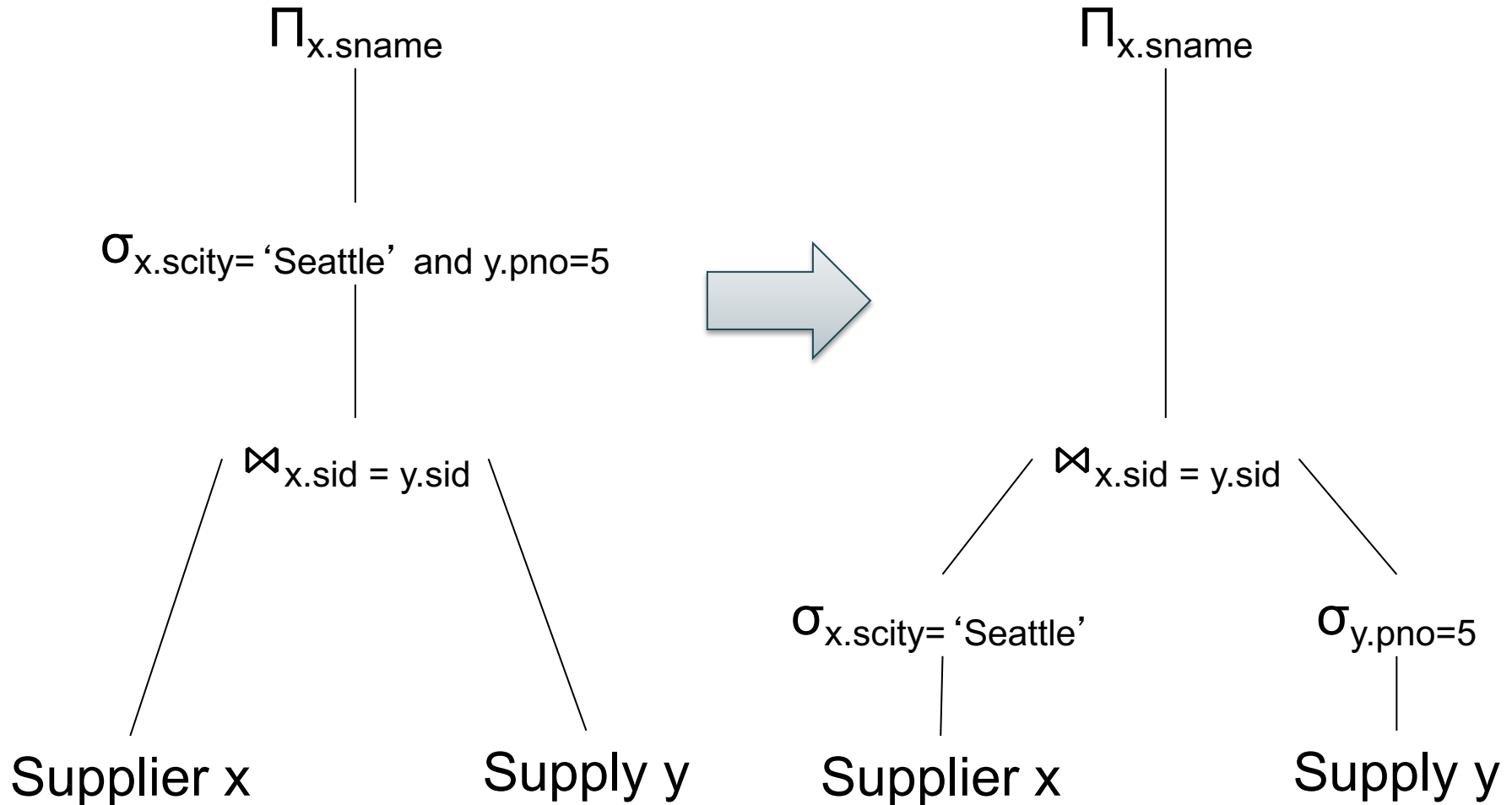
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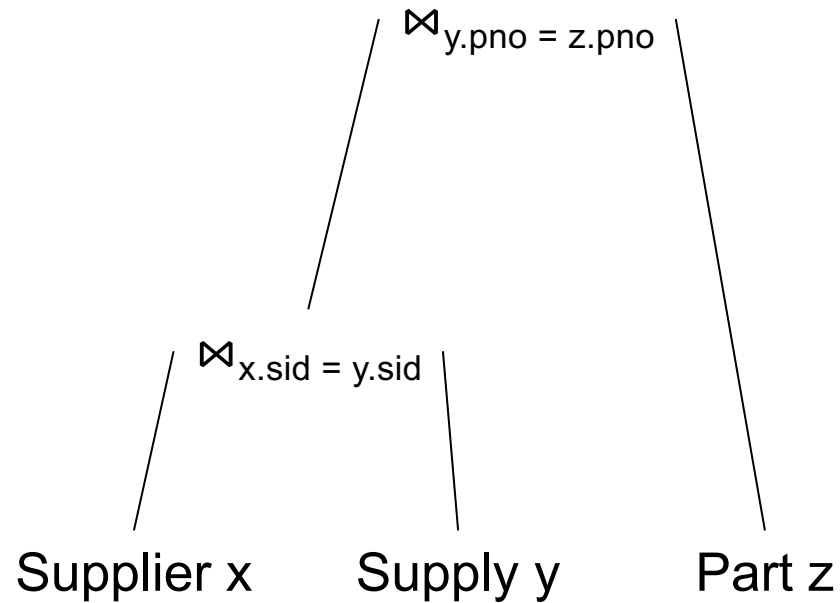
Push Selections Down



$$\sigma_{C1 \text{ and } C2}(R \bowtie S) = \sigma_{C1}(\sigma_{C2}(R \bowtie S)) = \sigma_{C1}(R \bowtie \sigma_{C2}(S)) = \sigma_{C1}(R) \bowtie \sigma_{C2}(S)$$

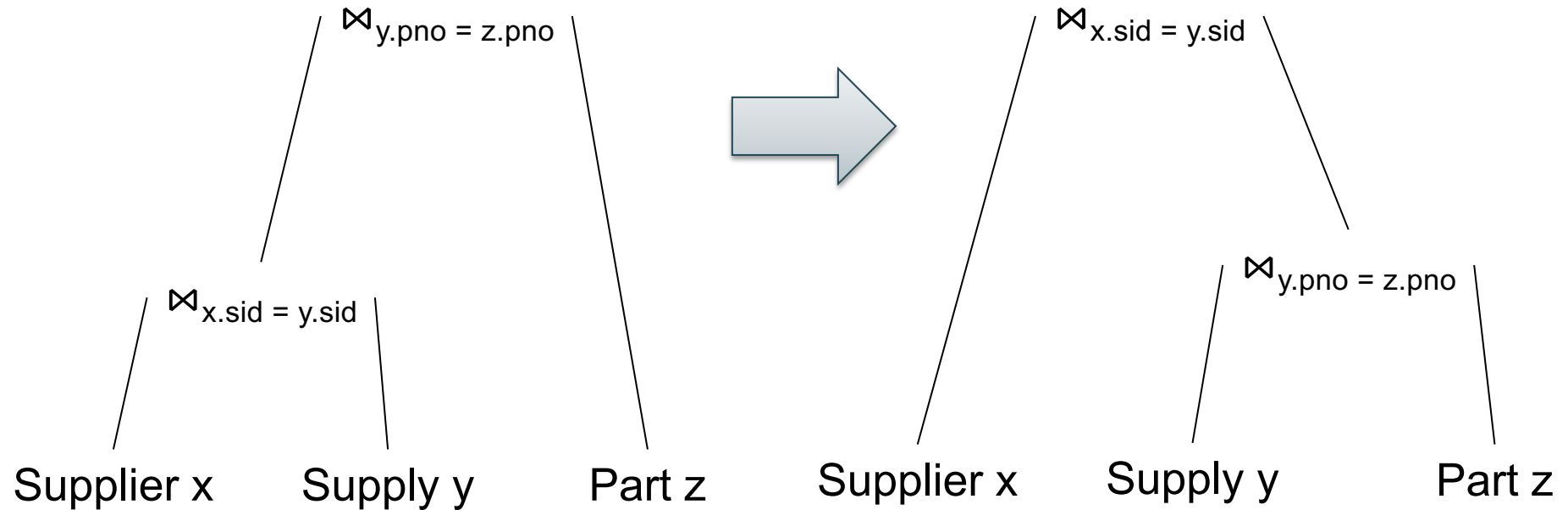
Supplier(sid, sname, scity, sstate)
Supply(sid, pno, quantity)
Part(pno, pname, pprice)

Join Reorder



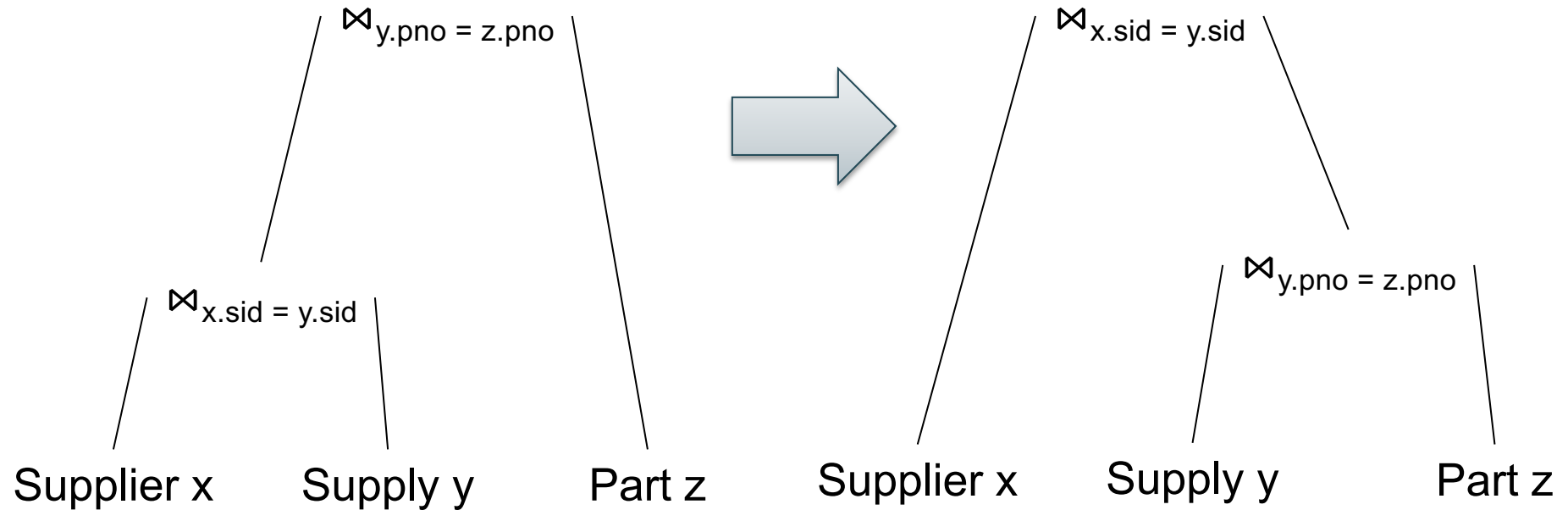
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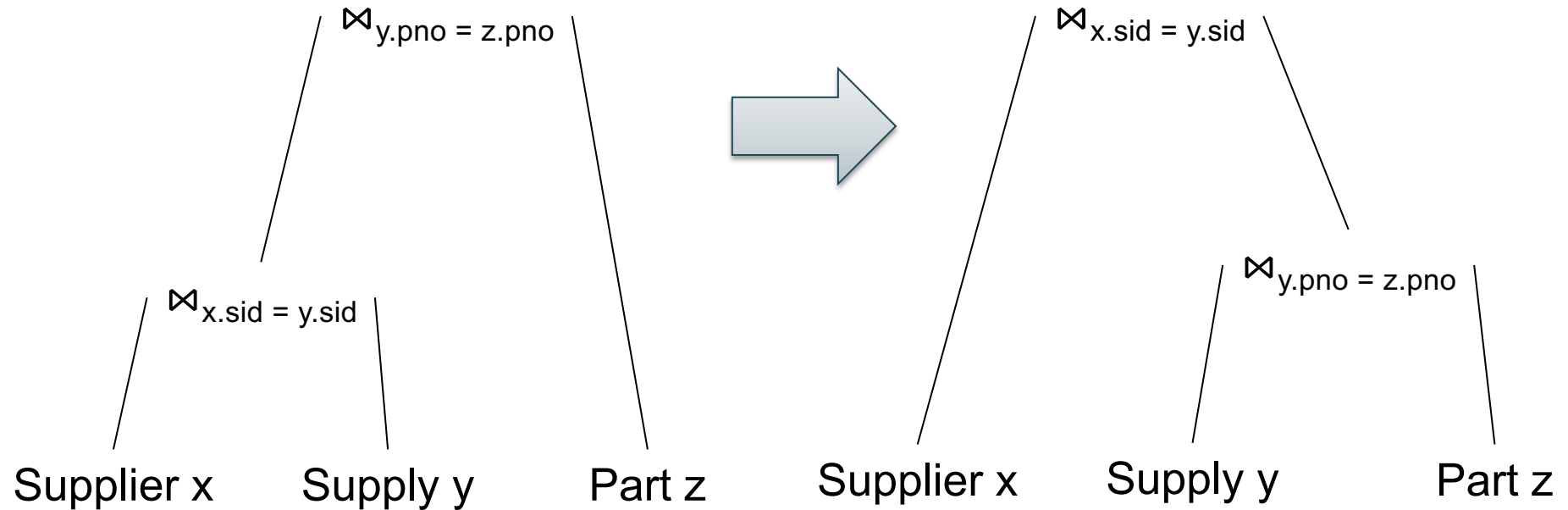
Join Reorder



