CSE 444: Database Internals

Lecture 8
Operator Algorithms (part 2)

Announcements

- Lab 2 / part 1 due on Wednesday
  - We will not run any tests – So bugs are OK
- Homework 2 due on Friday
- Paper review for master's due on Friday

Outline

- **Join operator algorithms**
  - One-pass algorithms (Sec. 15.2 and 15.3)
  - Index-based algorithms (Sec 15.6)
  - Two-pass algorithms (Sec 15.4 and 15.5)

Index Based Selection

Selection on equality: $\sigma_{a=v}(R)$
- B(R)= size of R in blocks
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Note: we ignore I/O cost for index pages

Index Based Selection

- Example: B(R) = 2000, T(R) = 100,000, V(R, a) = 20 — cost of $\sigma_{a=v}(R)$ = ?
- Table scan:
- Index based selection:

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Lesson: Don't build unclustered indexes when V(R,a) is small !

Index Nested Loop Join

R ⋈ S

- Assume S has an index on the join attribute
- Iterate over R, for each tuple fetch corresponding tuple(s) from S
- Cost:
  - If index on S is clustered: B(R) + T(R)B(S)/V(S,a)
  - If index on S is unclustered: B(R) + T(R)T(S)/V(S,a)

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Two-Pass Algorithms

- What if data does not fit in memory?
- Need to process it in multiple passes
- Two key techniques
  - Sorting
  - Hashing

Basic Terminology

- A run in a sequence is an increasing subsequence
- What are the runs?

2, 4, 99, 103, 88, 77, 3, 79, 100, 2, 50

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Phase one: load M blocks in memory, sort, sent to disk, repeat

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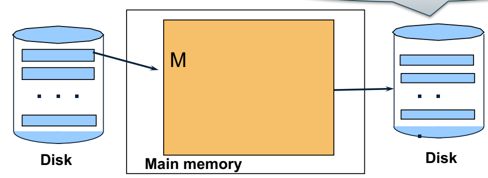

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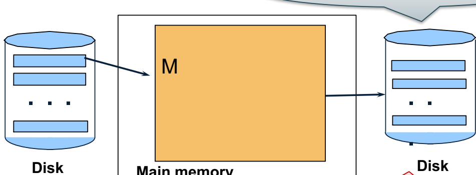

A: Length = M blocks

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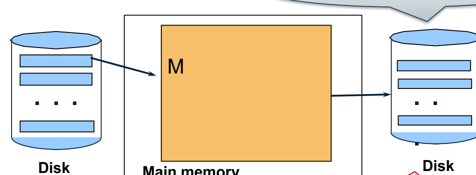


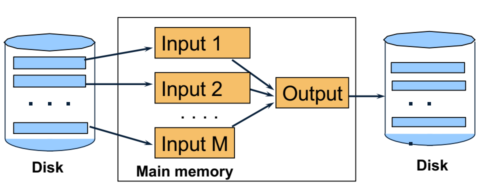
A: Length = M blocks

Can increase to length 2M using "replacement selection"

External Merge-Sort: Step 2

Phase two: merge M runs into a bigger run

- Merge M – 1 runs into a new run
- Result: runs of length M (M – 1) ≈ M^2



If B <= M^2 then we are done

Example

- Merging three runs to produce a longer run:

0, 14, 33, 88, 92, 192, 322
2, 4, 7, 43, 78, 103, 523
1, 6, 9, 12, 33, 52, 88, 320

Output:
0

Example

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Output:
0, 1, 2, 4, 6, 7, ?

Cost of External Merge Sort

- Read+write+read = 3B(R)
- Assumption: $B(R) <= M^2$

Discussion

- What does $B(R) <= M^2$ mean?
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- R can be as large as 10^{12}-pages
  - 32×10^{15} Bytes = 32 PB

Merge-Join

Join $R \bowtie S$

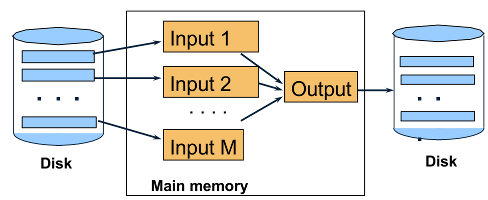
- How?....

Merge-Join

Join $R \bowtie S$

- Step 1a: initial runs for R
- Step 1b: initial runs for S
- Step 2: merge and join

Merge-Join



$M_1 = B(R)/M$ runs for R
$M_2 = B(S)/M$ runs for S
Merge-join $M_1 + M_2$ runs;
need $M_1 + M_2 <= M$

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- Goal: each R_i should fit in main memory:
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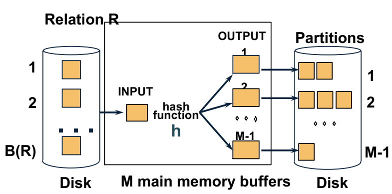
How do we choose k?

