Version Jan 19, 2011

## Introduction to Database Systems CSE 444

Lectures 6-7: Database Design

## Outline

Design theory: 3.1-3.4

▶ [Old edition: 3.4-3.6]

### Schema Refinements = Normal Forms

- 1st Normal Form = all tables are flat
- (2nd Normal Form = obsolete)
- Boyce Codd Normal Form = main focus
- 3rd Normal Form = see book for more details

## First Normal Form (1NF)

A database schema is in *First Normal Form* if all tables are flat
Student

#### **Student**

Name	GPA	Course
Alice	3.8	Math DB OS
Bob	3.7	DB OS
Carol	3.9	Math OS

May need to add keys

Name	GPA
Alice	3.8
Bob	3.7
Carol	3.9

#### **Takes**

Student	Course
Alice	Math
Carol	Math
Alice	DB
Bob	DB
Alice	OS
Carol	OS

#### Course

Course	
Math	
DB	
OS	

## Conceptual Schema Design

name **Conceptual Model:** Patient patient\_o Doctor **Relational Model:** plus FD's (FD = Functional Dependency) Normalization: Eliminates anomalies

### **Data Anomalies**

- When a database is poorly designed we get anomalies:
  - Redundancy: data is repeated
  - Update anomalies: need to change in several places
  - Delete anomalies: may lose data when we don't want

## Relational Schema Design

Recall set attributes (persons with several phones):

Name	<u>SSN</u>	<u>PhoneNumber</u>	City
Fred	123-45-6789	206-555-1234	Seattle
Fred	123-45-6789	206-555-6543	Seattle
Joe	987-65-4321	908-555-2121	Westfield

One person may have multiple phones, but lives in only one city

Primary key is thus (SSN, PhoneNumber)

The above is in 1NF, but what is the problem with this schema?

## Relational Schema Design

#### Recall set attributes (persons with several phones):

Name	<u>SSN</u>	<u>PhoneNumber</u>	City
Fred	123-45-6789	206-555-1234	Seattle
Fred	123-45-6789	206-555-6543	Seattle
Joe	987-65-4321	908-555-2121	Westfield

#### **Anomalies:**

- Redundancy = repeat data
- Update anomalies = what if Fred moves to "Bellevue"?
- Deletion anomalies = what if Joe deletes his phone number?
   (what if Joe had only one phone #)

## Relation Decomposition

#### Break the relation into two:

Name	SSN	PhoneNumber	City
Fred	123-45-6789	206-555-1234	Seattle
Fred	123-45-6789	206-555-6543	Seattle
Joe	987-65-4321	908-555-2121	Westfield

Name	<u>SSN</u>	City
Fred	123-45-6789	Seattle
Joe	987-65-4321	Westfield

<u>SSN</u>	<u>PhoneNumber</u>	
123-45-6789	206-555-1234	
123-45-6789	206-555-6543	
987-65-4321	908-555-2121	

#### Anomalies have gone:

- No more repeated data
- Easy to move Fred to "Bellevue" (how ?)
- Easy to delete all Joe's phone numbers (how ?)

## Relational Schema Design (Logical Design)

#### Main idea:

- Start with some relational schema
- Find out its functional dependencies (discussed next!)
- Use them to design a better relational schema

## Functional Dependencies

- A form of constraint
  - Hence, part of the schema
- Finding them is part of the database design
- Use them to normalize the relations

## Functional Dependencies (FDs)

#### **Definition:**

If two tuples agree on the attributes

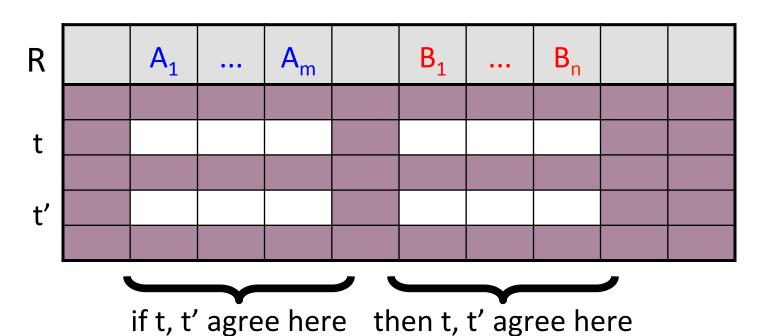
then they must also agree on the attributes