$$(R \bowtie S) \bowtie T = R \bowtie (S \bowtie T)$$

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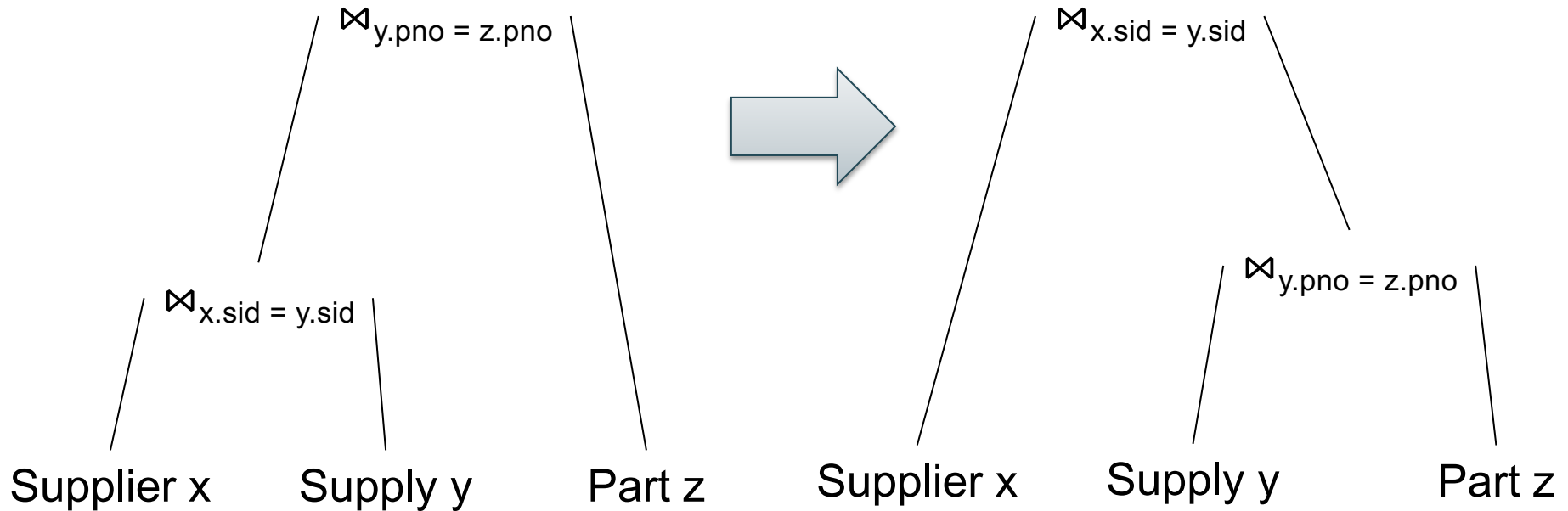
Also:

$$R \bowtie S = S \bowtie R$$

Supplier(sid, sname, scity, sstate)
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Join Reorder

When is one plan better than the other?



$$(R \bowtie S) \bowtie T = R \bowtie (S \bowtie T)$$

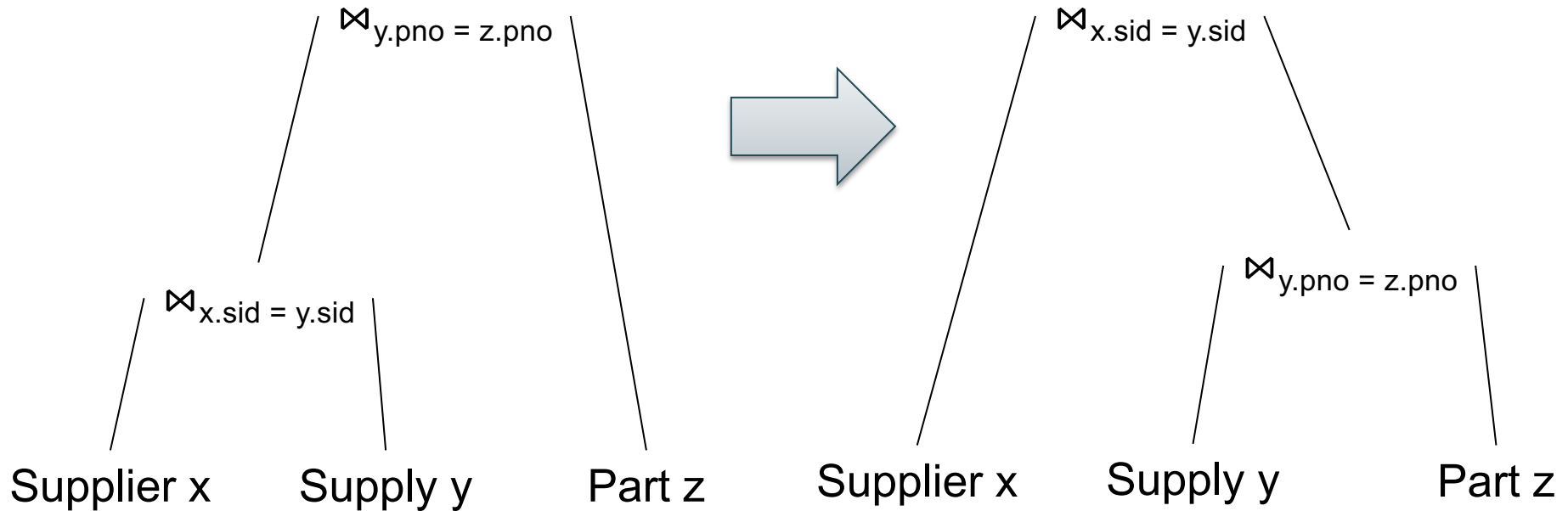
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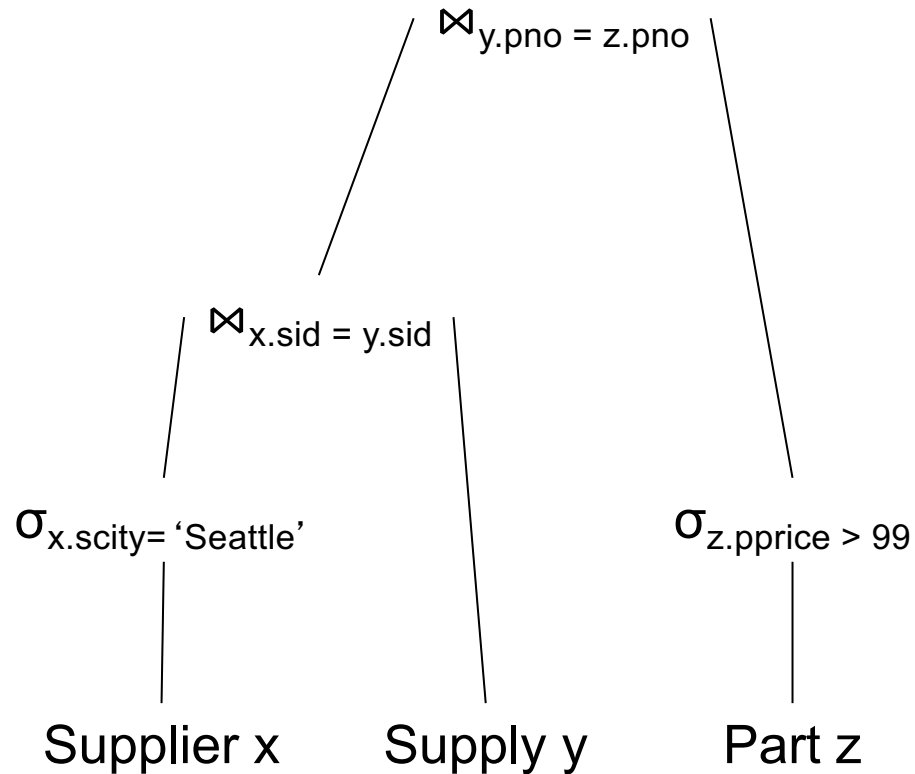
$$R \bowtie S = S \bowtie R$$

Depends which is smaller:

