

# CSE 444: Database Internals

## Lecture 12 Query Optimization (part 3)

# Acknowledgments

Today's lecture focuses on how to actually implement the Selinger optimizer

Designed to help you with Lab 5

Many slides from Sam Madden at MIT

# Selinger Optimizer

## Problem:

- How to order a series of joins over N tables A,B,C,...  
E.g.  $A.a = B.b \text{ AND } A.c = D.d \text{ AND } B.e = C.f$
- $N!$  ways to order joins; e.g. ABCD, ACBD, ....
- $C_{N-1} = \frac{1}{N} \binom{2(N-1)}{N-1}$  plans/ordering; e.g. (((AB)C)D), ((AB)(CD)))
- Multiple implementations (hash, nested loops)
- Naïve approach does not scale
  - E.g.  $N = 20$ , #join orders  $20! = 2.4 \times 10^{18}$ ; many more plans

# Selinger Optimizer

- Only **left-deep plan**:  $((AB)C)D$  – eliminate  $C_{N-1}$ .
- Push down selections
- Don't consider cartesian products
- Dynamic programming algorithm

# Dynamic Programming

OrderJoins:

$R$  = set of relations to join

For  $d = 1$  to  $N$ : /\* where  $N = |R|$  \*/

For  $S$  in {all size- $d$  subsets of  $R$ }:

**optjoin**( $S$ ) =  $(S - a)$  join  $a$ ,

where  $a$  is the single relation that minimizes:

$\text{cost}(\text{optjoin}(S - a)) +$

min.cost to join  $(S - a)$  with  $a$  +

min.access cost for  $a$

SimpleDB Lab5:  
you implement **orderJoins**

Use: **enumerateSubsets**

Use:  
**computerCostAndCardOfSubplan**

Note: **optjoin**( $S-a$ ) is cached from previous iterations

# Example

- **orderJoins(A, B, C, D)**
- Assume all joins are NL

Subplan S	optJoin(S)	Cost(OptJoin(S))
A		

# Example

- **orderJoins(A, B, C, D)**
- Assume all joins are NL
- $d = 1$ 
  - A = best way to access A  
(sequential scan, predicate-pushdown on index, etc)
  - B = best way to access B
  - C = best way to access C
  - D = best way to access D
- Total number of steps: choose(N, 1)

Subplan S	optJoin(S)	Cost(OptJoin(S))
A	Index scan	100
B	Seq. scan	50
C	Seq scan	120
D	B+tree scan	400

# Example

- **orderJoins(A, B, C, D)**
- $d = 2$ 
  - $\{A,B\} = AB \text{ or } BA$   
use previously computed  
best way to access A and B

Subplan S	optJoin(S)	Cost(OptJoin(S))
A	Index scan	100
B	Seq. scan	50
...		

# Example

- **orderJoins(A, B, C, D)**
- $d = 2$ 
  - $\{A, B\} = AB \text{ or } BA$   
use previously computed  
best way to access A and B

Subplan S	optJoin(S)	Cost(OptJoin(S))
A	Index scan	100
B	Seq. scan	50
...		
{A, B}	BA	156

# Example

- **orderJoins(A, B, C, D)**
- $d = 2$ 
  - $\{A, B\} = AB \text{ or } BA$   
use previously computed  
best way to access A and B
  - $\{B, C\} = BC \text{ or } CB$

Subplan S	optJoin(S)	Cost(OptJoin(S))
A	Index scan	100
B	Seq. scan	50
...		
{A, B}	BA	156
{B, C}	BC	98

# Example

- **orderJoins(A, B, C, D)**

- $d = 2$ 
  - $\{A, B\} = AB \text{ or } BA$   
use previously computed  
best way to access A and B
  - $\{B, C\} = BC \text{ or } CB$

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{A, B}	BA	156
{B, C}	BC	98

# Example

- **orderJoins(A, B, C, D)**

- $d = 2$

- $\{A, B\} = AB \text{ or } BA$   
use previously computed  
best way to access A and B