Partitioned Hash Algorithms

- We choose k = M-1 Each bucket has size approx. $B(R)/(M-1) \approx B(R)/M$



Assumption: $B(R)/M \le M$, i.e. $B(R) \le M^2$

Grace-Join

$R \bowtie S$

Note: grace-join is also called *partitioned hash-join*

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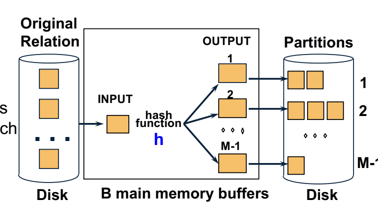
- Step 1:
  - Hash S into M buckets
  - Send all buckets to disk
- Step 2
  - Hash R into M buckets
  - Send all buckets to disk
- Step 3
  - Join every pair of buckets

Grace-Join

- Partition both relations using hash fn **h**: R tuples in partition i will only match S tuples in partition i.



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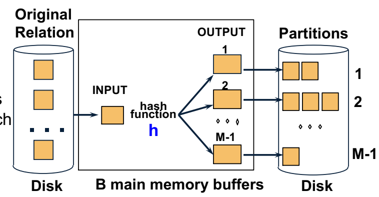
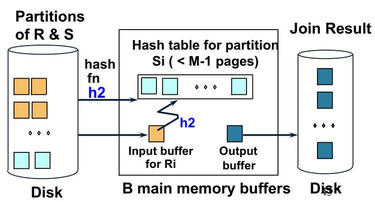


- Read in a partition of R, hash it using **h2 (<> h!)**. Scan matching partition of S, search for matches.



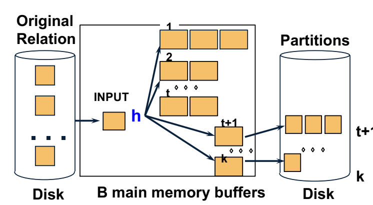
Grace Join

- Cost: 3B(R) + 3B(S)
- Assumption: min(B(R), B(S)) <= M^2

Hybrid Hash Join Algorithm

- Partition S into k buckets
  t buckets S_1 , …, S_t stay in memory
  k-t buckets S_{t+1}, …, S_k to disk
- Partition R into k buckets
  - First t buckets join immediately with S
  - Rest k-t buckets go to disk
- Finally, join k-t pairs of buckets:
  (R_{t+1},S_{t+1}), (R_{t+2},S_{t+2}), …, (R_k,S_k)

Hybrid Hash Join Algorithm



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  - Together: t/k * B(S) + k-t <= M

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- Assuming t/k * B(S) >> k-t: t/k = M/B(S)

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(Total size of first t buckets) (Number of remaining buckets)

Hybrid Join Algorithm

Even better: adjust t dynamically

- Start with t = k: all buckets are in main memory
- Read blocks from S, insert tuples into buckets
- When out of memory:
  - Send one bucket to disk
  - t := t-1
- Worst case:
  - All buckets are sent to disk (t=0)
  - Hybrid join becomes grace join

Hybrid Join Algorithm

Cost of Hybrid Join:

- Grace join: 3B(R) + 3B(S)
- Hybrid join:
  - Saves 2 I/Os for t/k fraction of buckets
  - Saves 2t/k(B(R) + B(S)) I/Os
  - Cost: (3-2t/k)(B(R) + B(S)) = (3-2M/B(S))(B(R) + B(S))

Hybrid Join Algorithm

- What is the advantage of the hybrid algorithm?

Hybrid Join Algorithm

- What is the advantage of the hybrid algorithm?

It degrades gracefully when S larger than M:

- When B(S) <= M
  - Main memory hash-join has cost B(R) + B(S)
- When B(S) > M
  - Grace-join has cost 3B(R) + 3B(S)
  - Hybrid join has cost (3-2t/k)(B(R) + B(S))

Summary of External Join Algorithms

- Block Nested Loop: B(S) + B(R)*B(S)/M
- Index Join: B(R) + T(R)B(S)/V(S,a)
- Partitioned Hash: 3B(R)+3B(S);
  - min(B(R),B(S)) <= M^2
- Merge Join: 3B(R)+3B(S)
  - B(R)+B(S) <= M^2

Summary of Query Execution

- For each logical query plan
  - There exist many physical query plans
  - Each plan has a different cost
  - Cost depends on the data
- Additionally, for each query
  - There exist several logical plans
- Next lecture: query optimization
  - How to compute the cost of a complete plan?
  - How to pick a good query plan for a query?