$R \bowtie S$ or $S \bowtie T$

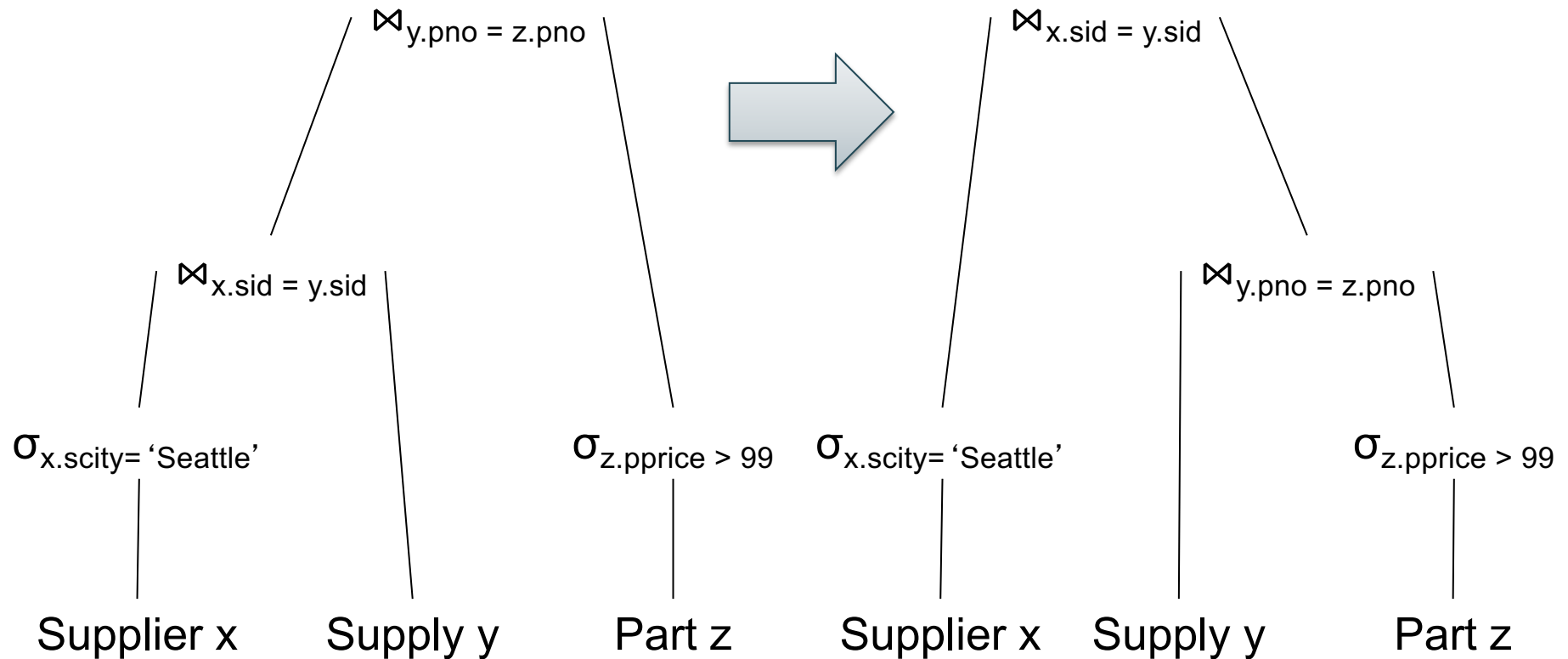
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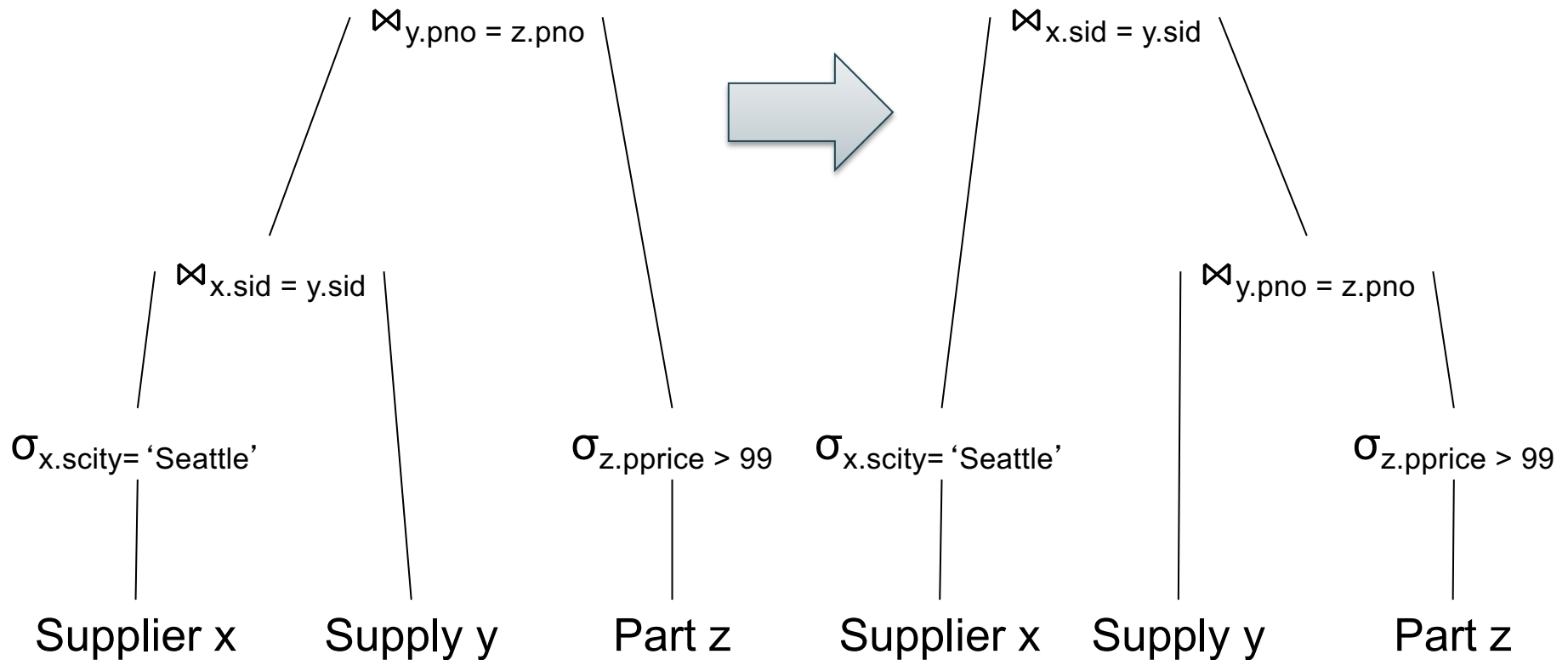
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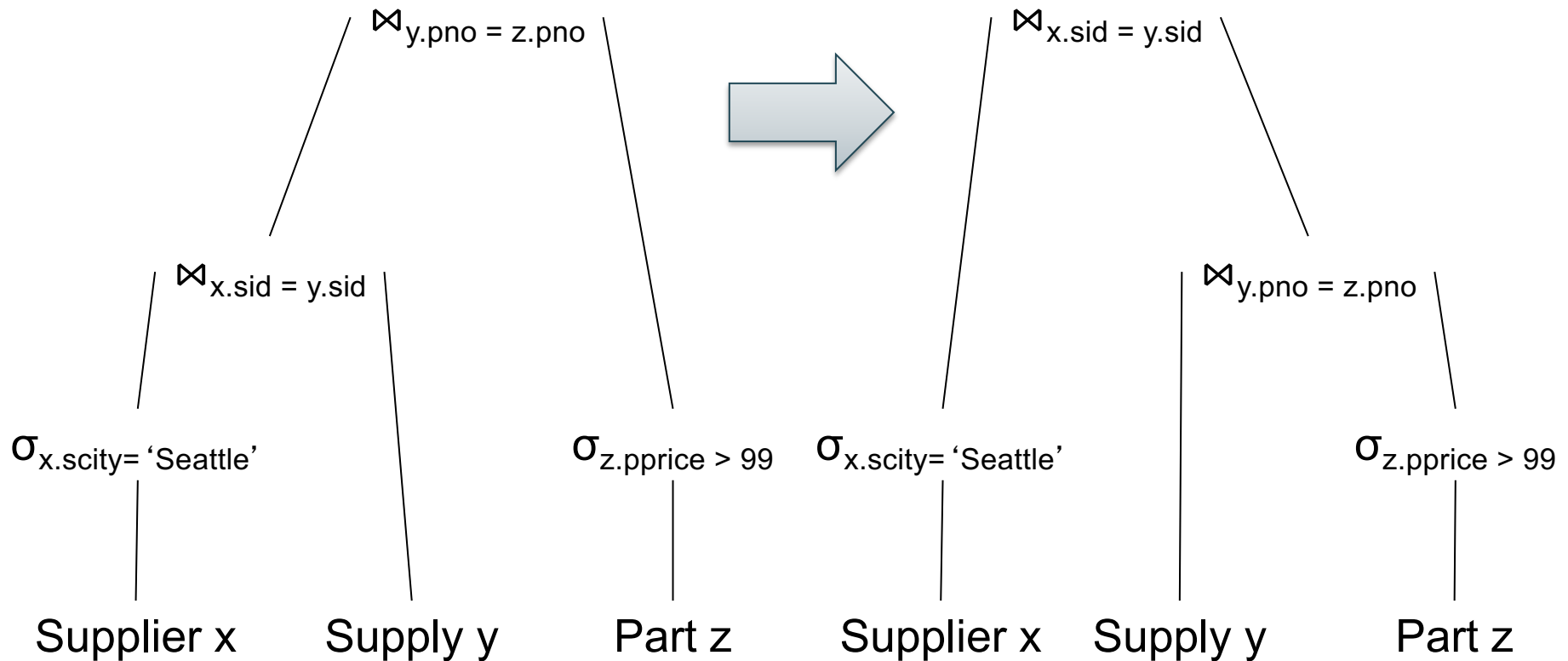
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Supplier(sid, sname, scity, sstate)
Supply(sid, pno, quantity)
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Join Reorder

When is one plan better than the other?



Lesson: need sizes of $\sigma_{x.scity = 'Seattle'}(\text{Supplier})$, $\sigma_{z.pprice > 99}(\text{Part})$

Query Optimizer

Three components:

- Cost estimation

- Cardinality estimation $T(R)$ each intermediate result
- Cost = CPU + I/O + Network, all depend on $T(R)$

- Search space

- Which plans do we consider?

- Search algorithm

- How do we search the space?

Cost Estimation

- Database statistics
 - Collect statistical summaries of stored data
- Estimate size (=cardinality) in a bottom-up fashion
 - This is the most difficult part, and still inadequate in today's query optimizers
- Estimate cost by using the estimated size
 - Hand-written formulas, similar to those we used for computing the cost of each physical operator

Database Statistics

- Number of tuples (cardinality), $T(R)$
- Number of distinct values of attribute a , $V(R,a)$
- Number of physical pages, $B(R)$
- Statistical information on attributes
 - Min value, Max value
- Histograms
- Collection approach: periodic, using sampling

Size Estimation Problem

```
Q = SELECT list  
    FROM   R1, ..., Rn  
    WHERE  cond1 AND cond2 AND . . . AND condk
```

Given $T(R1), T(R2), \dots, T(Rn)$
Estimate $T(Q)$

How can we do this ? Note: doesn't have to be exact.

Size Estimation Problem

```
Q = SELECT list  
      FROM   R1, ..., Rn  
      WHERE  cond1 AND cond2 AND . . . AND condk
```

Remark: $T(Q) \leq T(R1) \times T(R2) \times \dots \times T(Rn)$

Size Estimation Problem

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Remark: $T(Q) \leq T(R1) \times T(R2) \times \dots \times T(Rn)$

Key idea: each condition reduces the size of $T(Q)$ by some factor, called **selectivity factor**

Example

R(A,B)
S(B,C)
T(C,D)

```
Q = SELECT *  
    FROM R, S, T  
    WHERE R.B=S.B and S.C=T.C and R.A=40
```

$T(R) = 30k$, $T(S) = 200k$, $T(T) = 10k$

Selectivity of $R.B = S.B$ is $1/3$

Selectivity of $S.C = T.C$ is $1/10$

Selectivity of $R.A = 40$ is $1/200$

Q: What is the estimated size of the query output $T(Q)$?

Example

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Q: What is the estimated size of the query output $T(Q)$?

$$T(Q) = 30k * 200k * 10k * 1/3 * 1/10 * 1/200 = 10^{10}$$

Computing Selectivites

Will use these assumptions

- **Uniformity**
- **Independence**
- **Containment of values**
- **Preservation of values**

Selectivity Factors for Conditions

- $A = c$
 - Selectivity = $1/V(R,A)$ $/* \sigma_{A=c}(R) */$

Selectivity Factors for Conditions

- $A = c$ /* $\sigma_{A=c}(R)$ */
 - Selectivity = $1/V(R,A)$
- $A < c$ /* $\sigma_{A < c}(R)$ */
 - Selectivity = $(c - \text{Low}(R, A)) / (\text{High}(R, A) - \text{Low}(R, A))$

Selectivity Factors for Conditions

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$/^* \sigma_{A=c}(R) ^*/$

- Selectivity = $1/V(R,A)$

Uniformity
Assumption

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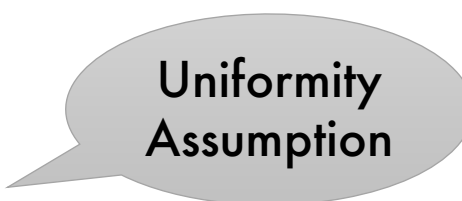
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■ Cond_1 and Cond_2

• Selectivity = $\text{Selectivity}(\text{Cond}_1) * \text{Selectivity}(\text{Cond}_2)$



Uniformity
Assumption

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Independence
Assumption

■ Cond_1 and Cond_2

• Selectivity = $\text{Selectivity}(\text{Cond}_1) * \text{Selectivity}(\text{Cond}_2)$

■ $A = B$ $/* R \bowtie_{A=B} S */$

• Selectivity = $1 / \max(V(R,A), V(S,A))$

• (will explain next)

Containment of values
Assumption

Assumptions

- Containment of values: if $V(R,A) \leq V(S,B)$, then all values $R.A$ occur in $S.B$
 - E.g. when A is a foreign key in R , and B is a key in S
- Preservation of values: for any attribute C of R ,
 $V(R \bowtie_{A=B} S, C) = V(R, C)$
 - We need this for multiple conditions

Selectivity of $R \bowtie_{A=B} S$

$$R \bowtie_{A=B} S$$

- Assume $V(R,A) \leq V(S,B)$

Selectivity of $R \bowtie_{A=B} S$

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- Assume $V(R,A) \leq V(S,B)$
- A tuple t in R joins with $T(S) / V(S,B)$ tuple(s) in S

Selectivity of $R \bowtie_{A=B} S$

$$R \bowtie_{A=B} S$$

- Assume $V(R,A) \leq V(S,B)$
- A tuple t in R joins with $T(S) / V(S,B)$ tuple(s) in S
- Hence $T(R \bowtie_{A=B} S) = T(R) T(S) / V(S,B)$

$$T(R \bowtie_{A=B} S) = T(R) T(S) / \max(V(R,A), V(S,B))$$

Supplier(sid, sname, scity, sstate)
Supply(sid, pno, quantity)

T(Supply) = 10000
T(Supplier) = 1000

Key Foreign-key Join

- How large is T(Q)?

```
SELECT sname
FROM Supplier x, Supply y
WHERE x.sid = y.sid
```

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We know
this

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Containment
of values assumption

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Supplier(sid, sname, scity, sstate)

Supply(sid, pno, quantity)

$T(\text{Supply}) = 10000$

$T(\text{Supplier}) = 1000$

$V(\text{Supplier}, \text{sstate}) = 10$

Preservation of Values

- How large is $T(Q)$?

```
SELECT sname
FROM Supplier x, Supply y
WHERE x.sid = y.sid
      and x.sstate = 'WA'
```

Supplier(sid, sname, scity, sstate)
Supply(sid, pno, quantity)

$T(\text{Supply}) = 10000$
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Preservation of Values

- How large is $T(Q)$?

