# CSE 444: Database Internals 

Lecture 12<br>Query Optimization (part 3)

## Selinger Optimizer

Problem:

- How to order a series joins over N tables $\mathrm{A}, \mathrm{B}, \mathrm{C}, \ldots$ E.g. A.a = B.b AND A.c = D.d AND B.e = C.f
- N! ways to order joins; e.g. ABCD, ACBD, ....
- $C_{N-1}=\frac{1}{N}\binom{2(N-1)}{N-1}$ plans/ordering; e.g. (((AB)C)D), ((AB)(CD)))
- Multiple implementations (hash, nested loops)
- Naïve approach does not scale
- E.g. $\mathrm{N}=20$, \#join orders $20!=2.4 \times 10^{18}$; many more plans


## Selinger Optimizer

- Only left-deep plan: $(((\mathrm{AB}) \mathrm{C}) \mathrm{D})$ - eliminate $\mathrm{C}_{\mathrm{N}-1}$.
- Push down selection
- Don't consider cartesian product
- Dynamic programming algorithm


## Dynamic Programming

OrderJoin:
$\mathrm{R}=$ set of relations to join
For $\mathrm{d}=1$ to N : $\quad \mathrm{J}^{*}$ where $\mathrm{N}=|\mathrm{R}|$ */
For $S$ in \{all size-d subsets of $R$ \}:
optjoin(S) = (S -a) join a,
where $a$ is the single relation that minimizes:
cost(optjoin(S - a)) +
min.cost to join ( $S-a$ ) with a +
min.access cost for a

Note: optjoin(S-a) is cached from previous iterations

SimpleDB Lab4: called CostCard(cost, card, plan)

## Example

- optJoin(A, B, C, D)

| Subplan S | optJoin(S) | Cost(OptJoin(S)) |
| :--- | :--- | :--- |
| A |  |  |

- Assume all joins are NL


## Example

- optJoin(A, B, C, D)
- Assume all joins are NL
- $d=1$

| Subplan S | optJoin(S) | Cost(OptJoin(S)) |
| :--- | :--- | :--- |
| A | Index scan | 100 |
| B | Seq. scan | 50 |
| C | Seq scan | 120 |
| D | B+tree <br> scan | 400 |

- A = best way to access A (sequential scan, predicate-pushdown on index, etc)
- B = best way to access B
- C = best way to access C
- D = best way to access D
- Total number of steps: choose(N, 1)


## Example

- optJoin(A, B, C, D)
- d=2
$-\{\mathrm{A}, \mathrm{B}\}=\mathrm{AB}$ or BA use previously computed best way to access $A$ and $B$

| Subplan S | optJoin(S) | Cost(OptJoin(S)) |
| :--- | :--- | :--- |
| A | Index scan | 100 |
| B | Seq. scan | 50 |
| $\ldots$ |  |  |
|  |  |  |
|  |  |  |
|  |  |  |

## Example

- optJoin(A, B, C, D)
- d=2
$-\{\mathrm{A}, \mathrm{B}\}=\mathrm{AB}$ or BA use previously computed best way to access $A$ and $B$

| Subplan S | optJoin(S) | Cost(OptJoin(S)) |
| :--- | :--- | :--- |
| A | Index scan | 100 |
| B | Seq. scan | 50 |
| $\ldots$ |  |  |
| $\{$ A, B $\}$ | BA | 156 |
|  |  |  |
|  |  |  |

## Example

- optJoin(A, B, C, D)
- d=2
$-\{\mathrm{A}, \mathrm{B}\}=\mathrm{AB}$ or BA use previously computed best way to access $A$ and $B$

| Subplan S | optJoin(S) | Cost(OptJoin(S)) |
| :--- | :--- | :--- |
| A | Index scan | 100 |
| B | Seq. scan | 50 |
| $\ldots$ |  |  |
| $\{A, B\}$ | BA | 156 |
| $\{B, C\}$ | BC | 98 |
|  |  |  |

$-\{B, C\}=B C$ or $C B$

## Example

- optJoin(A, B, C, D)
- $d=2$
$-\{A, B\}=A B$ or $B A$ use previously computed best way to access $A$ and $B$

| Subplan S | optJoin(S) | Cost(OptJoin(S)) |
| :--- | :--- | :--- |
| A | Index scan | 100 |
| B | Seq. scan | 50 |
| $\ldots$ |  |  |
| $\{A, B\}$ | BA | 156 |
| $\{B, C\}$ | BC | 98 |
|  |  |  |

$-\{B, C\}=B C$ or $C B$

## Example

- optJoin(A, B, C, D)
- $d=2$
$-\{A, B\}=A B$ or $B A$ use previously computed best way to access $A$ and $B$

| Subplan S | optJoin(S) | Cost(OptJoin(S)) |
| :--- | :--- | :--- |
| A | Index scan | 100 |
| B | Seq. scan | 50 |
| $\ldots$ |  |  |
| $\{A, B\}$ | BA | 156 |
| $\{B, C\}$ | BC | 98 |
| $\ldots \ldots$. |  |  |

