# CSE 444 

Lecture 28:
Provenance

## Announcements

- Quiz section on Thursday: canceled
- Lecture on Friday: canceled
- Lab 4 / Lab 6: due on Friday night
- Final writeup: on on Saturday night
- UW Course Evaluations:
- Online https://uw.iasystem.org/survey/130405
- Until June 12, 2014


## Data Provenance

## Data Provenance

- Provenance inside the DBMS
- Will discuss today
- Provenance outside of the DBMS
- In workflows: keep track of which dataset was produced by what program, which version, on what date, and using what input data
- Much more messy; there is a standard, OPM (Open Provenance Model)


## Provenance Annotations

- Some query produces an output table $T(A, B, C)$
- We store it over some period of time
- Later we ask: "where did

| A | B | C |
| :---: | :---: | :---: |
| a1 | b1 | c1 |
| a2 | b1 | c1 |
| a2 | b2 | c2 |
| a2 | b2 | c3 |

provenance1
provenance2
provenance3
provenance4 this tuple come from?"

- The "provenance annotation" answers this.


## Provenance Annotations

- Start by annotating each tuple in the original database with a unique identifier; can be the Tuple Id (TID)

| A | B |
| :---: | :---: |
| a1 | b1 |
| a2 | b1 |
| a2 | b2 |

- Next, compute the provenance expression inductively, based on the query plan


## Join Operator



## Projection Operator



## Union Operator



## Selection Operator

| $\sigma_{A=a 1}$ |  |
| :---: | :---: |
| A | B |
| a1 | b1 |
| a1 | b2 |
| a2 | b1 |
| a2 | b2 |
| a2 | b3 |


| A | B |
| :---: | :---: |
| a1 | b1 |
| a1 | b2 |

We could simply remove the tuples filtered out. But it's better to keep them around (we'll see why). What is their annotation?

## Selection Operator

| $\sigma_{A=a 1}$ |  |
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| A | B |
| a1 | b1 |
| a1 | b2 |
| a2 | b1 |
| a2 | b2 |
| a2 | b3 |


| A | B |
| :---: | :---: |
| a1 | b1 |
| a1 | b2 |
| a2 | b1 |
| a2 | b2 |
| a2 | b3 |

We could simply remove the tuples filtered out. But it's better to keep them around (we'll see why). What is their annotation?

## Simple Example 1

## $\Pi_{A C}(R) \bowtie \Pi_{B C}(R)=$

R

| A | B | C |
| :---: | :---: | :---: |
| a | b | c |
| X | X |  |
| d | b | e |
| f | y | e |
| Z |  |  |

## Simple Example 1

## $\Pi_{A C}(R) \bowtie \Pi_{B C}(R)=$

| R |  |  |  | $\prod_{\mathrm{AC}}(\mathrm{R})$ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| A | B | C |  | A | C |  |
| a | b | c | X | a | c | X |
| d | b | e | Y | d | e |  |
| f | g | e | Z | f | e |  |

## Simple Example 1

## $\Pi_{\mathrm{AC}}(R) \bowtie \Pi_{\mathrm{BC}}(R)=$

| R |  |  |  | $\prod_{A C}(\mathrm{R})$ |  |  | $\prod_{B C}(\mathrm{R})$ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| A | B | C |  | A | C |  | B | C |  |
| a | b | c | $X$ | a | c | X | b | c | X |
| d | b | e | Y | d | e | Y | b | e |  |
| f | g | e | Z | f | e | Z | g | e | Z |

## Simple Example 1

## $\Pi_{\mathrm{AC}}(R) \bowtie \Pi_{\mathrm{BC}}(R)=$

| R |  |  | $\prod_{\mathrm{AC}}(\mathrm{R})$ |  |  |  | $\prod_{B C}(\mathrm{R})$ |  |  | A | B | C |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| A | B | C | X | A | C | X | B | C | $x$ | a | b | c |  | X |
| a | b | c |  | a | c |  | b | c |  | d | b | e |  | Y |
| d | b | e | Y | d | e | Y | b | e | Y | d | g | e |  | Z |
| f | g | e |  | f | e | Z |  | e |  | f | b | e |  | Y |
|  |  |  |  |  |  |  | 9 |  |  | f | g | e |  |  |

## Simple Example 2

$$
\sigma_{C=e}(R)=
$$

R

| $A$ | $B$ | $C$ |
| :---: | :---: | :---: |
| $a$ | $b$ | $c$ |
|  | $X$ |  |
| $d$ | $b$ | $e$ |
|  | $Y$ |  |
| $f$ | $g$ | $e$ |
| $Z$ |  |  |


| A | B | C |  |
| :---: | :---: | :---: | :---: |
| a | b | C | $0=X \cdot 0$ |
| d | b | e | $Y=Y \cdot 1$ |
| f | g | e | $\mathbf{Z}=\mathbf{Z} \cdot 1$ |