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SELECT sname
FROM Supplier x, Supply y
WHERE x.sid = y.sid
      and x.sstate = 'WA'
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$$\begin{aligned} T(Q) &= T(\sigma_{\text{sstate}='WA'} (\text{Supply} \bowtie \text{Supplier})) \\ &= T(\text{Supply} \bowtie \text{Supplier}) / V(\text{Supply} \bowtie \text{Supplier}, \text{sstate}) \end{aligned}$$

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Preservation of
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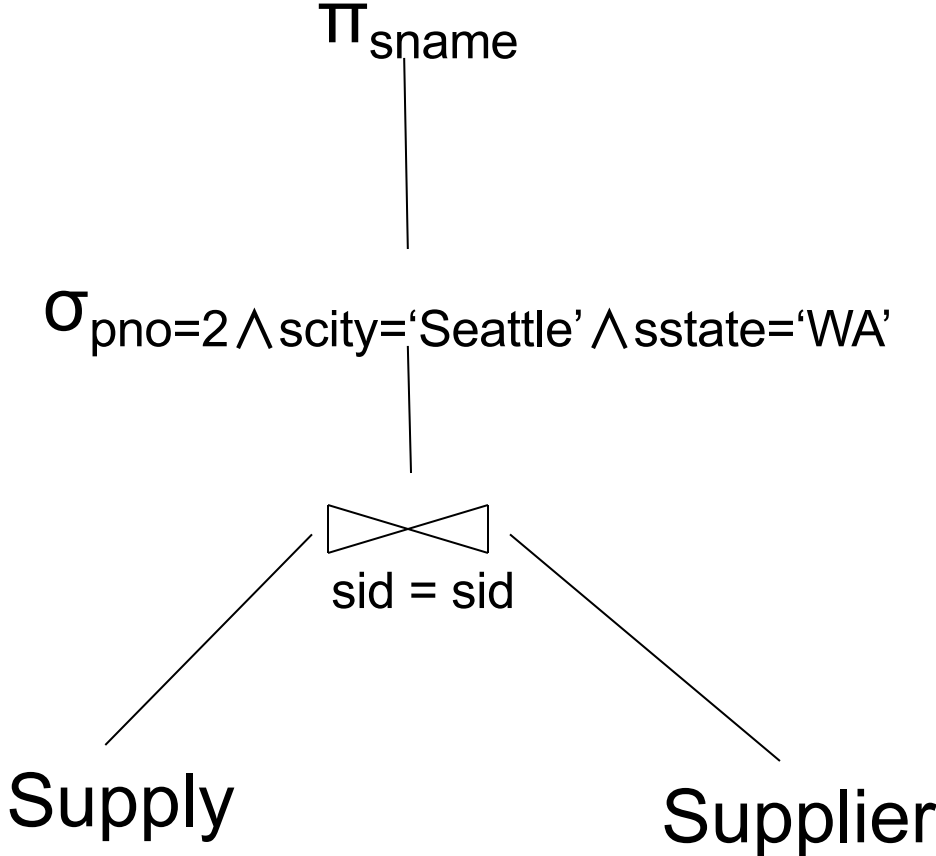
Example

- Enumerate logical plans,
estimate T(temp relations)
- For each logical plan,
enumerate physical plans,
estimate Cost

```
SELECT sname
FROM Supplier x, Supply y
WHERE x.sid = y.sid
      and y.pno = 2
      and x.scity = 'Seattle'
      and x.sstate = 'WA'
```

Supplier(sid, sname, scity, sstate)
Supply(sid, pno, quantity)

Logical Query Plan 1



```
SELECT sname
FROM Supplier x, Supply y
WHERE x.sid = y.sid
      and y.pno = 2
      and x.scity = 'Seattle'
      and x.sstate = 'WA'
```

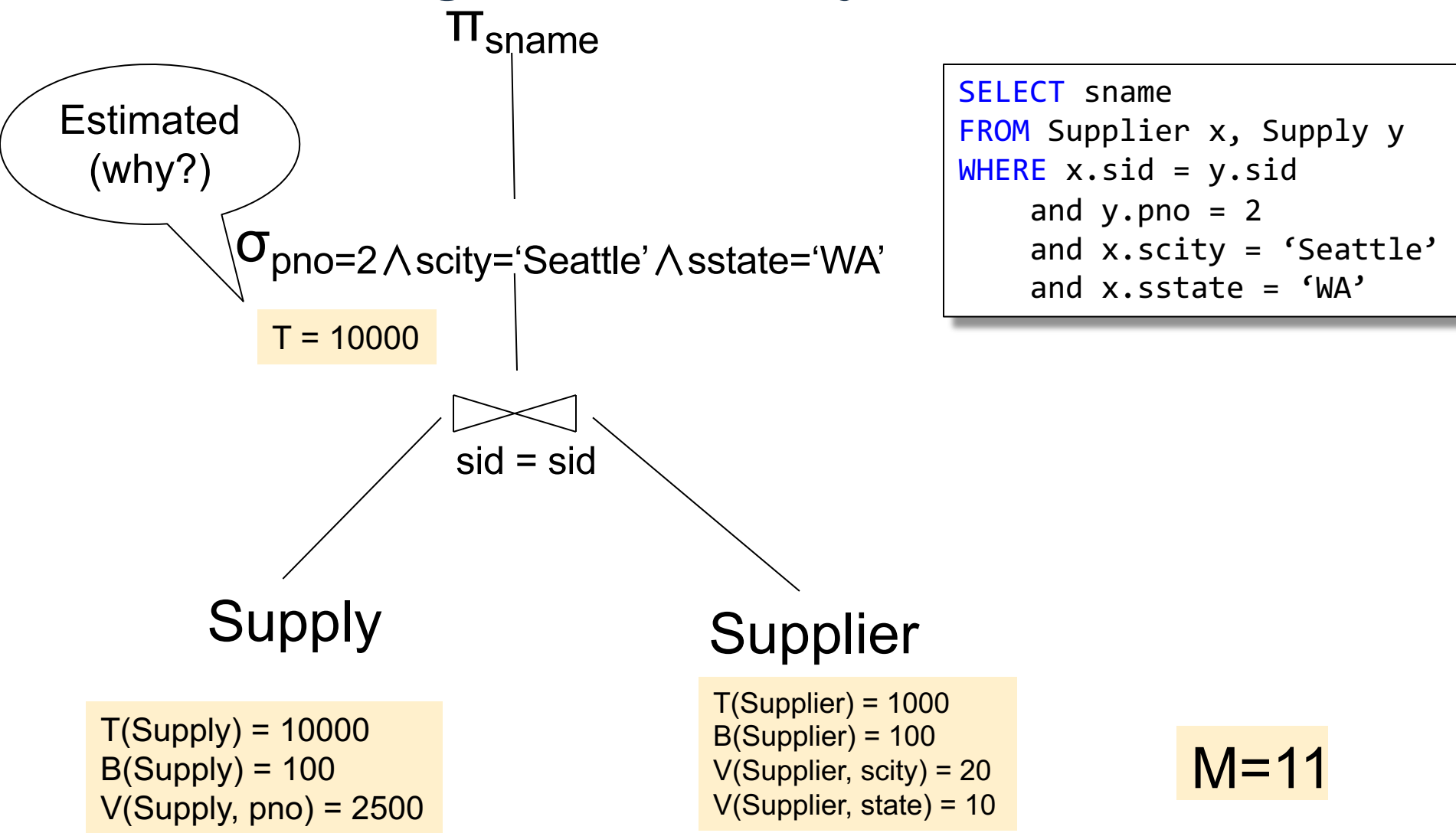
T(Supply) = 10000
B(Supply) = 100
V(Supply, pno) = 2500

T(Supplier) = 1000
B(Supplier) = 100
V(Supplier, scity) = 20
V(Supplier, state) = 10

M=11

Supplier(sid, sname, scity, sstate)
Supply(sid, pno, quantity)

Logical Query Plan 1



Supplier(sid, sname, scity, sstate)
Supply(sid, pno, quantity)

Logical Query Plan 1

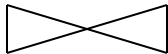
Estimated
(why?)

T < 1

Π_{sname}

$\sigma_{pno=2 \wedge scity='Seattle' \wedge sstate='WA'}$

T = 10000



sid = sid

Supply

Supplier

```
SELECT sname
FROM Supplier x, Supply y
WHERE x.sid = y.sid
      and y.pno = 2
      and x.scity = 'Seattle'
      and x.sstate = 'WA'
```

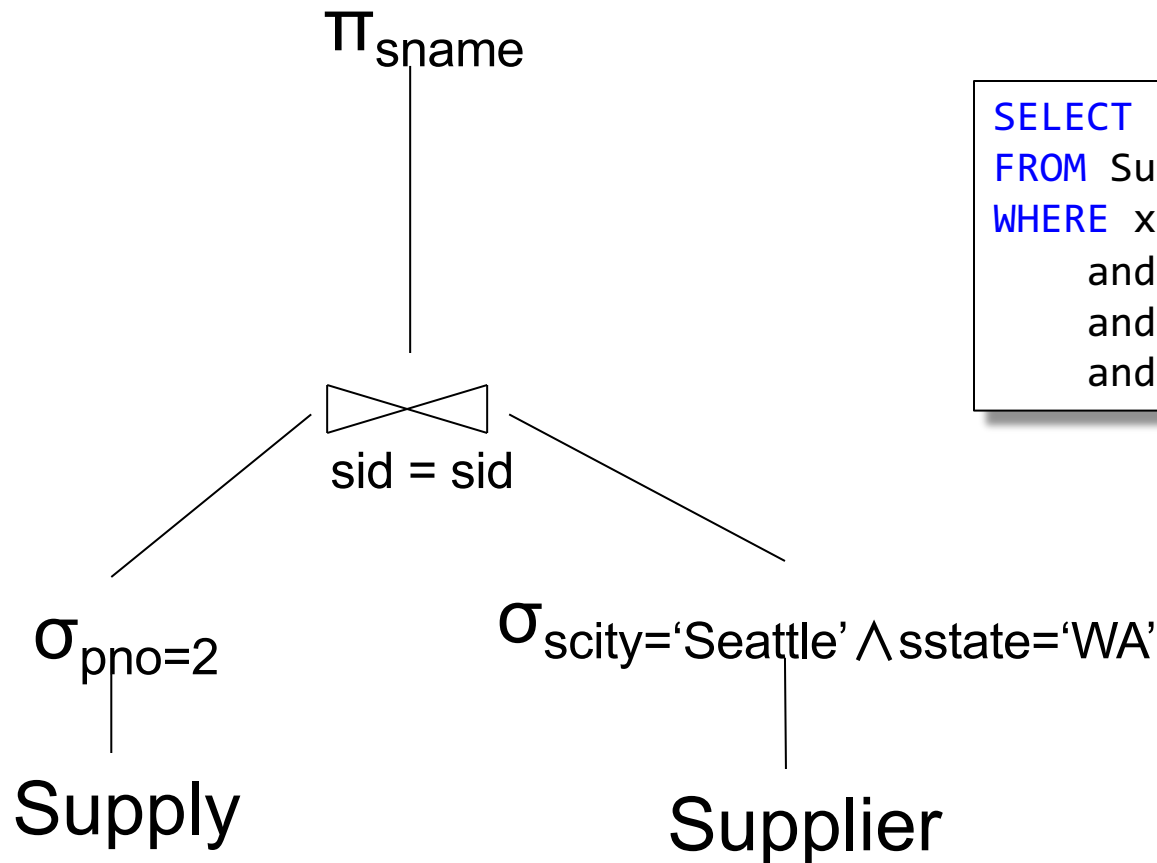
T(Supply) = 10000
B(Supply) = 100
V(Supply, pno) = 2500

T(Supplier) = 1000
B(Supplier) = 100
V(Supplier, scity) = 20
V(Supplier, state) = 10

M=11

Supplier(sid, sname, scity, sstate)
Supply(sid, pno, quantity)

Logical Query Plan 2



```
SELECT sname
FROM Supplier x, Supply y
WHERE x.sid = y.sid
      and y.pno = 2
      and x.scity = 'Seattle'
      and x.sstate = 'WA'
```