$-\{B, C\}=B C$ or $C B$
$-\{C, D\}=C D$ or $D C$
$-\{A, C\}=A C$ or $C A$
$-\{B, D\}=B D$ or $D B$
$-\{A, D\}=A D$ or $D A$

## Example

- optJoin(A, B, C, D)
- $d=2$
$-\{A, B\}=A B$ or $B A$ use previously computed best way to access $A$ and $B$

| Subplan S | optJoin(S) | Cost(OptJoin(S)) |
| :--- | :--- | :--- |
| A | Index scan | 100 |
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| $\ldots$ |  |  |
| $\{A, B\}$ | BA | 156 |
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| $\ldots \ldots$. |  |  |

$-\{B, C\}=B C$ or $C B$
$-\{C, D\}=C D$ or $D C$
$-\{A, C\}=A C$ or $C A$
$-\{B, D\}=B D$ or $D B$

- $\{\mathrm{A}, \mathrm{D}\}=\mathrm{AD}$ or DA
- Total number of steps: choose $(\mathrm{N}, 2) \times 2$


## Example



## Example

| Subplan S | optJoin(S) | Cost(OptJoin(S)) |
| :--- | :--- | :--- |
| A | Index scan | 100 |
| B | Seq. scan | 50 |
| $\ldots .$. |  |  |
| $\{A, B\}$ | BA | 156 |
| $\{B, C\}$ | BC | 98 |
| $\ldots$ |  |  |
|  |  |  |
|  | to (\{B,C $\}$ )A |  |

optJoin(B,C) and its cost are already cached in table

## Example

| Subplan S | optJoin(S) | Cost(OptJoin(S)) |
| :---: | :---: | :---: |
| A | Index scan | 100 |
| B | Seq. scan | 50 |
| $\ldots$ |  |  |
| $\{\mathrm{A}, \mathrm{B}\}$ | BA | 156 |
| \{B, C\} | BC | 98 |
| $\ldots$ |  |  |
| $\{\mathrm{A}, \mathrm{B}, \mathrm{C}\}$ | BAC | 500 |
| to (\{B, |  |  |

- $\{\mathrm{A}, \mathrm{B}, \mathrm{C}\}=$

Remove A: compare $A(\sqrt{B}, C\} \mid$ to $(\{B, C\}) A$ Remove B: compare B(\{A,C\}) to (\{A,C\})B Remove C: compare C(\{A,B\}) to (\{A,B\})C
optJoin(B,C) and its cost are already cached in table

## Example

| Subplan S | optJoin(S) | Cost(OptJoin(S)) |
| :--- | :--- | :--- |
| A | Index scan | 100 |
| B | Seq. scan | 50 |
| $\ldots$. |  |  |
| $\{A, B\}$ | BA | 156 |
| $\{B, C\}$ | BC | 98 |
| $\ldots$ |  |  |
| $\{A, B, C\}$ | BAC | 500 |
| $\ldots \ldots \ldots, B, C\}) A$ |  |  |
| to (\{B,C\} |  |  |

Remove B: compare $B(\{\bar{A}, \mathrm{C}\})$ to $(\{\mathrm{A}, \mathrm{C}\}) \mathrm{B}$ Remove C: compare C(\{A,B\}) to (\{A,B\})C
optJoin(B,C) and its cost are already cached in table

## Example

| Subplan S | optJoin(S) | Cost(OptJoin(S)) |
| :--- | :--- | :--- |
| $A$ | Index scan | 100 |
| B | Seq. scan | 50 |
| $\ldots .$. |  |  |
| $\{A, B\}$ | BA | 156 |
| $\{B, C\}$ | BC | 98 |
| $\ldots$ |  |  |
| $\{A, B, C\}$ | BAC | 500 |
| $\ldots \ldots \ldots$ |  |  |
| to $\{B, C\}) A$ |  |  | Remove B: compare $B(\{\bar{A}, \mathrm{C}\})$ to $(\{\mathrm{A}, \mathrm{C}\}) \mathrm{B}$ Remove C: compare C(\{A,B\}) to (\{A,B\})C optJoin(B,C)

- $\{A, B, D\}=$

Remove A: compare $A(\{B, D\})$ to (\{B,D\})A
and its cost are already cached in table

- $\{\mathrm{A}, \mathrm{C}, \mathrm{D}\}=\ldots$
- $\{B, C, D\}=\ldots$
- Total number of steps: choose $(\mathrm{N}, 3) \times 3 \times 2$


## Example

- optJoin(A, B, C, D)
- $d=4$
- $\{A, B, C, D\}=$

| Subplan S | optJoin(S) | Cost(OptJoin(S)) |  |  |
| :--- | :--- | :--- | :---: | :---: |
| A | Index <br> scan | 100 |  |  |
| B | Seq. scan | 50 |  |  |
| $\{A, B\}$ | BA | 156 |  |  |
| $\{B, C\}$ | BC | 98 |  |  |
| $\{A, B, C\}$ | BAC | 500 |  |  |
| $\{B, C, D\}$ | DBC | 150 |  |  |
| $\ldots \ldots \ldots$ |  |  |  |  |

