## CSE 444: Database Internals

Lecture 8 Operator Algorithms (part 2)
for each page of tuples $r$ in $R$ do
for each page of tuples $r$ in R do
for each page of tuples $s$ in $S$ do
for all pairs of tuples $t_{1}$ in $r, t_{2}$ in s
if $t_{1}$ and $t_{2}$ join then output ( $t_{1}, t_{2}$ )
What is the Cost?
- Cost: $B(R)+B(R) B(S)$
What is the Cost?


## Page-at-a-time Refinement




Block-Nested-Loop Refinement
for each group of $M-1$ pages $r$ in $R$ do for each page of tuples $s$ in S do
for each page of tuples $s$ in $S$ do
for all pairs of tuples $t_{1}$ in $r, t_{2}$ in $s$
if $t_{1}$ and $t_{2}$ join then output $\left(t_{1}, t_{2}\right)$

What is the Cost?


Block Memory Refinement


## Block Memory Refinement




## Block Memory Refinement



Block-Nested-Loop Refinement
for each group of M-1 pages $r$ in $R$ do for each page of tuples $s$ in $S$ do
for all pairs of tuples $t_{1}$ in $r, t_{2}$ in $s$ if $t_{1}$ and $t_{2}$ join then output $\left(t_{1}, t_{2}\right)$

- Cost: $B(R)+B(R) B(S) /(M-1) \quad$ What is the Cost?


## Sort-Merge Join

Sort-merge join: $R \bowtie S$

- Scan R and sort in main memory
- Scan S and sort in main memory
- Merge R and S
- Cost: $B(R)+B(S)$
- One pass algorithm when $B(S)+B(R)<=M$
- Typically, this is NOT a one pass algorithm


## Sort-Merge Join Example

Step 3: Merge Patient and Insurance


Sort-Merge Join Example
Step 1: Scan Patient and sort in memory
Memory $M=21$ pages
1/2 344 5/6|89

Patient Insurance

| 1 | 2 |
| :--- | :--- |


| 1 | 4 |
| :--- | :--- |

2466

| 4 | 3 | 1 | 3 |
| :--- | :--- | :--- | :--- |


| 2 | 8 |
| :--- | :--- |
|  | 8 |

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## Sort-Merge Join Example

Step 3: Merge Patient and Insurance


## Outline

- Join operator algorithms
- One-pass algorithms (Sec. 15.2 and 15.3)
- Index-based algorithms (Sec 15.6)
- Two-pass algorithms (Sec 15.4 and 15.5)



## Index Based Selection

Selection on equality: $\sigma_{a=v}(R)$

- $B(R)=$ size of $R$ in blocks
- $T(R)=$ number of tuples in $R$
- $V(R, a)=\#$ of distinct values of attribute a


## Index Based Selection

Selection on equality: $\sigma_{a=v}(R)$

- $B(R)=$ size of $R$ in blocks
- $T(R)=$ number of tuples in $R$
- $V(R, a)=\#$ of distinct values of attribute a

What is the cost in each case?

- Clustered index on $a: \quad B(R) / V(R, a)$
- Unclustered index on a:


## Index Based Selection

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What is the cost in each case?

- Clustered index on a: $\quad B(R) / V(R, a)$
- Unclustered index on $a: \quad T(R) / V(R, a)$


## Index Based Selection

Selection on equality: $\sigma_{a=v}(R)$

- $B(R)=$ size of $R$ in blocks
- $T(R)=$ number of tuples in $R$
- $V(R, a)=\#$ of distinct values of attribute a

What is the cost in each case?