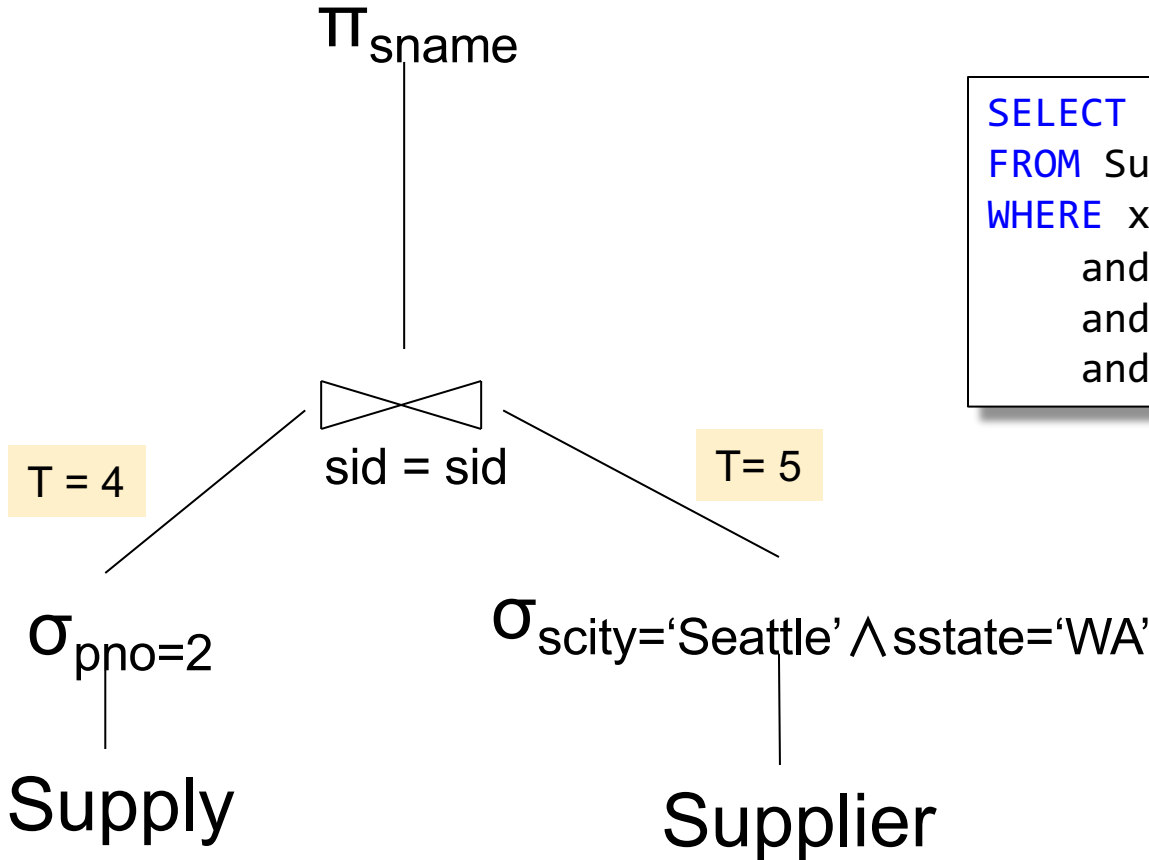
T(Supply) = 10000
B(Supply) = 100
V(Supply, pno) = 2500

T(Supplier) = 1000
B(Supplier) = 100
V(Supplier, scity) = 20
V(Supplier, state) = 10

M=11

Supplier(sid, sname, scity, sstate)
Supply(sid, pno, quantity)

Logical Query Plan 2



```
SELECT sname
FROM Supplier x, Supply y
WHERE x.sid = y.sid
      and y.pno = 2
      and x.scity = 'Seattle'
      and x.sstate = 'WA'
```

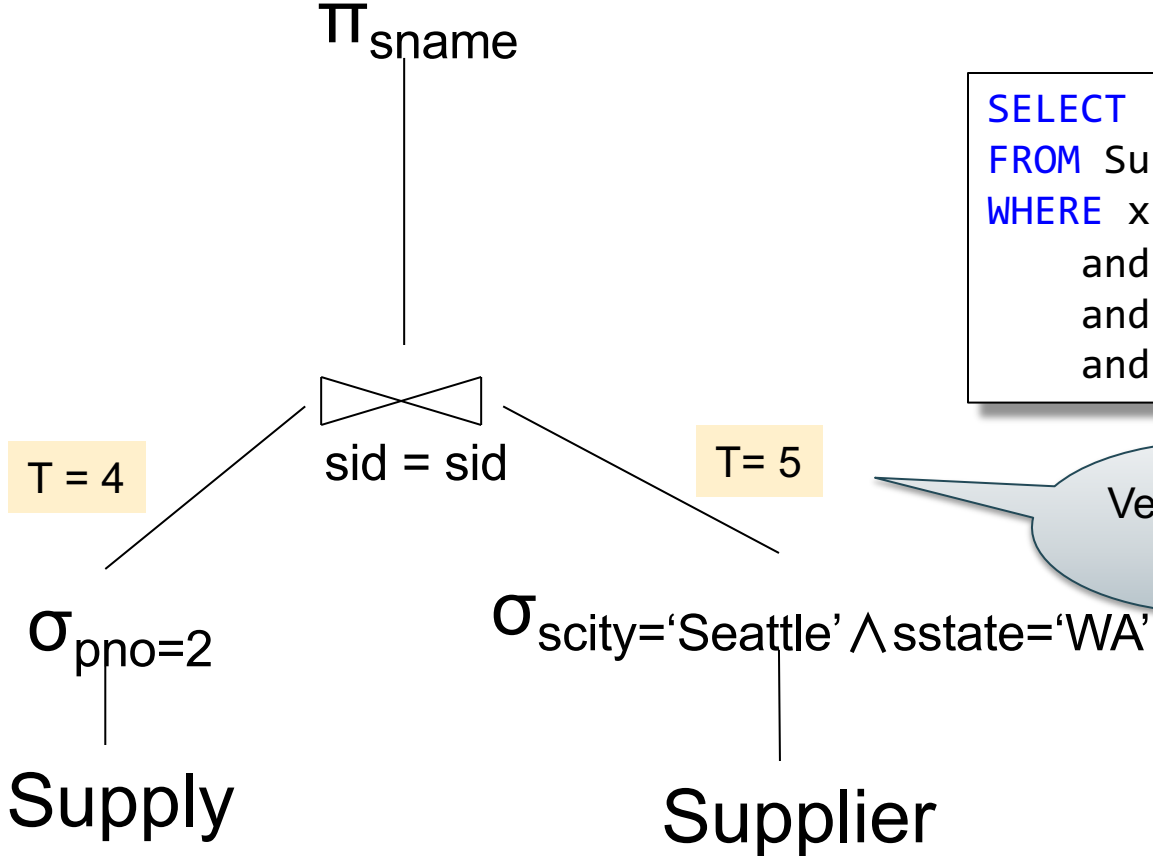
T(Supply) = 10000
B(Supply) = 100
V(Supply, pno) = 2500

T(Supplier) = 1000
B(Supplier) = 100
V(Supplier, scity) = 20
V(Supplier, state) = 10

M=11

Supplier(sid, sname, scity, sstate)
Supply(sid, pno, quantity)

Logical Query Plan 2



```
SELECT sname
FROM Supplier x, Supply y
WHERE x.sid = y.sid
      and y.pno = 2
      and x.scity = 'Seattle'
      and x.sstate = 'WA'
```

Very wrong!
Why?

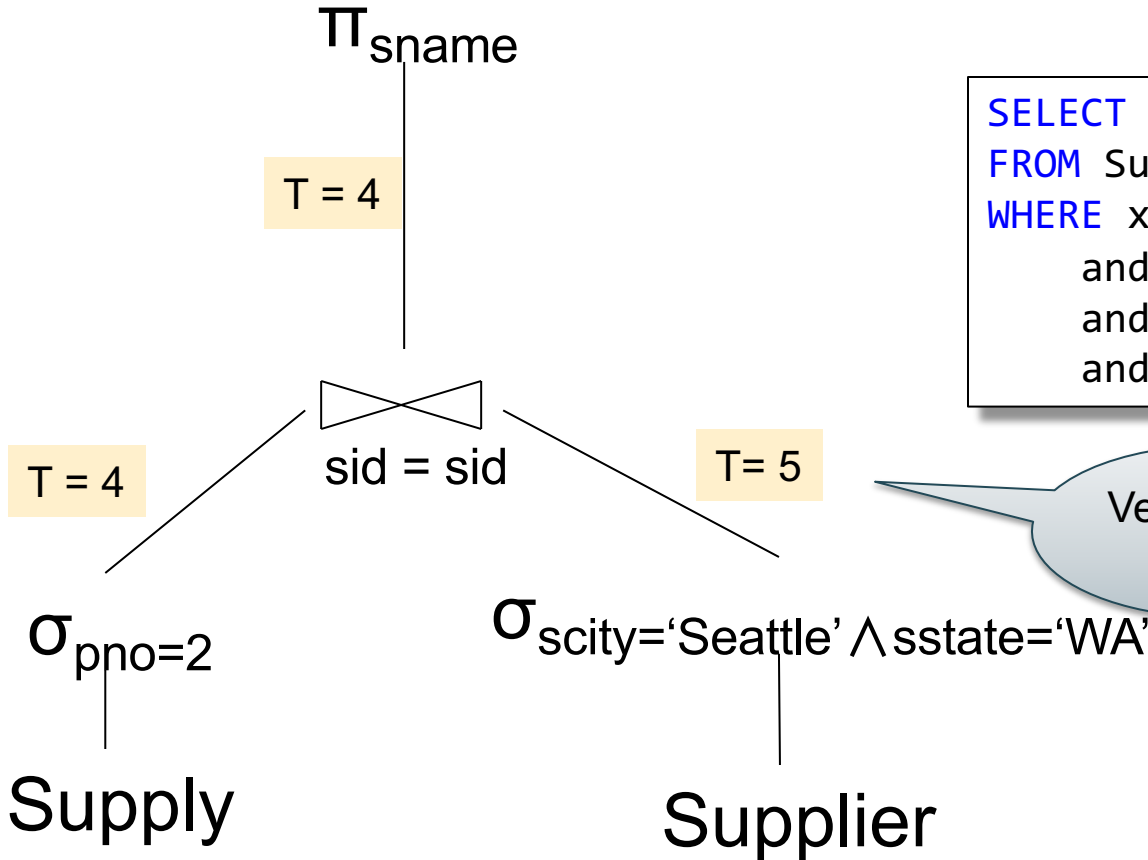
T(Supply) = 10000
B(Supply) = 100
V(Supply, pno) = 2500

T(Supplier) = 1000
B(Supplier) = 100
V(Supplier, scity) = 20
V(Supplier, state) = 10

M=11

Supplier(sid, sname, scity, sstate)
Supply(sid, pno, quantity)

Logical Query Plan 2



```
SELECT sname
FROM Supplier x, Supply y
WHERE x.sid = y.sid
      and y.pno = 2
      and x.scity = 'Seattle'
      and x.sstate = 'WA'
```

Very wrong!
Why?