#### Formally:

$$A_1, A_2, ..., A_n \rightarrow B_1, B_2, ..., B_m$$

#### When Does an FD Hold

Definition:  $A_1, ..., A_m \rightarrow B_1, ..., B_n$  holds in R if:  $\forall t, t' \in R$ ,  $(t.A_1 = t'.A_1 \land ... \land t.A_m = t'.A_m \Rightarrow t.B_1 = t'.B_1 \land ... \land t.B_n = t'.B_n)$ 



#### An FD holds, or does not hold on an instance:

EmplD	Name	Phone	Position
E0045	Smith	1234	Clerk
E3542	Mike	9876	Salesrep
E1111	Smith	9876	Salesrep
E9999	Mary	1234	Lawyer

EmpID → Name, Phone, Position

Position → Phone

but not: Phone → Position

EmpID	Name	Phone	Position
E0045	Smith	1234	Clerk
E3542	Mike	9876 ←	Salesrep
E1111	Smith	9876 ←	Salesrep
E9999	Mary	1234	Lawyer

#### Position → Phone

EmpID	Name	Phone	Position
E0045	Smith	1234 →	Clerk
E3542	Mike	9876	Salesrep
E1111	Smith	9876	Salesrep
E9999	Mary	1234 →	Lawyer

But not: Phone → Position

#### FD's are constraints:

- On some instances they hold
- On others they don't

name → color
category → department
color, category → price

name	category	color	department	price
Gizmo	Gadget	Green	Toys	49
Tweaker	Gadget	Green	Toys	99

Does this instance satisfy all the FDs?

#### FD's are constraints:

- On some instances they hold
- On others they don't

name → color
category → department
color, category → price

name	category	color	department	price
Gizmo	Gadget	Green	Toys	49
Tweaker	Gadget	Green	Toys	99
Gizmo	Stationary	Blue	Supplies	59

#### What about this one?

## An Interesting Observation

If all these FDs are true:

name → color
category → department
color, category → price

Then this FD also holds:

name, category → price

Why??

## Goal: Find ALL Functional Dependencies

- Anomalies occur when certain "bad" FDs hold
- We know some of the FDs
- Need to find all FDs
- Then look for the "bad" ones

## Armstrong's Rules (1/3)

$$A_1, A_2, ..., A_n \rightarrow B_1, B_2, ..., B_m$$

Is equivalent to

$$A_{1}, A_{2}, ..., A_{n} \rightarrow B_{1}$$

$$A_{1}, A_{2}, ..., A_{n} \rightarrow B_{2}$$

$$....$$

$$A_{1}, A_{2}, ..., A_{n} \rightarrow B_{m}$$

# Splitting rule and Combing rule

A1	 Am	B1	 Bm	

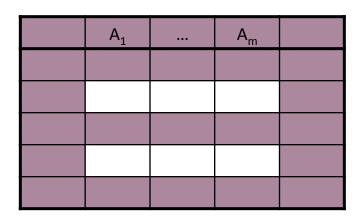
## Armstrong's Rules (2/3)

$$A_1, A_2, ..., A_n \rightarrow A_i$$

where i = 1, 2, ..., n

#### **Trivial Rule**

Why?



## Armstrong's Rules (3/3)

#### **Transitive Rule**

$$A_1, A_2, ..., A_n \rightarrow B_1, B_2, ..., B_m$$

$$B_1, B_2, ..., B_m \rightarrow C_1, C_2, ..., C_p$$

$$A_1, A_2, ..., A_n \rightarrow C_1, C_2, ..., C_p$$

#### Why?

## Armstrong's Rules (3/3)

### Illustration for Transitivity

A <sub>1</sub>	 A <sub>m</sub>	B <sub>1</sub>	 B <sub>m</sub>	C <sub>1</sub>	 C <sub>p</sub>	

## Example (continued)

#### Start from the following FDs:

- 1. name → color
- 2. category → department
- 3. color, category → price

#### Infer the following FDs:

Inferred FD	Which Rule did we apply ?
4. name, category → name	
5. name, category → color	
6. name, category → category	
7. name, category $\rightarrow$ color, category	
8. name, category $\rightarrow$ price	

## Example (continued)

- 1. name → color
- 2. category → department
- 3. color, category → price

#### **Answers:**

Inferred FD	Which Rule did we apply ?
4. name, category → name	Trivial
5. name, category → color	Transitivity on 4, 1
6. name, category → category	Trivial
7. name, category → color, category	Split/combine on 5, 6
8. name, category → price	Transitivity on 3, 7

THIS IS TOO HARD! Let's see an easier way.