- Clustered index on a: $\quad B(R) / V(R, a)$
- Unclustered index on a: $T(R) / V(R, a)$

Note: we ignore I/O cost for index pages

## Index Based Selection

- Example: $\begin{aligned} & B(R)=2000 \\ & T(R)=100,000 \\ & V(R, a)=20\end{aligned}$
cost of $\sigma_{a=v}(R)=$ ?
$V(R, a)=20$
- Table scan: $B(R)=2,000 \mathrm{I} / \mathrm{Os}$
- Index based selection:


## Index Based Selection

- Example: | $B(R)=2000$ |
| :--- |
| $T(R)=100,000$ |
| $V(R, ~ a)=20$ | cost of $\sigma_{a-v}(\mathrm{R})=$ ?
- Table scan: $B(R)=2,000$ I/Os
- Index based selection:
- If index is clustered: $B(R) / V(R, a)=100 \mathrm{I} / \mathrm{Os}$
- If index is unclustered:


## Index Based Selection

- Example: $\begin{aligned} & B(R)=2000 \\ & T(R)=100,000 \\ & V(R, a)=20\end{aligned}$
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## Index Based Selection

- Example: | $B(R)=2000$ |
| :--- | :--- |
| $T(R)=100,000$ |
| $V(R, a)=20$ |$\quad$ cost of $\sigma_{a-v}(R)=$ ?
- Table scan: $B(R)=2,000 \mathrm{I} / \mathrm{Os}$
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## Index Based Selection

- Example: $\begin{aligned} & \mathrm{B}(\mathrm{R})=2000 \\ & \mathrm{~T}(\mathrm{R})=100,000 \\ & \mathrm{~V}(\mathrm{R}, \mathrm{a})=20\end{aligned} \quad$ cost of $\sigma_{\mathrm{a}-\mathrm{v}}(\mathrm{R})=$ ?
- Table scan: $B(R)=2,000 \mathrm{I} / \mathrm{Os}$
- Index based selection:
- If index is clustered: $B(R) / V(R, a)=100 \mathrm{I} / \mathrm{Os}$
- If index is unclustered: $T(R) / V(R, a)=5,000 \mathrm{I} / \mathrm{Os}$

Index Based Selection

- Example: | $B(R)=2000$ |
| :--- | :--- |
| $T(R)=100,000 \quad$ cost of $\sigma_{a-v}(R)=$ ? |

$V(R, a)=20$

- Table scan: $B(R)=2,000$ I/Os !
- Index based selection:
- If index is clustered: $B(R) / N(R, a)=100 I / O s$
- If index is unclustered: $T(R) / V(R, a)=5,000 I / O s$ !


## Index Nested Loop Join

$R \bowtie S$

- Assume $S$ has an index on the join attribute
- Iterate over R, for each tuple fetch corresponding tuple(s) from $S$
- Previous nested loop join: cost $-B(R)+T(R) * B(S)$
- Index Nested Loop Join Cost:
- If index on $S$ is clustered: $B(R)+T(R) B(S) / V(S, a)$
- If index on $S$ is unclustered: $B(R)+T(R) T(S) / V(S, a)$


## Two-Pass Algorithms

- Fastest algorithm seen so far is one-pass hash join What if data does not fit in memory?
- Need to process it in multiple passes
- Two key techniques
- Sorting
- Hashing


## Index Based Selection

- Example: | $\begin{array}{l}B(R)=2000 \\ T(R)=100,000\end{array} \quad$ cost of $\sigma_{a-v}(R)=$ ? |
| :--- |
| $(R$, |

$V(R, a)=20$

- Table scan: $B(R)=2,000 I / O s$
- Index based selection:
- If index is clustered: $B(R) / V(R, a)=100 I / O s$
- If index is unclustered: $T(R) / N(R, a)=5,000 \mathrm{I} / \mathrm{Os}$

Lesson: Don't build unclustered indexes when $\mathrm{V}(\mathrm{R}, \mathrm{a})$ is small !