- $\{B, C\} = BC \text{ or } CB$
  - $\{C, D\} = CD \text{ or } DC$
  - $\{A, C\} = AC \text{ or } CA$
  - $\{B, D\} = BD \text{ or } DB$
  - $\{A, D\} = AD \text{ or } DA$

Subplan S	optJoin(S)	Cost(OptJoin(S))
A	Index scan	100
B	Seq. scan	50
...		
$\{A, B\}$	BA	156
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# Example

- **orderJoins(A, B, C, D)**

- $d = 2$ 
  - $\{A,B\} = AB \text{ or } BA$   
use previously computed  
best way to access A and B
  - $\{B,C\} = BC \text{ or } CB$
  - $\{C,D\} = CD \text{ or } DC$
  - $\{A,C\} = AC \text{ or } CA$
  - $\{B,D\} = BD \text{ or } DB$
  - $\{A,D\} = AD \text{ or } DA$

Subplan S	optJoin(S)	Cost(OptJoin(S))
A	Index scan	100
B	Seq. scan	50
...		
{A, B}	BA	156
{B, C}	BC	98
.....		

# Example

- **orderJoins(A, B, C, D)**
- $d = 3$ 
  - $\{A, B, C\} =$   
Remove A: compare  $A(\{B, C\})$  to  $(\{B, C\})A$

Subplan S	optJoin(S)	Cost(OptJoin(S))
A	Index scan	100
B	Seq. scan	50
....		
{A, B}	BA	156
{B, C}	BC	98
....		

# Example

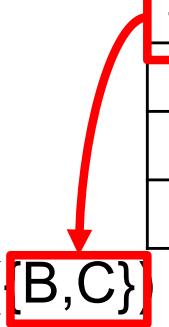
- **orderJoins(A, B, C, D)**

- $d = 3$

- $\{A, B, C\} =$

Remove A: compare  $A(\boxed{\{B, C\}})$  to  $(\{B, C\})A$

Subplan S	optJoin(S)	Cost(OptJoin(S))
A	Index scan	100
B	Seq. scan	50
....		
{A, B}	BA	156
{B, C}	BC	98
....		



optJoin(B,C)  
and its cost are  
already cached  
in table

# Example

- **orderJoins(A, B, C, D)**

- $d = 3$

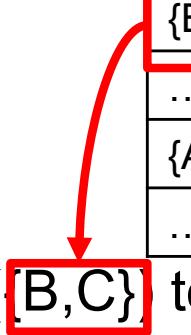
- $\{A, B, C\} =$

Remove A: compare  $A(\boxed{\{B,C\}})$  to  $(\{B,C\})A$

Remove B: compare  $B(\{A,C\})$  to  $(\{A,C\})B$

Remove C: compare  $C(\{A,B\})$  to  $(\{A,B\})C$

Subplan S	optJoin(S)	Cost(optJoin(S))
A	Index scan	100
B	Seq. scan	50
....		
{A, B}	BA	156
{B, C}	BC	98
....		
{A, B, C}	BAC	500
.....		



optJoin(B,C)  
and its cost are  
already cached  
in table

# Example

- **orderJoins(A, B, C, D)**

- $d = 3$

- $\{A, B, C\} =$

Remove A: compare  $A(\{B, C\})$  to  $(\{B, C\})A$

Remove B: compare  $B(\{A, C\})$  to  $(\{A, C\})B$

Remove C: compare  $C(\{A, B\})$  to  $(\{A, B\})C$

Subplan S	optJoin(S)	Cost(optJoin(S))
A	Index scan	100
B	Seq. scan	50
....		
{A, B}	BA	156
{B, C}	BC	98
....		
{A, B, C}	BAC	500
.....		