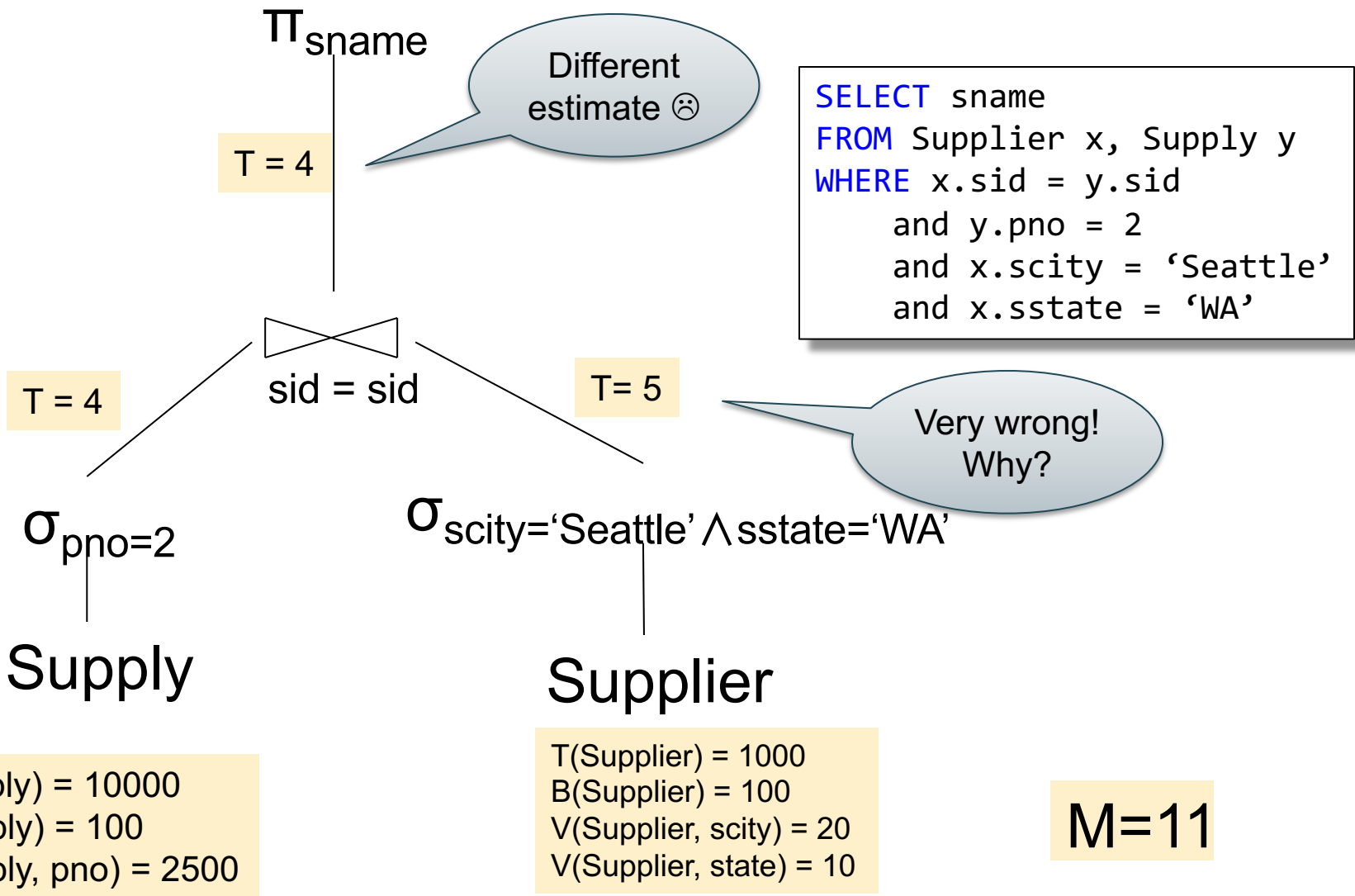
T(Supply) = 10000
B(Supply) = 100
V(Supply, pno) = 2500

T(Supplier) = 1000
B(Supplier) = 100
V(Supplier, scity) = 20
V(Supplier, state) = 10

M=11

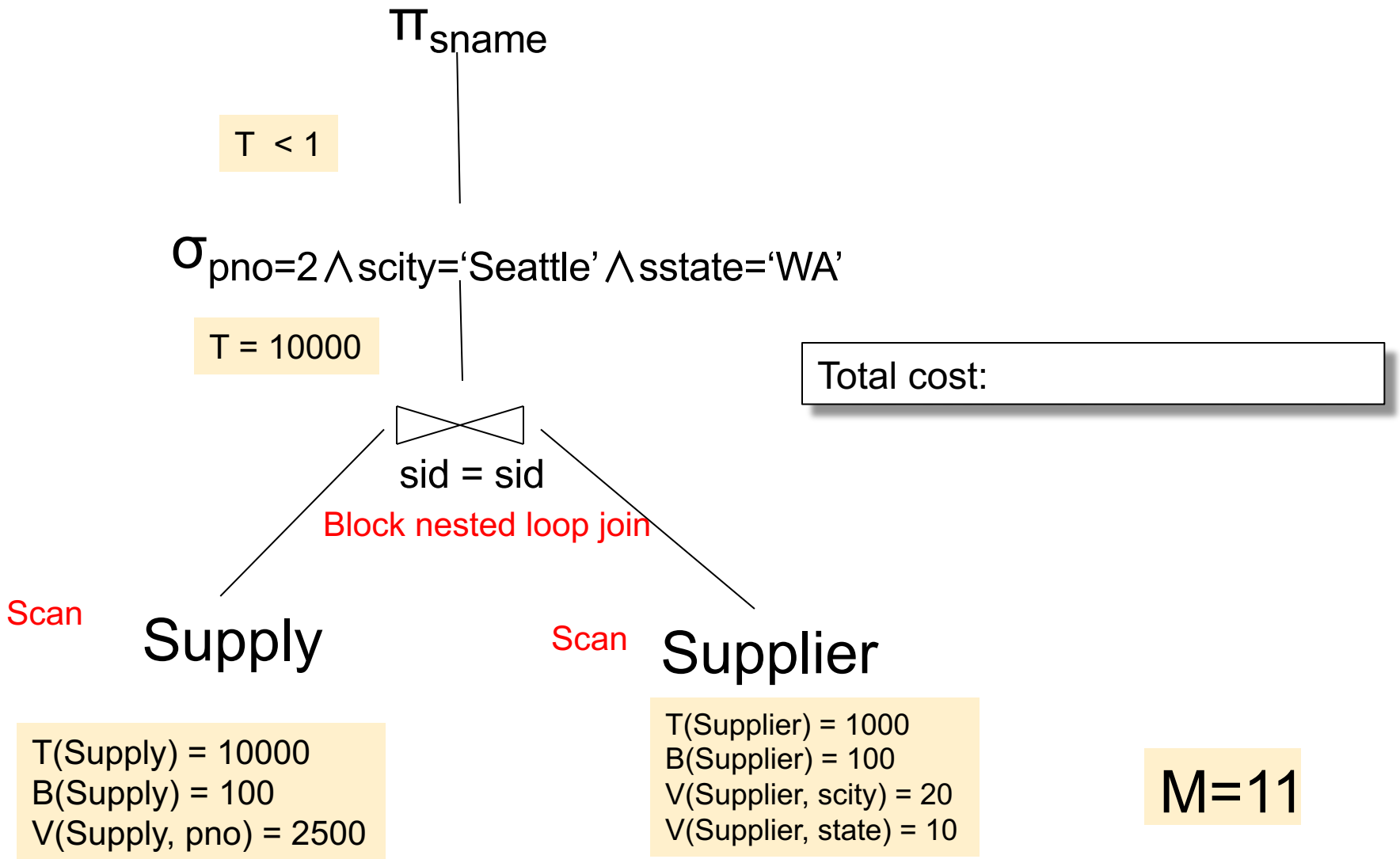
Supplier(sid, sname, scity, sstate)
Supply(sid, pno, quantity)

Logical Query Plan 2



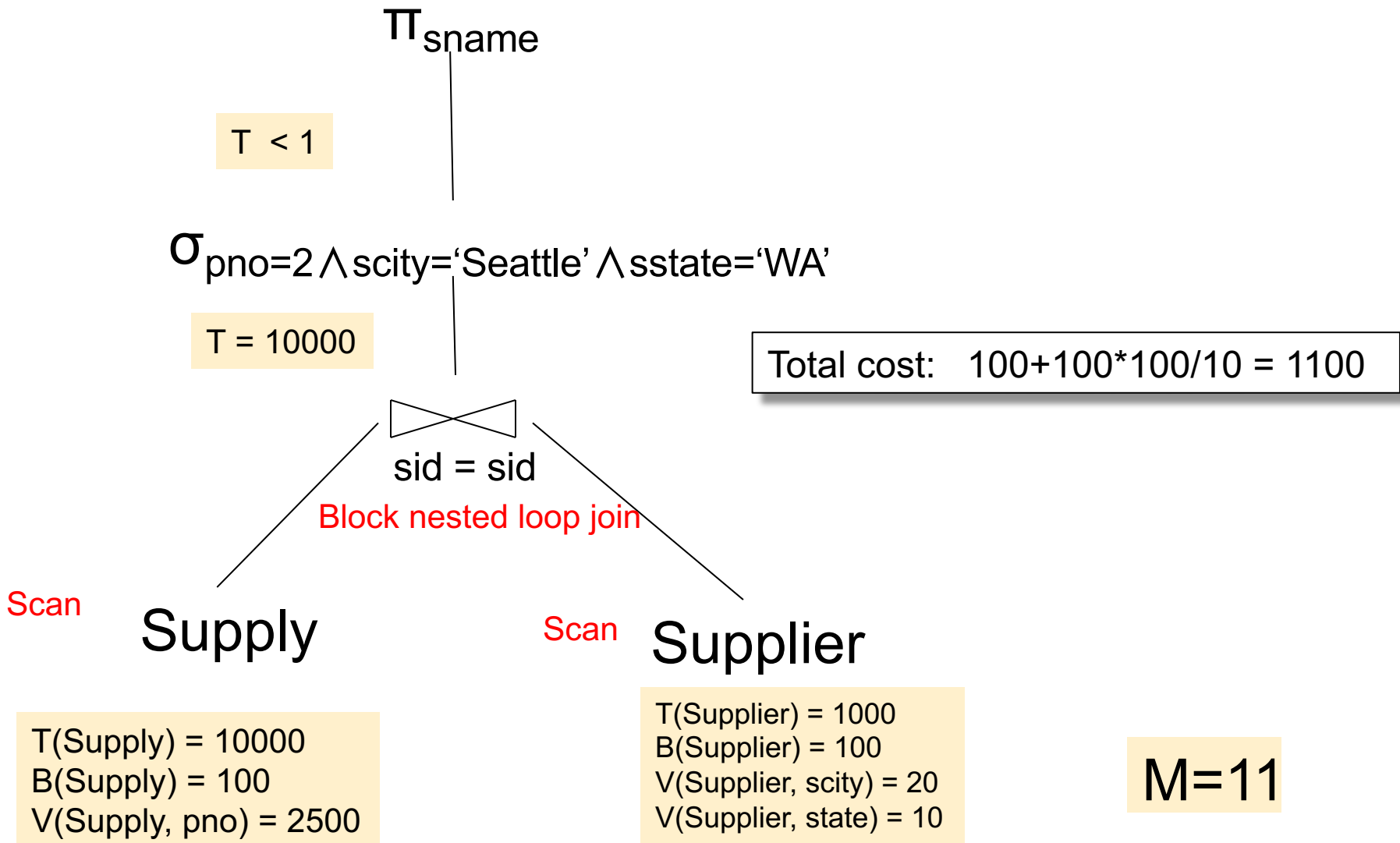
Supplier(sid, sname, scity, sstate)
Supply(sid, pno, quantity)

Physical Plan 1



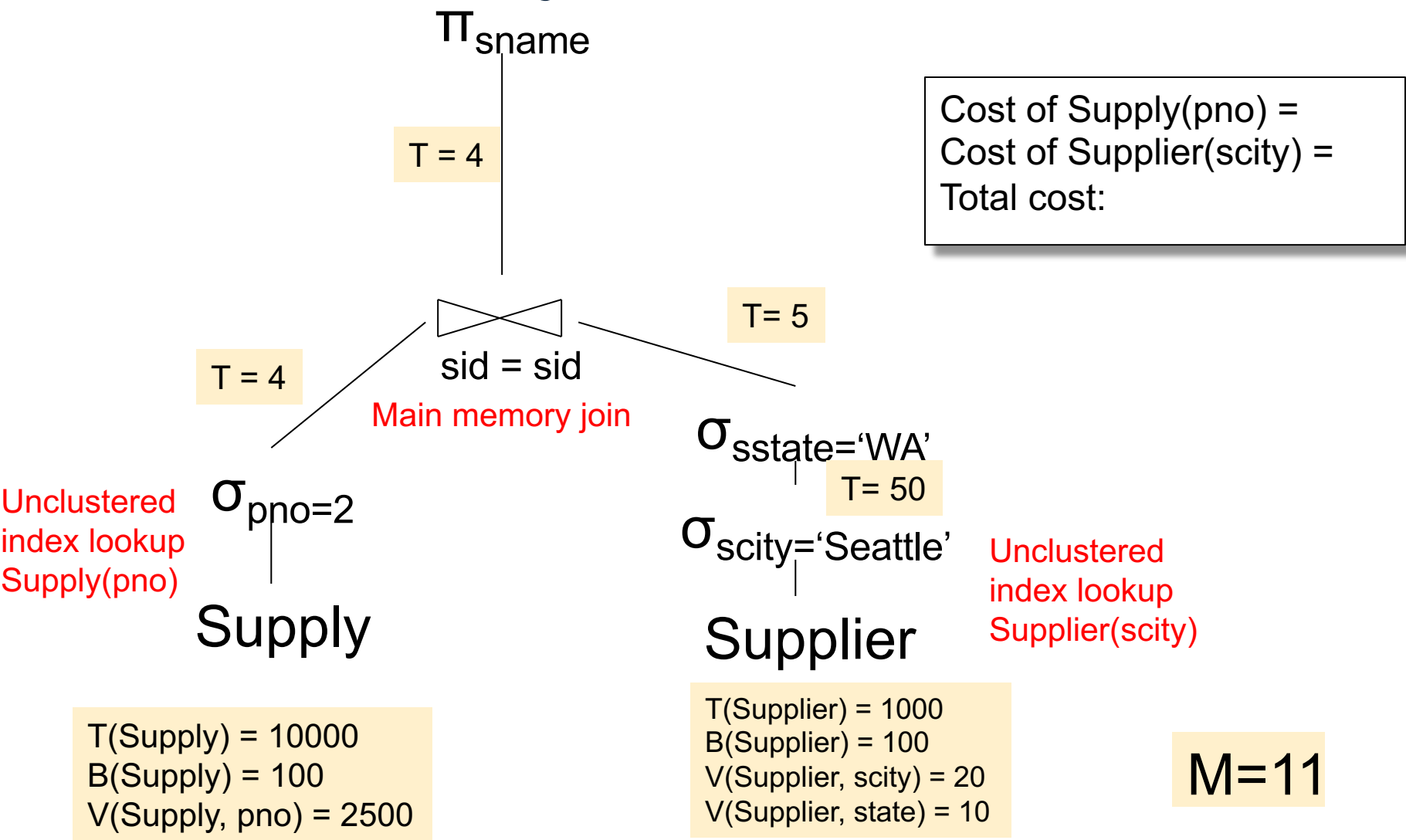
Supplier(sid, sname, scity, sstate)
Supply(sid, pno, quantity)