#### Closure of a set of Attributes

**Given** a set of attributes  $A_1, ..., A_n$ 

The **closure**,  $\{A_1, ..., A_n\}^+$  = the set of attributes B s.t.  $A_1, ..., A_n \rightarrow B$ 

Example:

name → color
category → department
color, category → price

#### **Closures:**

```
name+ = {name, color}
{name, category}+ = {name, category, color, department, price}
color+ = {color}
```

## Closure Algorithm

```
X = \{A_1, ..., A_n\}.
Repeat until X doesn't change do:
  if B_1, ..., B_n \rightarrow C is a FD and
        B_1, ..., B_n are all in X
  then add C to X.
```

#### Example:

name -> color category -> department color, category → price

```
{name, category}+ =
   { name, category, color, department, price }
```

Hence:

name, category  $\rightarrow$  color, department, price

#### In class:

A, B 
$$\rightarrow$$
 C  
A, D  $\rightarrow$  E  
B  $\rightarrow$  D  
A, F  $\rightarrow$  B

Compute 
$$\{A, F\}^+ X = \{A, F, A, F,$$

#### In class:

A, B 
$$\rightarrow$$
 C  
A, D  $\rightarrow$  E  
B  $\rightarrow$  D  
A, F  $\rightarrow$  B

Compute 
$$\{A,B\}^+$$
  $X = \{A, B, C, D, E\}$ 

Compute 
$$\{A, F\}^+ X = \{A, F,$$

#### In class:

A, B 
$$\rightarrow$$
 C  
A, D  $\rightarrow$  E  
B  $\rightarrow$  D  
A, F  $\rightarrow$  B

Compute 
$$\{A,B\}^+$$
  $X = \{A, B, C, D, E\}$ 

Compute 
$$\{A, F\}^+ X = \{A, F, B, C, D, E\}$$

## Why Do We Need Closure

- With closure we can find all FD's easily
- ▶ To check if  $X \rightarrow A$ 
  - Compute X<sup>+</sup>
  - ▶ Check if  $A \subseteq X^+$

## Using Closure to Infer ALL FDs

Example: 
$$A, B \rightarrow C$$
  
 $A, D \rightarrow B$   
 $B \rightarrow D$ 

#### Step 1: Compute X<sup>+</sup>, for every X:

Step 2: Enumerate all FD's X  $\rightarrow$  Y, s.t. Y  $\subseteq$  X<sup>+</sup> and X $\cap$ Y =  $\emptyset$ :

$$B \rightarrow D$$
,  $AB \rightarrow CD$ ,  $AD \rightarrow BC$ ,  $BC \rightarrow D$ ,  $ABC \rightarrow D$ ,  $ABD \rightarrow C$ ,  $ACD \rightarrow B$ 

## Another Example

Enrollment(student, major, course, room, time)

student → major major, course → room course → time

What else can we infer ? [ in class ]

Solution is on our group wiki: https://cubist.cs.washington.edu/wiki/index.php/CSE444

## Keys

▶ A superkey is a set of attributes  $A_1, ..., A_n$  s.t. for any other attribute B, we have  $A_1, ..., A_n \rightarrow B$ 

- A key is a minimal superkey
  - I.e. set of attributes which is a superkey and for which no subset is a superkey

## Computing (Super)Keys

- Compute X<sup>+</sup> for all sets X
- ▶ If X<sup>+</sup> = all attributes, then X is a superkey
- List only the minimal X's to get the keys

### Example

Product(name, price, category, color)

name, category → price category → color

What is the key?

### Example

Product(name, price, category, color)

name, category → price category → color

```
What is the key?

(name, category)<sup>+</sup> = { name, category, price, color }

Hence (name, category) is a key
```

### Examples of Keys

Enrollment(student, address, course, room, time)

student → address
room, time → course
student, course → room, time

Find keys at home!