## Outline

- Join operator algorithms
- One-pass algorithms (Sec. 15.2 and 15.3)
- Index-based algorithms (Sec 15.6)
- Two-pass algorithms (Sec 15.4 and 15.5)


## Basic Terminology

- A run in a sequence is an increasing subsequence
- What are the runs?
$2,4,99,103,88,77,3,79,100,2,50$


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$2,4,99,103,|88,|77,|3,79,100| 2,50$,



## External Merge-Sort: Step 2

Phase two: merge $M$ runs into a bigger run

- Merge M-1 runs into a new run
- Result: runs of length $M(M-1) \approx M^{2}$


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## Example

- Merging three runs to produce a longer run:
$0,14,33,88,92,192,322$
2, 4, 7, 43, 78, 103, 523
1, 6, 9, 12, 33, 52, 88, 320
Output:
0


## Example

- Merging three runs to produce a longer run:

0, 14, 33, 88, 92, 192, 322
2, 4, 7, 43, 78, 103, 523
1, 6, 9, 12, 33, 52, 88, 320
Output:
0 ,?

## Example

- Merging three runs to produce a longer run:

0, 14, 33, 88, 92, 192, 322
2, 4, 7, 43, 78, 103, 523
$1,6, \mathbf{9}, \mathbf{1 2}, \mathbf{3 3}, \mathbf{5 2}, \mathbf{8 8}, \mathbf{3 2 0}$
Output:
$0,1,2,4,6,7$, ?

## External Merge-Sort: Step 2

## Cost of External Merge Sort

Phase two: merge M runs into a bigger run

- Merge $\mathrm{M}-1$ runs into a new run
- Result: runs of length $M(M-1) \approx M^{2}$


If approx. $\mathrm{B}<=\mathrm{M}^{2}$ then we are done 53

## Discussion

- What does $B(R)<=M^{2}$ mean?
- How large can R be?


## Discussion

- What does $B(R)<=M^{2}$ mean?
- How large can R be?
- Example:
- Page size $=32 \mathrm{~KB}$
- Memory size 32GB: $\mathrm{M}=10^{6}$ pages
- $R$ can be as large as $10^{12}$ pages
$-32 \times 10^{15}$ Bytes $=32$ PB
Join $R \bowtie S$
- How?....


## Merge-Join

- What does $B(R)<=M^{2}$ mean?
- How large can R be?
- Example:
- Page size = 32KB
- Memory size 32GB: $M=10^{6}$-pages

|  | Merge-Join <br> Join R $\bowtie$ S <br> - How?.... |
| :---: | :---: |


| Merge-Join Example |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Setup: Want to join R and S <br> - Relation $R$ has 10 pages with 2 tuples per page <br> - Relation $S$ has 8 pages with 2 tuples per page <br> Values shown are values of join attribute for each given tuple |  |  |  |  |  |
|  |  |  |  |  |  |
|  |  |  |  |  |  |
|  |  |  |  |  |  |
| Disk |  |  |  |  |  |
| R S |  |  |  | Memory M = 5 pages |  |
| 4 1 | 17 | 3 | 0 |  |  |
| 5 2 | 119 | 1 | 7 |  |  |
| 3 4 |  | 4 | 3 |  |  |
| 8 6 |  | 2 | 5 |  |  |
| 7 9 |  | 9 | 8 |  |  |
| 12 14 <br>   |  |  | 9 |  |  |
| 5 11 <br> 2  |  | 12 | 11 |  |  |
| 2 3 |  |  |  |  |  |
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## Merge-Join Example

Step 1: Do the same with S







## Announcements

- Lab 2 / part 1 due on Thursday
- We will not run any tests - So bugs are OK
- Homework 2 due on Friday
- Paper review for master's due on Friday



## Partitioned Hash Algorithms

- Partition R it into k buckets:
$R_{1}, R_{2}, R_{3}, \ldots, R_{k}$


## Partitioned Hash Algorithms

- Partition R it into k buckets: $R_{1}, R_{2}, R_{3}, \ldots, R_{k}$
- Assuming $B\left(R_{1}\right)=B\left(R_{2}\right)=\ldots=B\left(R_{k}\right)$, we have $B\left(R_{i}\right)=B(R) / k$, for all $i$
- Goal: each $\mathrm{R}_{\mathrm{i}}$ should fit in main memory: $B\left(R_{i}\right) \leq M \quad$ How do we choose $k$ ?