Physical Plan 1



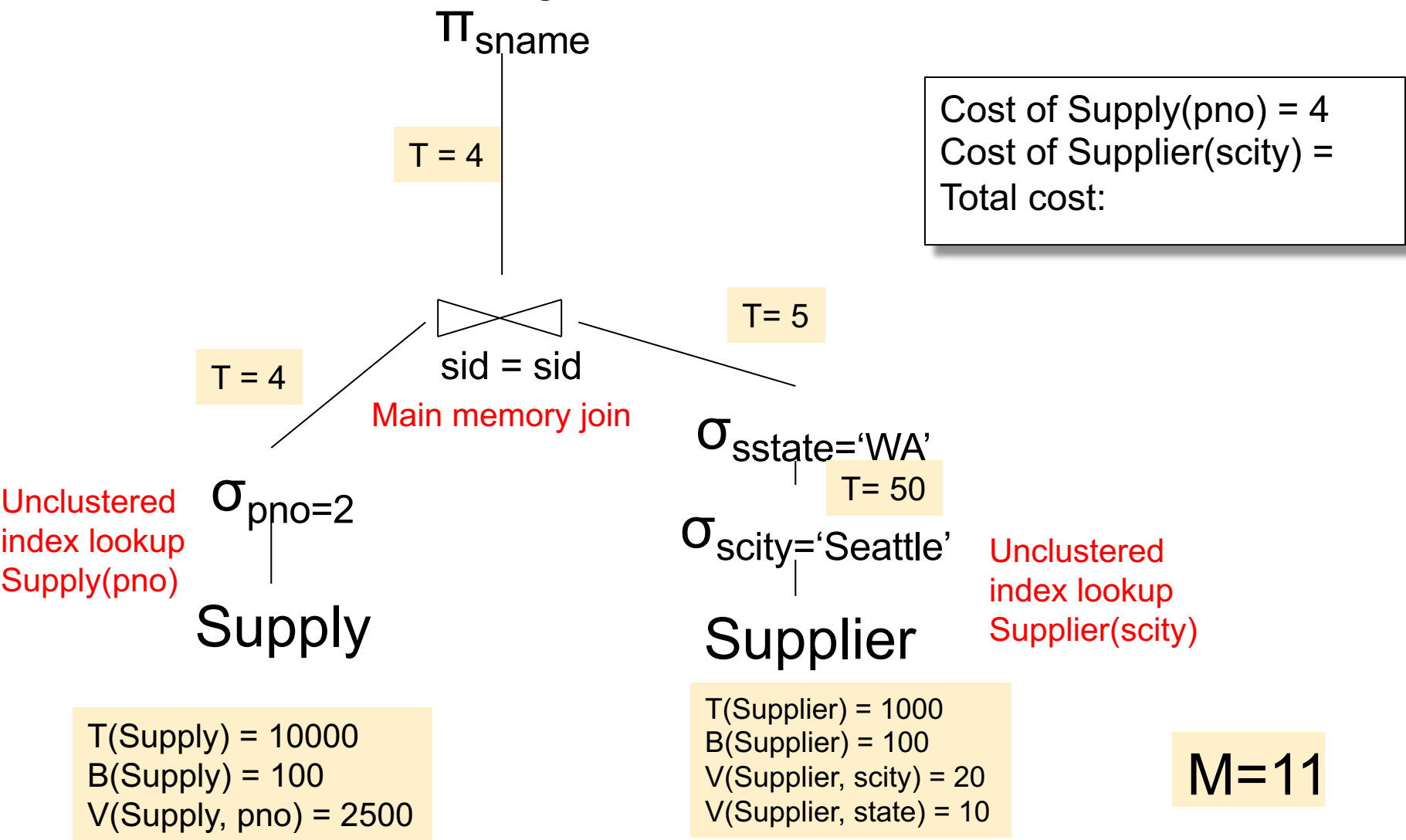
Supplier(sid, sname, scity, sstate)
Supply(sid, pno, quantity)

Physical Plan 2



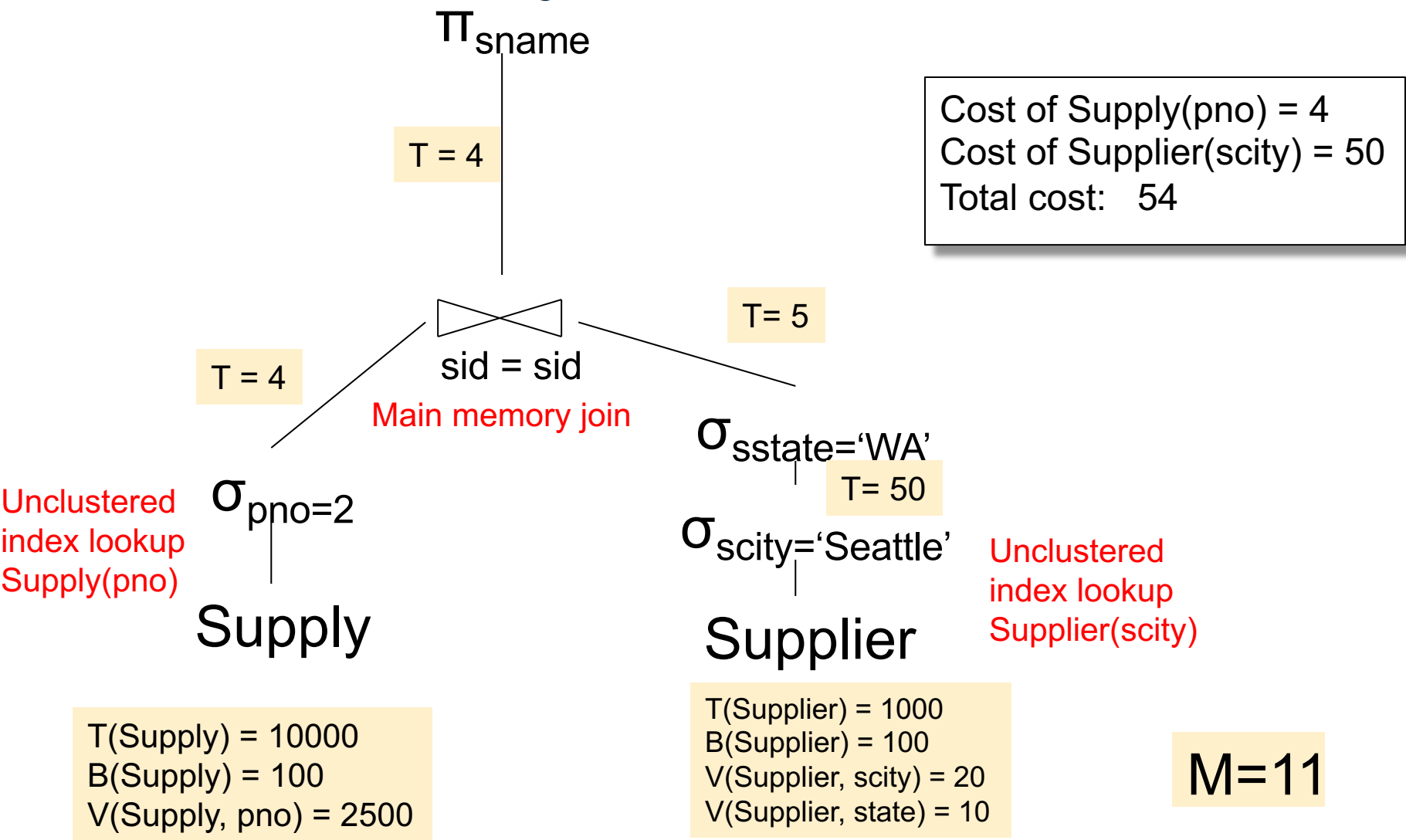
Supplier(sid, sname, scity, sstate)
Supply(sid, pno, quantity)

Physical Plan 2



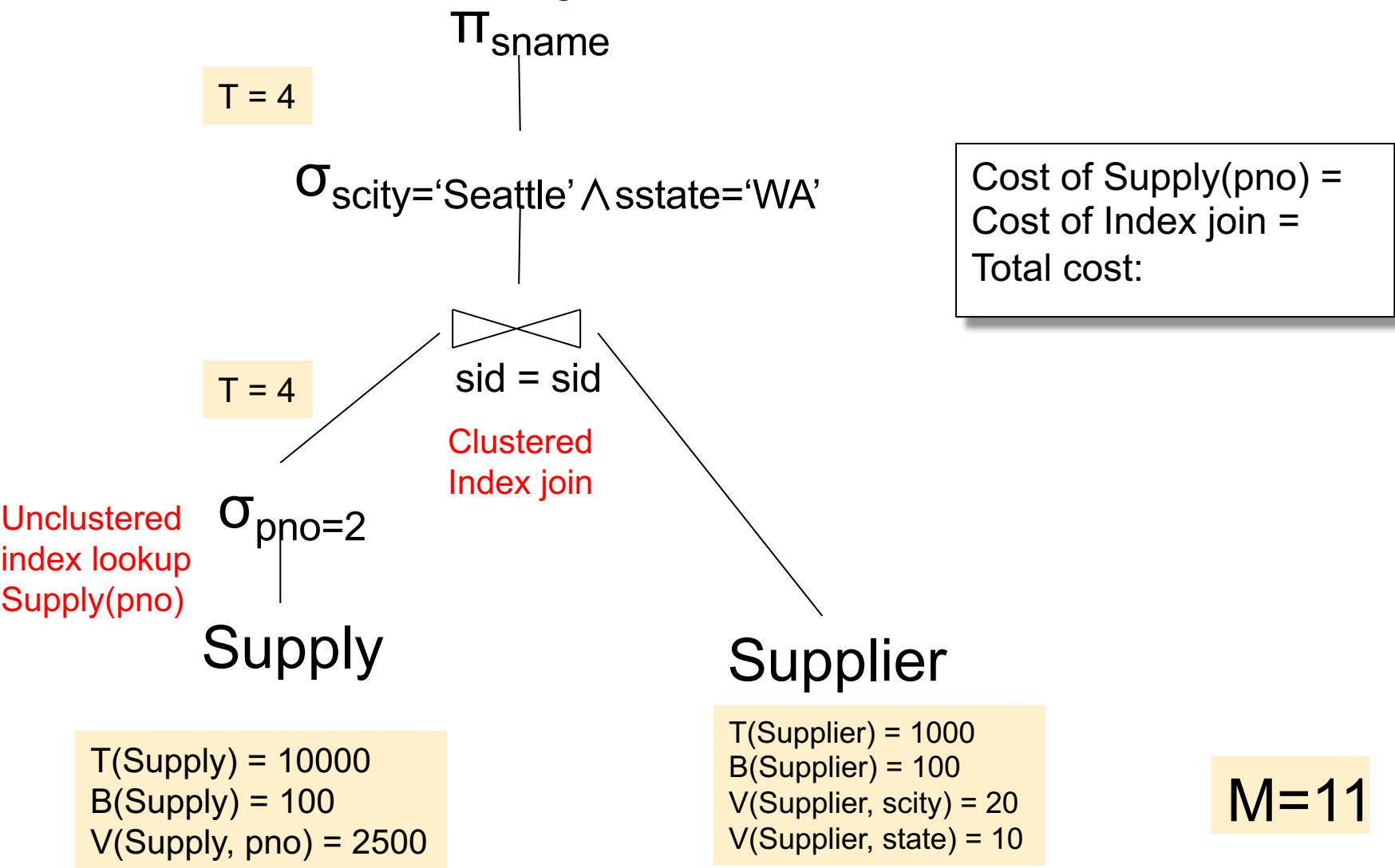
Supplier(sid, sname, scity, sstate)
Supply(sid, pno, quantity)