optJoin(B,C)  
and its cost are  
already cached  
in table

# Example

- **orderJoins(A, B, C, D)**

- $d = 3$

–  $\{A, B, C\} =$

Remove A: compare  $A(\{B, C\})$  to  $(\{B, C\})A$

Remove B: compare  $B(\{A, C\})$  to  $(\{A, C\})B$

Remove C: compare  $C(\{A, B\})$  to  $(\{A, B\})C$

–  $\{A, B, D\} =$

Remove A: compare  $A(\{B, D\})$  to  $(\{B, D\})A$

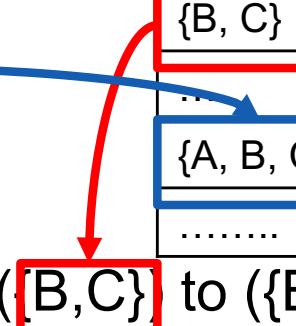
...

–  $\{A, C, D\} = \dots$

–  $\{B, C, D\} = \dots$

- Total number of steps:  $\text{choose}(N, 3) \times 3 \times 2$

Subplan S	optJoin(S)	Cost(OptJoin(S))
A	Index scan	100
B	Seq. scan	50
....		
{A, B}	BA	156
{B, C}	BC	98
....		
{A, B, C}	BAC	500
.....		



optJoin(B,C)  
and its cost are  
already cached  
in table

# Example

- **orderJoins(A, B, C, D)**

- $d = 4$ 
  - $\{A, B, C, D\} =$

Subplan S	optJoin(S)	Cost(OptJoin(S))
A	Index scan	100
B	Seq. scan	50
{A, B}	BA	156
{B, C}	BC	98
{A, B, C}	BAC	500
{B, C, D}	DBC	150
.....		

Remove A: compare  $A(\{B, C, D\})$  to  $(\{B, C, D\})A$

Remove B: compare  $B(\{A, C, D\})$  to  $(\{A, C, D\})B$

Remove C: compare  $C(\{A, B, D\})$  to  $(\{A, B, D\})C$

Remove D: compare  $D(\{A, B, C\})$  to  $(\{A, B, C\})D$

optJoin(B, C, D)  
and its cost are  
already cached  
in table

- Total number of steps:  $\text{choose}(N, 4) \times 4 \times 2$

# Complexity

- Total #subsets considered
  - $\text{Choose}(N, 1) + \text{Choose}(N, 2) + \dots + \text{Choose}(N, N)$
  - All nonempty subsets of a size  $N$  set:  $2^N - 1$
  - Equivalently: number of binary strings of size  $N$ , except 00...0:  
000, 001, 010, 011, 100, 101, 110, 111

# Complexity

- Total #subsets considered
  - $\text{Choose}(N, 1) + \text{Choose}(N, 2) + \dots + \text{Choose}(N, N)$
  - All nonempty subsets of a size  $N$  set:  $2^N - 1$
  - Equivalently: number of binary strings of size  $N$ , except 00...0:  
000, 001, 010, 011, 100, 101, 110, 111
- For each subset of size  $d$ :
  - $d$  ways to remove one element
  - 2 ways for compute AB or BA (except when  $d=2$ , when we already accounted for that – why?)

# Complexity

- Total #subsets considered
  - $\text{Choose}(N, 1) + \text{Choose}(N, 2) + \dots + \text{Choose}(N, N)$
  - All nonempty subsets of a size  $N$  set:  $2^N - 1$
  - Equivalently: number of binary strings of size  $N$ , except 00...0:  
000, 001, 010, 011, 100, 101, 110, 111
- For each subset of size  $d$ :
  - $d$  ways to remove one element
  - 2 ways for compute AB or BA (except when  $d=2$ , when we already accounted for that – why?)
- Total #plans considered
  - $\text{Choose}(N, 1) + 2 \text{Choose}(N, 2) + \dots + N \text{Choose}(N, N)$
  - Equivalently: total number of 1's in all strings of size  $N$
  - $N 2^{N-1}$  because every 1 occurs  $2^{N-1}$  times
  - Need to further multiply by 2, to account for AB or BA