Solution soon on our group wiki: https://cubist.cs.washington.edu/wiki/index.php/CSE444

# **Eliminating Anomalies**

#### Main idea:

 $\rightarrow$  X  $\rightarrow$  A is OK if X is a (super)key

 $\rightarrow$  X  $\rightarrow$  A is not OK otherwise

#### Example

SSN → Name, City

Name	SSN	PhoneNumber	City
Fred	123-45-6789	206-555-1234	Seattle
Fred	123-45-6789	206-555-6543	Seattle
Joe	987-65-4321	908-555-2121	Westfield
Joe	987-65-4321	908-555-1234	Westfield

What is the key?

{SSN, PhoneNumber}

Hence SSN → Name, City is a "bad" dependency

## Key or Keys?

Can we have more than one key?

Given R(A,B,C) define FD's, s.t. there are two or more keys

## Key or Keys?

Can we have more than one key?

Given R(A,B,C) define FD's, s.t. there are two or more keys

$$AB \rightarrow C$$
  
 $BC \rightarrow A$  or  $A \rightarrow BC$   
 $B \rightarrow AC$ 

what are the keys here?
Can you design FDs such that there are three keys?

### Boyce-Codd Normal Form (BCNF)

A simple condition for removing anomalies from relations:

#### A relation R is in BCNF if:

If  $A_1, ..., A_n \rightarrow B$  is a non-trivial dependency in R,

then  $\{A_1, ..., A_n\}$  is a superkey for R

In other words: there are no "bad" FDs

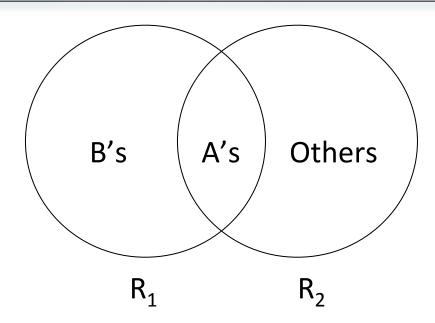
#### **Equivalently:**

for all X, either  $(X^+ = X)$  or  $(X^+ = all attributes)$ 

### BCNF Decomposition Algorithm

#### repeat

choose  $A_1$ , ...,  $A_m \rightarrow B_1$ , ...,  $B_n$  that violates BCNF split R into  $R_1(A_1, ..., A_m, B_1, ..., B_n)$  and  $R_2(A_1, ..., A_m, [others])$  continue with both  $R_1$  and  $R_2$  until no more violations



Is there a
2-attribute
relation that is
not in BCNF?

In practice, we have a better algorithm (coming up)

### Example (revisited)

SSN → Name, City

Name	SSN	PhoneNumber	City
Fred	123-45-6789	206-555-1234	Seattle
Fred	123-45-6789	206-555-6543	Seattle
Joe	987-65-4321	908-555-2121	Westfield
Joe	987-65-4321	908-555-1234	Westfield

What is the key?

{SSN, PhoneNumber}

Hence SSN → Name, City is a "bad" dependency

### Example (revisited)

SSN → Name, City

Name	<u>SSN</u>	City
Fred	123-45-6789	Seattle
Joe	987-65-4321	Westfield

<u>SSN</u>	<u>PhoneNumber</u>
123-45-6789	206-555-1234
123-45-6789	206-555-6543
987-65-4321	908-555-2121
987-65-4321	908-555-1234

#### Let's check anomalies:

- Redundancy?
- Update?
- Delete?

### **Example Decomposition**

Person(name, SSN, age, hairColor, phoneNumber)

 $FD1: SSN \rightarrow name, age$ 

FD2: age → hairColor

Decompose into BCNF (in class):

#### **Example Decomposition**

Person(name, SSN, age, hairColor, phoneNumber)

```
FD1: SSN \rightarrow name, age
    FD2: age → hairColor
Decompose into BCNF (in class):
    What is the key?
                          {SSN, phoneNumber}
But how to decompose?
    Person(SSN, name, age)
    Phone(SSN, hairColor, phoneNumber)
or
    Person(SSN, name, age, hairColor)
    Phone(SSN, phoneNumber)
                                     SSN → name, age, hairColor
or ....
```

### BCNF Decomposition Algorithm

BCNF\_Decompose(R)

find X s.t.:  $X \neq X^+ \neq [all attributes]$ 

if (not found) then "R is in BCNF"