Physical Plan 2



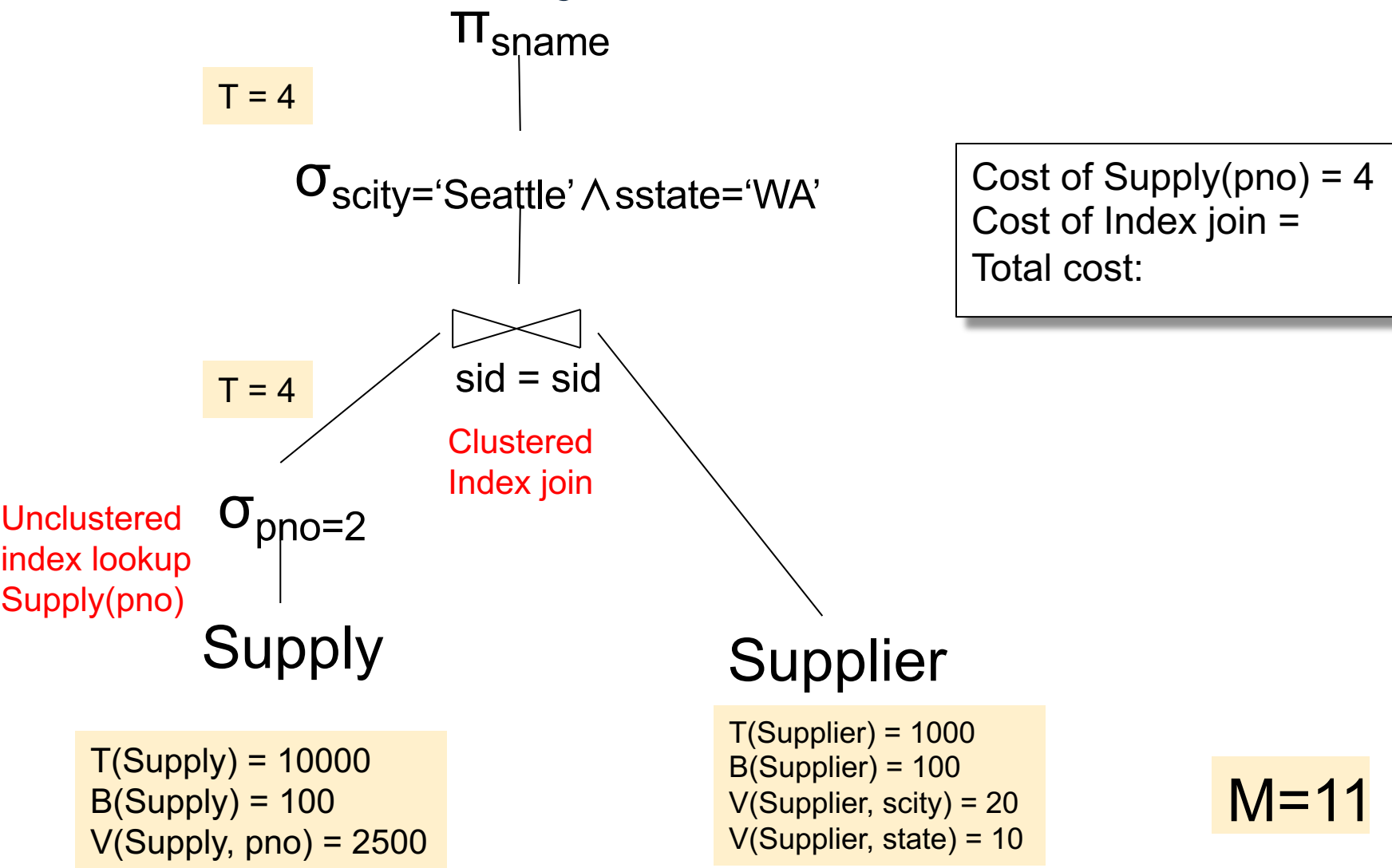
Supplier(sid, sname, scity, sstate)
Supply(sid, pno, quantity)

Physical Plan 3



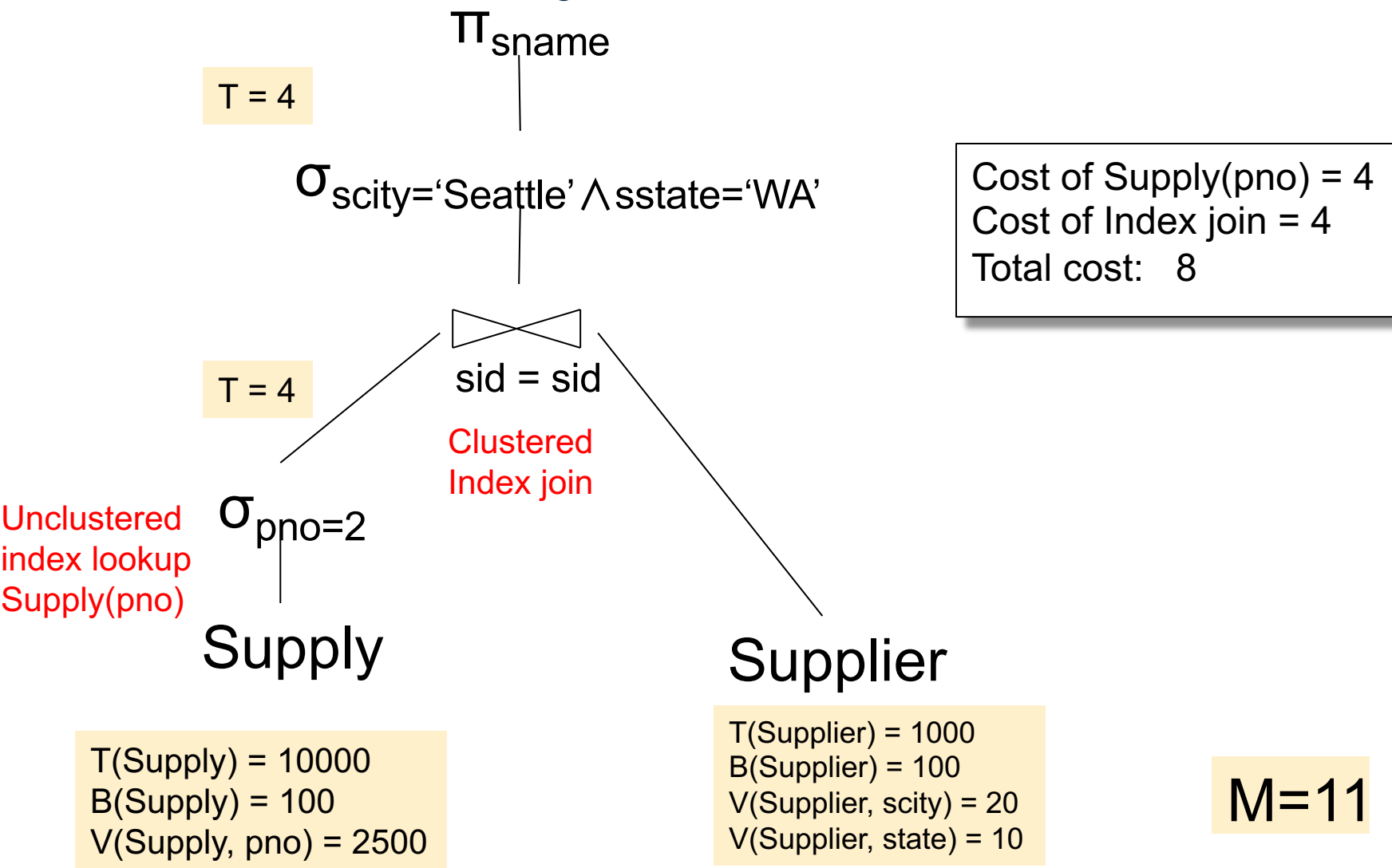
Supplier(sid, sname, scity, sstate)
Supply(sid, pno, quantity)

Physical Plan 3



Supplier(sid, sname, scity, sstate)
Supply(sid, pno, quantity)

Physical Plan 3



Histograms

- Relax uniformity assumption:
$$T(\sigma_{A=v}(R)) = T(R) / V(R,A)$$
- Histogram:
 - Partition R into buckets by the values of A
 - For each bucket, store T(bucket) and other stats
- RDBMS maintain histograms on some attributes of some tables; recomputed periodically using sampling

Histograms

Employee(ssn, name, age)

$T(\text{Employee}) = 25000$, $V(\text{Employee}, \text{age}) = 50$
 $\min(\text{age}) = 19$, $\max(\text{age}) = 68$

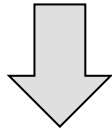
$\sigma_{\text{age}=48}(\text{Employee}) = ?$ $\sigma_{\text{age}>28 \text{ and } \text{age}<35}(\text{Employee}) = ?$

Histograms

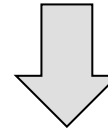
Employee(ssn, name, age)

$T(\text{Employee}) = 25000$, $V(\text{Employee}, \text{age}) = 50$
 $\min(\text{age}) = 19$, $\max(\text{age}) = 68$

$\sigma_{\text{age}=48}(\text{Employee}) = ?$ $\sigma_{\text{age}>28 \text{ and } \text{age}<35}(\text{Employee}) = ?$



Estimate = $25000 / 50 = 500$



Estimate = $25000 * 6 / 50 = 3000$

Histograms

Employee(ssn, name, age)

$T(\text{Employee}) = 25000$, $V(\text{Employee}, \text{age}) = 50$
 $\min(\text{age}) = 19$, $\max(\text{age}) = 68$

$\sigma_{\text{age}=48}(\text{Employee}) = ?$ $\sigma_{\text{age}>28 \text{ and } \text{age}<35}(\text{Employee}) = ?$

Age:	0-20	20-29	30-39	40-49	50-59	> 60
Tuples	200	800	5000	12000	6500	500

Histograms

Employee(ssn, name, age)

$T(\text{Employee}) = 25000$, $V(\text{Employee}, \text{age}) = 50$
 $\min(\text{age}) = 19$, $\max(\text{age}) = 68$

$\sigma_{\text{age}=48}(\text{Employee}) = ?$ $\sigma_{\text{age}>28 \text{ and } \text{age}<35}(\text{Employee}) = ?$

Age:	0..20	20..29	30-39	40-49	50-59	> 60
Tuples	200	800	5000	12000	6500	500

Estimate = 1200

Estimate = $1 \cdot 80 + 5 \cdot 500 = 2580$

Types of Histograms

- How should we determine the bucket boundaries in a histogram?

Types of Histograms

- How should we determine the bucket boundaries in a histogram?
- Eq-Width
- Eq-Depth
- Compressed
- V-Optimal histograms

Histograms

Employee(ssn, name, age)

Eq-width:

Age:	0..20	20..29	30-39	40-49	50-59	> 60
Tuples	200	800	5000	12000	6500	500

Eq-depth:

Age:	0-33	33-38	38-43	43-45	45-54	> 54
Tuples	1800	2000	2100	2200	1900	1800

Compressed: store separately highly frequent values: (48,1900)

V-Optimal Histograms

- Defines bucket boundaries in an optimal way, to minimize the error over all point queries
- Computed rather expensively, using dynamic programming
- Modern databases systems use V-optimal histograms or some variations

Difficult Questions on Histograms

- Small number of buckets
 - Hundreds, or thousands, but not more
 - WHY ?
- *Not* updated during database update, but recomputed periodically
 - WHY ?
- Multidimensional histograms rarely used
 - WHY ?

Difficult Questions on Histograms

- Small number of buckets
 - Hundreds, or thousands, but not more
 - WHY? All histograms are kept in main memory during query optimization; plus need fast access
- *Not updated during database update, but recomputed periodically*
 - WHY? Histogram update creates a write conflict; would dramatically slow down transaction throughput
- Multidimensional histograms rarely used
 - WHY? Too many possible multidimensional histograms, unclear which ones to choose