# Interesting Orders

- Some query plans produce data in sorted order
  - E.g scan over a primary index, merge-join
  - Called *interesting order*
- Next operator may use this order
  - E.g. can be another merge-join
- For each subset of relations, compute multiple optimal plans, one for each interesting order
- Increases complexity by factor  $k+1$ , where  $k=\text{number of interesting orders}$

# Why Left-Deep

Asymmetric, cost depends on the order

- Left: Outer relation      Right: Inner relation
- For nested-loop-join, we try to load the outer (typically smaller) relation in memory, then read the inner relation one page at a time  
 $B(R) + B(R)^*B(S)$  or  $B(R) + B(R)/M * B(S)$
- For index-join,  
we assume right (inner) relation has index

# Why Left-Deep

- Advantages of left-deep trees?
  1. Fits well with standard join algorithms (nested loop, one-pass), more efficient
  2. One pass join: Uses smaller memory
    1.  $((R, S), T)$ , can reuse the space for R while joining  $(R, S)$  with T
    2.  $(R, (S, T))$ : Need to hold R, compute  $(S, T)$ , then join with R, worse if more relations
  3. Nested loop join, consider top-down iterator next()
    1.  $((R, S), T)$ , Reads the chunks of  $(R, S)$  once, reads stored base relation T multiple times
    2.  $(R, (S, T))$ : Reads the chunks of R once, reads computed relation  $(S, T)$  multiple times, either more time or more space

# Implementation in SimpleDB (lab5)

1. JoinOptimizer.java (and the classes used there)

2. Returns vector of “LogicalJoinNode”

Two base tables, two join attributes, predicate

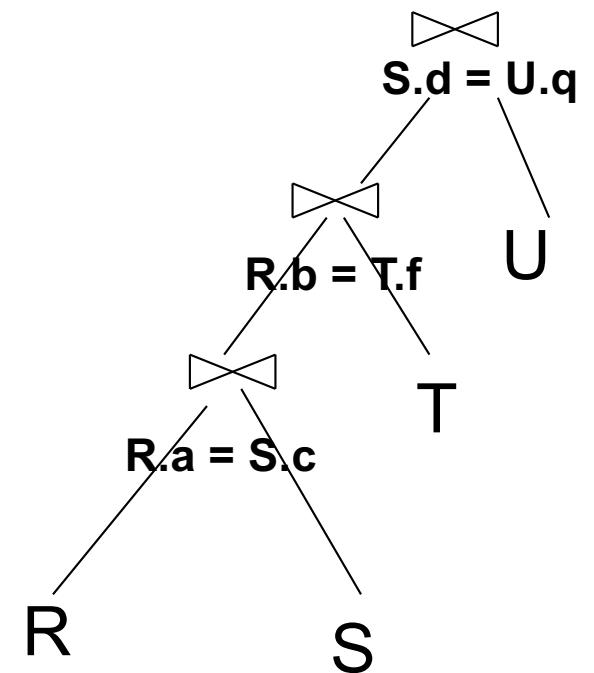
e.g.  $R(a, b)$ ,  $S(c, d)$ ,  $T(a, f)$ ,  $U(p, q)$

$(R, S, R.a, S.c, =)$

Recall that SimpleDB keeps all attributes of  
R, S after their join  $R.a, R.b, S.c, S.d$

3. Output vector looks like:

$\langle (R, S, R.a, S.c), (R, T, R.b, T.f), (S, U, S.d, U.q) \rangle$



# Implementation in SimpleDB (lab5)

Any advantage of returning pairs?

- Flexibility to consider all linear plans  
 $\langle(R, S, R.a, S.c), (R, T, R.b, T.f), (U, S, U.q, S.d)\rangle$

More Details:

- You mainly need to implement “`orderJoins(..)`”
- “`CostCard`” data structure stores a plan, its cost and cardinality: you would need to estimate them
- “`PlanCache`” stores the table in dyn. Prog:

Maps a set of LJN to  
a vector of LJN (best plan for the vector),  
its cost, and its cardinality  
**LJN = LogicalJoinNode**