## Complex Example

$$
\sigma_{\mathrm{C}=\mathrm{e}} \prod_{\mathrm{AC}}\left(\prod_{\mathrm{AC}}(\mathrm{R}) \bowtie \prod_{\mathrm{BC}}(\mathrm{R}) \cup \prod_{\mathrm{AB}}(\mathrm{R}) \bowtie \prod_{\mathrm{BC}}(\mathrm{R})\right)=
$$

## R

| A | B | C |
| :---: | :---: | :---: |
| a | b | c |
| d | b | e |
| f | y | e |
| Z |  |  |


| A | C |  |
| :---: | :---: | :--- |
| $a$ | $c$ | $(X \cdot X+X \cdot X) \cdot 0=0 \cdot 2 \cdot X^{2}=0$ |
| $a$ | $e$ | $X \cdot Y \cdot 1=X \cdot Y$ |
| $d$ | $c$ | $Y \cdot X \cdot 0=0$ |
| $d$ | $e$ | $(Y \cdot Y+Y \cdot Z+Y \cdot Y) \cdot 1=2 \cdot Y^{2}+Y \cdot Z$ |
| $f$ | $e$ | $(Z \cdot Z+Z \cdot Y+Z \cdot Z) \cdot 1=2 \cdot Z^{2}+Y \cdot Z$ |

Discuss in class what these annotations mean

## Independence of Plan

## $q(x, y):=R(x), S(x, y), T(y)$

Do these plans compute the same provenance for the output $(\mathrm{a}, \mathrm{b})$ ?

$\mathrm{R}=$


S=


## Independence of Plan

$$
\begin{aligned}
& q(x):=R(x), S(x) \\
& q(x):=R(x), T(x)
\end{aligned}
$$

Do these two plans compute the same provenance expression for the output (a)?

$$
\begin{aligned}
& V(x):=S(x) \\
& V(x):=T(x) \\
& q(x):=R(x), V(x)
\end{aligned}
$$



$\mathrm{R}=$| x |
| :--- |
| a |
| a | $\mathrm{S} \quad \mathrm{S}$| x |
| :--- |
| a |
| y |$\quad \mathrm{T}=$| x |
| :--- |
| a |
| Z |

## Identities on Provenance Expressions

Definition. A structure $(\mathrm{K},+, \cdot, 0,1)$ is called a commutative semiring if:

1. $(\mathrm{K},+, 0)$ is a commutative monoid:
a. + is associative: $\quad(x+y)+z=x+(y+z)$
b. + is commutative: $\quad x+y=y+x$
c. 0 is the identity for $+: \quad x+0=0+x=x$
2. $(K, \cdot, 1)$ is a commutative monoid:
a. ... (similar identities)
3. distributes over + : $\quad x \cdot(y+z)=x \cdot y+x \cdot z$
4. For all x :
$x \cdot 0=0 \cdot x=0$

## Identities on Provenance Expressions

Definition. A structure $(\mathrm{K},+, \cdot, 0,1)$ is called a commutative semiring if:

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b. + is commutative: $\quad x+y=y+x$
c. 0 is the identity for $+: \quad x+0=0+x=x$
2. ( $\mathrm{K}, \cdot, 1$ ) is a commutative monoid:
a. ... (similar identities)
3. distributes over +: $\quad x \cdot(y+z)=x \cdot y+x \cdot z$
4. For all x :
$x \cdot 0=0 \cdot x=0$

Fact: if we compute annotations in a commutative semiring, then the final result is the same for all plans that are equivalent under set semantics

## Example

## $q(x, u):=R(x, y), S(y, z), T(z, u)$

In class: compute the provenance of the output ( $a, b$ ) for both plans.

| x | y | X1 | y | z | Y1 | z | u |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| a | b1 |  | b1 | c1 |  | c1 | d | Z1 |
| a | b2 | X2 | b1 | c2 | Y2 | c2 | d | Z2 |
|  |  |  | b2 | c2 | Y3 |  |  |  |