## Partitioned Hash Algorithms

- Partition R it into k buckets:
$R_{1}, R_{2}, R_{3}, \ldots, R_{k}$
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## Partitioned Hash Algorithms

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- Goal: each $\mathrm{R}_{\mathrm{i}}$ should fit in main memory: $B\left(R_{i}\right) \leq M$


## Partitioned Hash Algorithms

- We choose $k=M-1$ Each bucket has size approx. $B(R) /(M-1) \approx B(R) / M$



## Partitioned Hash Algorithms

- We choose $\mathrm{k}=\mathrm{M}-1$ Each bucket has size approx. $B(R) /(M-1) \approx B(R) / M$


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## Grace-Join

$R \bowtie S$

- Step 1:

Note: grace-join is also called

- Hash S into M-1 buckets partitioned hash-join
- Send all buckets to disk
- Step 2
- Hash R into M-1 buckets
- Send all buckets to disk
- Step 3
- Join every pair of buckets


## Partitioned Hash-Join Example

Step 1: Read relation $S$ one page at a time and hash into $M-1$ (=4 buckets)


## Partitioned Hash-Join Example

Partitioned Hash-Join Example

Step 1: Read relation S one page at a time and hash into the 4 buckets


| Partitioned Hash-Join Example <br> Step 1: Read relation $S$ one page at a time and hash into the 4 buckets |  |  |
| :---: | :---: | :---: |
|  |  |  |

## Partitioned Hash-Join Example

Step 1: Read relation S one page at a time and hash into the 4 buckets
When a bucket fills up, flush it to disk


## Partitioned Hash-Join Example

Step 1: Read relation S one page at a time and hash into the 4 buckets
When a bucket fills up, flush it to disk

|  |  |  |  | Memory $\mathrm{M}=5$ pages | $\longrightarrow$ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| R | S |  |  |  |  |  |  |
| 1 | $1{ }^{1} 7$ | 3 | 0 | Hash h: value \% 4 |  |  |  |
| 5 2 | 11.9 | 1 | 7 | 0 4 |  |  |  |
| 3 4 |  | 4 | 3 |  3 1 1 |  |  |  |
| 8 6 |  | 2 | 5 | Input buffer $2 \square$ |  |  |  |
| 7 9 |  | 9 | 8 | $3 \square$ | 3 |  |  |
| 12 14 <br> 5  |  | 11 | 9 |  |  |  |  |
| 5 11 <br> 2  |  | 12 | 1 |  |  |  |  |
| 2 3 |  | 5 | 7 |  |  |  |  |
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Partitioned Hash-Join Example

Step 1: Read relation S one page at a time and hash into the 4 buckets When a bucket fills up, flush it to disk


## Partitioned Hash-Join Example

Step 2: Read relation $R$ one page at a time and hash into same 4 buckets



- Cost: 3B(R) + 3B(S)
- Assumption: $\min (\mathrm{B}(\mathrm{R}), \mathrm{B}(\mathrm{S}))<=\mathrm{M}^{2}$


## Hybrid Hash Join Algorithm

- Partition S into k buckets
$t$ buckets $S_{1}, \ldots, S_{t}$ stay in memory
$k$-t buckets $\mathrm{S}_{\mathrm{t}+1}, \ldots, \mathrm{~S}_{\mathrm{k}}$ to disk
- Partition R into k buckets
- First t buckets join immediately with S
- Rest k-t buckets go to disk
- Finally, join k-t pairs of buckets:
$\left(R_{t+1}, S_{t+1}\right),\left(R_{t+2}, S_{t+2}\right), \ldots,\left(R_{k}, S_{k}\right)$



## Hybrid Join Algorithm

- How to choose $k$ and $t$ ?


## Hybrid Join Algorithm

- How to choose k and t ?
- Choose k large but s.t. $k<=M$
- Choose k large but s.t.


Hybrid Join Algorithm

- How to choose k and t?