Remove B: compare $B(\{A, C, D\})$ to $(\{A, C, D\}) B$ Remove C: compare C(\{A,B,D\}) to (\{A,B,D\})C Remove D: compare $D(\{A, B, C\})$ to $(\{A, B, C\}) D$
optJoin(B, C, D) and its cost are already cached in table

- Total number of steps: choose $(\mathrm{N}, 4) \times 4 \times 2$


## Complexity

- Total \#subsets considered
- Choose( $\mathrm{N}, 1$ ) + Choose( $\mathrm{N}, 2$ ) + ..... + Choose ( $\mathrm{N}, \mathrm{N}$ )
- All nonempty subsets of a size $N$ set: $2^{N}-1$
- Equivalently: number of binary strings of size N , except $00 \ldots 0$ : $000,001,010,011,100,101,110,111$


## Complexity

- Total \#subsets considered
- Choose(N, 1) + Choose(N, 2) + .... + Choose (N, N)
- All nonempty subsets of a size N set: $2^{\mathrm{N}}-1$
- Equivalently: number of binary strings of size N , except 00... 0 : $000,001,010,011,100,101,110,111$
- For each subset of size d :
- d ways to remove a set
- 2 ways for compute AB or BA (except when d=2, when we already accounted for that - why?)


## Complexity

- Total \#subsets considered
- Choose(N, 1) + Choose(N, 2) + .... + Choose (N, N)
- All nonempty subsets of a size N set: $2^{\mathrm{N}}-1$
- Equivalently: number of binary strings of size N , except 00...0: 000, 001, 010, 011, 100, 101, 110, 111
- For each subset of size d:
- d ways to remove a set
- 2 ways for compute AB or BA (except when d=2, when we already accounted for that - why?)
- Total \#plans considered
- Choose(N, 1) + 2 Choose( $\mathrm{N}, 2$ ) $+\ldots . .+\mathrm{N}$ Choose ( $\mathrm{N}, \mathrm{N}$ )
- Equivalently: total number of 1's in all strings of size $N$
- $\mathrm{N} 2^{\mathrm{N}-1}$ because every 1 occurs $2^{\mathrm{N}-1}$ times
- Need to further multiply by 2 , to account for AB or BA


## Interesting Orders

- Some query plans produce data in sorted order
- E.g scan over a primary index, merge-join
- Called interesting order
- Next operator may use this order
- E.g. can be another merge-join
- For each subset of relations, compute multiple optimal plans, one for each interesting order
- Increases complexity by factor $\mathrm{k}+1$, where $\mathrm{k}=$ number of interesting orders


## Why Left-Deep

Asymmetric, cost depends on the order

- Left: Outer relation

Right: Inner relation

- For nested-loop-join, we try to load the outer (typically smaller) relation in memory, then read the inner relation one page at a time

$$
B(R)+B(R) * B(S) \text { or } B(R)+B(R) / M * B(S)
$$

- For index-join, we assume right (inner) relation has index


## Why Left-Deep

- Advantages of left-deep trees?

1. Fits well with standard join algorithms (nested loop, one-pass), more efficient
2. One pass join: Uses smaller memory
3. ( $(R, S), T)$, can reuse the space for $R$ while joining $(R, S)$ with $T$
4. ( $R,(S, T)$ ): Need to hold $R$, compute ( $S, T$ ), then join with $R$, worse if more relations
5. Nested loop join, consider top-down iterator next()
6. ( $(R, S), T)$, Reads the chunks of $(R, S)$ once, reads stored base relation T multiple times
7. ( $R,(S, T)$ ): Reads the chunks of $R$ once, reads computed relation $(S, T)$ multiple times, either more time or more space

## Implementation in SimpleDB (lab4)

1. JoinOptimizer.java (and the classes used there)
2. Returns vector of "LogicalJoinNode"
a) Two base tables, two join attributes, predicate
b) e.g. $R(a, b), S(c, d), T(a, f), U(p, q)$
c) (R, S, R.a, S.c, =)
d) Recall that SimpleDB stores all attributes of

R, S after their join R.a, R.b, S.c, S.d

3. Output vector looks like: <(R, S, R.a, S.c), (R, T, R.b, T.f), (S, U, S.d, U.q)>

## Implementation in SimpleDB (lab4)

## Any advantage of returning pairs?

- Flexibility to consider all linear plans
<(R, S, R.a,S.c), (R, T, R.b, T.f), (U, S, U.q, S.d)>

More Details:

1. You mainly need to implement "orderJoin(..)"
2. "CostCard" data structure stores a plan, its cost and cardinality: you would need to estimate them
3. "PlanCache" stores the table in dyn. Prog: Maps a set of LJN to
a vector of LJN (best plan for the vector),
 its cost, and its cardinality