## Applications

$$
\sigma_{\mathrm{C}=\mathrm{e}} \prod_{\mathrm{AC}}\left(\prod_{\mathrm{AC}}(\mathrm{R}) \bowtie \prod_{\mathrm{BC}}(\mathrm{R}) \cup \prod_{\mathrm{AB}}(\mathrm{R}) \bowtie \prod_{\mathrm{BC}}(\mathrm{R})\right)=
$$

| $\mathrm{R}=$ |  |  |
| :---: | :---: | :---: |
| A | B | C |
| a | b | c |
| d | b | e |
| f | g | e |


| A | C |  |
| :---: | :---: | :---: |
| a | c | 0 |
| a | e | $X \cdot Y$ |
| d | e | $2 \cdot Y^{2}+Y \cdot Z$ |
| f | e | $2 \cdot Z^{2}+Y \cdot Z$ |

Q: Suppose we delete the tuple ( $\mathrm{d}, \mathrm{b}, \mathrm{e}$ ) from R . Which tuple(s) disappear from the result?

## Applications

$$
\sigma_{C=e} \Pi_{A C}\left(\Pi_{A C}(R) \bowtie \Pi_{B C}(R) \cup \Pi_{A B}(R) \bowtie \Pi_{B C}(R)\right)=
$$

$\mathrm{R}=$

| A | B | C |
| :---: | :---: | :---: |
| a | b | c |
| X |  |  |
| d | b | e |
| f | y | e |
| Z |  |  |


| A | C |  |
| :---: | :---: | :---: |
| a | c | 0 |
| a | e | X•Y |
| d | e | $2 \cdot Y^{2}+Y \cdot Z$ |
| f | e | $2 \cdot Z^{2}+Y \cdot Z$ |


| A | C |
| :---: | :---: |
| a | c |
| a | e |
| d | e |
| f | e |

Q: Suppose we delete the tuple ( $\mathrm{d}, \mathrm{b}, \mathrm{e}$ ) from R.
A: Set $\mathrm{Y}=0$

## Applications

$$
\sigma_{\mathrm{C}=\mathrm{e}} \prod_{\mathrm{AC}}\left(\prod_{\mathrm{AC}}(\mathrm{R}) \bowtie \prod_{\mathrm{BC}}(\mathrm{R}) \cup \prod_{\mathrm{AB}}(\mathrm{R}) \bowtie \prod_{\mathrm{BC}}(\mathrm{R})\right)=
$$

| $\mathrm{R}=$ |  |  |
| :---: | :---: | :---: |
| A | B | C |
| a | b | c |
| d | b | e |
| f | g | e |


| A | C |  |
| :---: | :---: | :---: |
| a | c | 0 |
| a | e | $X \cdot Y$ |
| d | e | $2 \cdot Y^{2}+Y \cdot Z$ |
| f | e | $2 \cdot Z^{2}+Y \cdot Z$ |

Q: Suppose each tuple in R occurs 3 times (bag semantics). How many times occurs each tuple in the answer?

## Applications

$$
\sigma_{C=e} \Pi_{A C}\left(\Pi_{A C}(R) \bowtie \Pi_{\mathrm{BC}}(R) \cup \Pi_{A B}(R) \bowtie \Pi_{\mathrm{BC}}(R)\right)=
$$

$R=$

| $A$ | $B$ | $C$ |
| :--- | :--- | :--- |
| $a$ | $b$ | $c$ |
|  | $X$ |  |
| $d$ | $b$ | $e$ |
| $f$ | $g$ | $e$ |


| A | C |  |
| :---: | :---: | :---: |
| a | c | 0 |
| a | e | $X \cdot Y$ |
| d | e | $2 \cdot Y^{2}+Y \cdot Z$ |
| f | e | $2 \cdot Z^{2}+Y \cdot Z$ |


| A | C |
| :---: | :---: |
| a | C |
| a | e |
| d | e |
| f | e |

Q: Suppose each tuple in R occurs 3 times (bag semantics).
A. Set $X=Y=Z=3$ How many times occurs each tuple in the answer?

## Application: A Simpler Provenance of Sets of Contributing Tuples

$\sigma_{C=e} \Pi_{A C}\left(\Pi_{A C}(R) \bowtie \Pi_{B C}(R) \cup \Pi_{A B}(R) \bowtie \Pi_{B C}(R)\right)=$

| $\mathrm{R}=$ |  |  |
| :---: | :---: | :---: |
| A | B | C |
| a | b | c |
| d | b | e |
| f | g | e |


| $A$ | $C$ |  |
| :---: | :---: | :--- |
| $a$ | $c$ | 0 |
| $a$ | $e$ | $X \cdot Y$ |
| $d$ | $e$ | $2 \cdot Y^{2}+Y \cdot Z$ |
| $f$ | $e$ | $2 \cdot Z^{2}+Y \cdot Z$ |


$\rightarrow \quad$| $A$ | $C$ |  |
| :---: | :---: | :--- |
| $a$ | $c$ | - |
| $a$ | $e$ | $X, Y$ |
| $d$ | $e$ | $Y, Z$ |
| $f$ | $e$ | $Y, Z$ |

Trace only the set of input tuples that contributed to an output tuple
This is also a semi-ring! Which one?