## Hybrid Join Algorithm

- How to choose k and t ?
- Choose k large but s.t. One block/bucket in memory
$\mathrm{k}<=\mathrm{M}$
- Choose $t / k$ large but s.t. $\quad t / k * B(S)<=M$


## Hybrid Join Algorithm

- How to choose k and t ?
- Choose k large but s.t.
- Choose t/k large but s.t.



## Hybrid Join Algorithm

- How to choose k and t?
- Choose k large but s.t.
- Choose t/k large but s.t.
- Together:
$t / k * B(S)+k-t<=M$


## Hybrid Join Algorithm

- How to choose k and t?
- Choose k large but s.t.
- Choose t/k large but s.t.
k <= M
First t buckets in memory
- Choose t/k large but s.t.
$t / k$ * $B(S)<=M$
- Together:
$t / k$ * $B(S)+k-t<=M$
- Assuming $\mathrm{t} / \mathrm{k}$ * $\mathrm{B}(\mathrm{S}) \gg \mathrm{k}-\mathrm{t}$ : $\mathrm{t} / \mathrm{k}=\mathrm{M} / \mathrm{B}(\mathrm{S})$

Total size of first t buckets
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## Hybrid Join Algorithm

Even better: adjust t dynamically

- Start with $\mathrm{t}=\mathrm{k}$ : all buckets are in main memory
- Read blocks from S, insert tuples into buckets
- When out of memory:
- Send one bucket to disk
- $\mathrm{t}:=\mathrm{t}-1$
- Worst case.
- All buckets are sent to disk ( $\mathrm{t}=0$ )
- Hybrid join becomes grace join


## Hybrid Join Algorithm

Cost of Hybrid Join:

- Grace join: 3B(R) + 3B(S)
- Hybrid join:
- Saves $2 \mathrm{I} / \mathrm{Os}$ for $\mathrm{t} / \mathrm{k}$ fraction of buckets
- Saves 2t/k(B(R) + B(S)) I/Os
- Cost:
$(3-2 \mathrm{t} / \mathrm{k})(\mathrm{B}(\mathrm{R})+\mathrm{B}(\mathrm{S}))=(3-2 \mathrm{M} / \mathrm{B}(\mathrm{S})(\mathrm{B}(\mathrm{R})+\mathrm{B}(\mathrm{S}))$


## Hybrid Join Algorithm

- How to choose k and t ?
- Choose k large but s.t.
- Choose t/k large but s.t.
$t / k$ * $B(S)<=M$
- Together:
$t / k$ * $B(S)+k-t<=M$



## Hybrid Join Algorithm

- What is the advantage of the hybrid algorithm?


## Summary of External Join Algorithms

- Block Nested Loop: $\mathrm{B}(\mathrm{S})+\mathrm{B}(\mathrm{R})^{*} \mathrm{~B}(\mathrm{~S}) /(\mathrm{M}-1)$
- Index Join: $B(R)+T(R) B(S) / V(S, a)$
(unclustered)
- Partitioned Hash: 3B(R)+3B(S);
$-\min (B(R), B(S))<=M^{2}$
- Merge Join: $3 B(R)+3 B(S)$
$-B(R)+B(S)<=M^{2}$
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## Hybrid Join Algorithm

- What is the advantage of the hybrid algorithm?

It degrades gracefully when $S$ larger than $M$ :

- When $B(S)<=M$
- Main memory hash-join has cost $B(R)+B(S)$
- When $B(S)>M$
- Grace-join has cost $3 \mathrm{~B}(\mathrm{R})+3 \mathrm{~B}(\mathrm{~S})$
- Hybrid join has cost $(3-2 t / k)(B(R)+B(S))$


## Summary of Query Execution

- For each logical query plan
- There exist many physical query plans
- Each plan has a different cost
- Cost depends on the data
- Additionally, for each query
- There exist several logical plans
- Next lecture: query optimization
- How to compute the cost of a complete plan?
- How to pick a good query plan for a query?