## Application: Security

## Discretionary Access Control [LaPadula]

- Public $=P$
- Confidential = C
- Secret = S
- Top Secret = T
- No Such Thing... $=0$

| $A$ | $C$ |  |
| :---: | :---: | :--- |
| $a$ | $c$ | $2 \cdot X^{2}=?$ |
| $a$ | $e$ | $X \cdot Y=?$ |
| $d$ | $e$ | $2 \cdot Y^{2}+Y \cdot Z=?$ |
| $f$ | $e$ | $2 \cdot Z^{2}+Y \cdot Z=?$ |

## Application: Security

Discretionary Access Control [LaPadula]

- Public = $P$
- Confidential = C
- Secret = S
- Top Secret = T
- No Such Thing... $=0$

Alice has clearance S :

- Alice can read C data
- Alice cannot read T data
- Alice can write T data
- Alice cannot read C data

Why??

## Application: Security

## Discretionary Access Control [LaPadula]

- Public = P
- Confidential $=\mathrm{C}$
- Secret = S
- Top Secret = T
- No Such Thing... $=0$

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- Alice cannot read C data

Why??

Q: Join record $A$ labeled $C$ with record $B$ labeled $S$. What is the label of $(A, B)$ ?

## Application: Security

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Why??

Q: Join record $A$ labeled $C$ with record $B$ labeled $S$. What is the label of $(A, B)$ ?
A: S

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- Public = P
- Confidential = C
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- Top Secret = T
- No Such Thing... $=0$

Alice has clearance S:

- Alice can read C data
- Alice cannot read T data
- Alice can write T data
- Alice cannot read C data

Why??

Q: Join record $A$ labeled $C$ with record $B$ labeled $S$. What is the label of $(A, B)$ ? A: S

Q: Eliminate duplicates $\{A, A, A, A\}$ labeled $T, C, C, S$. What is the label of $A$ ?

## Application: Security

## Discretionary Access Control [LaPadula]

- Public = P
- Confidential = C
- Secret = S
- Top Secret = T
- No Such Thing... $=0$

Alice has clearance S:

- Alice can read C data
- Alice cannot read T data
- Alice can write T data
- Alice cannot read C data

Why??

Q: Join record $A$ labeled $C$ with record $B$ labeled $S$. What is the label of $(A, B)$ ? A: S

Q: Eliminate duplicates $\{A, A, A, A\}$ labeled $T, C, C, S$. What is the label of $A$ ? A: C

## Application: Security

## Discretionary Access Control [LaPadula]

- Public = P
- Confidential = C
- Secret = S
- Top Secret = T
- No Such Thing... $=0$

> What are the labels of these records?

| $A$ | $C$ |  |
| :---: | :---: | :--- |
| $a$ | $c$ | $2 \cdot X^{2}$ |
| $a$ | $e$ | $X \cdot Y$ |
| $d$ | $e$ | $2 \cdot Y^{2}+Y \cdot Z$ |
| $f$ | $e$ | $2 \cdot Z^{2}+Y \cdot Z$ |

(A, min, max, 0, P), where A $=$ P $<\mathrm{C}<\mathrm{S}<\mathrm{T}<0$

## Application: Security

## Discretionary Access Control [LaPadula]

- Public = P
- Confidential = C
- Secret = S
- Top Secret = T
- No Such Thing... $=0$

| $A$ | $C$ |  |
| :---: | :---: | :--- |
| $a$ | $c$ | $2 \cdot X^{2}=C$ |
| $a$ | $e$ | $X \cdot Y=C$ |
| $d$ | $e$ | $2 \cdot Y^{2}+Y \cdot Z=c$ |
| $f$ | $e$ | $2 \cdot Z^{2}+Y \cdot Z=T$ |

(A, min, max, 0, P), where A $=\mathrm{P}<\mathrm{C}<\mathrm{S}<\mathrm{T}<0$

## Summary

- In many applications it is critical to record the provenance of the data
- Fine grained provenance:
- Inside the database system
- Clear semantics that aligns to relational queries
- This is what we discussed today
- Coarse grained provenance:
- Lossy, by necessity
- Trade off accuracy for size