 $\underline{\mathbf{let}} \; \mathsf{Y} = \mathsf{X}^+ - \mathsf{X}$ 

<u>let</u>  $Z = [all attributes] - X^+$ decompose R into  $R_1(X \cup Y)$  and  $R_2(X \cup Z)$ continue to decompose recursively  $R_1$  and  $R_2$ 

### Example BCNF Decomposition

Person(name, SSN, age, hairColor, phoneNumber)

 $FD1: SSN \rightarrow name, age$ 

FD2: age → hairColor

Find X s.t.:  $X \neq X^+ \neq [all attributes]$ 

**Iteration 1: Person** 

SSN<sup>+</sup> = SSN, name, age, hairColor

Decompose into: P(SSN, name, age, hairColor)

Phone(SSN, phoneNumber)

Iteration 2: P

age<sup>+</sup> = age, hairColor

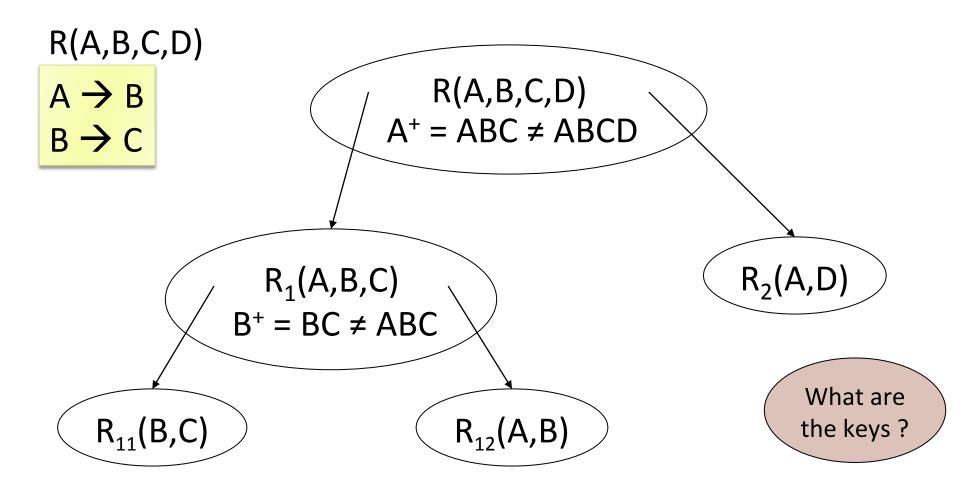
Decompose: People(SSN, name, age)

Hair(age, hairColor)

Phone(SSN, phoneNumber)

What are the keys?

#### Example



What happens if in R we first pick B<sup>+</sup>? Or AB<sup>+</sup>?

### Decompositions in General

$$R(A_{1}, ..., A_{n}, B_{1}, ..., B_{m}, C_{1}, ..., C_{p})$$

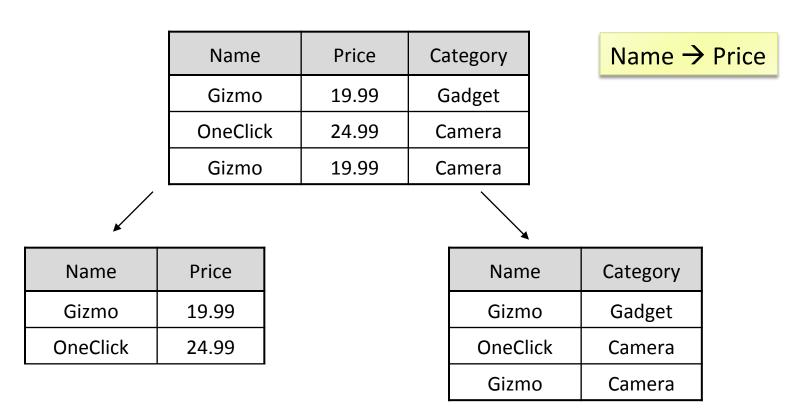
$$R_{1}(A_{1}, ..., A_{n}, B_{1}, ..., B_{m})$$

$$R_{2}(A_{1}, ..., A_{n}, C_{1}, ..., C_{p})$$

$$R_1$$
 = projection of R on  $A_1$ , ...,  $A_n$ ,  $B_1$ , ...,  $B_m$   
 $R_2$  = projection of R on  $A_1$ , ...,  $A_n$ ,  $C_1$ , ...,  $C_p$ 

### Theory of Decomposition

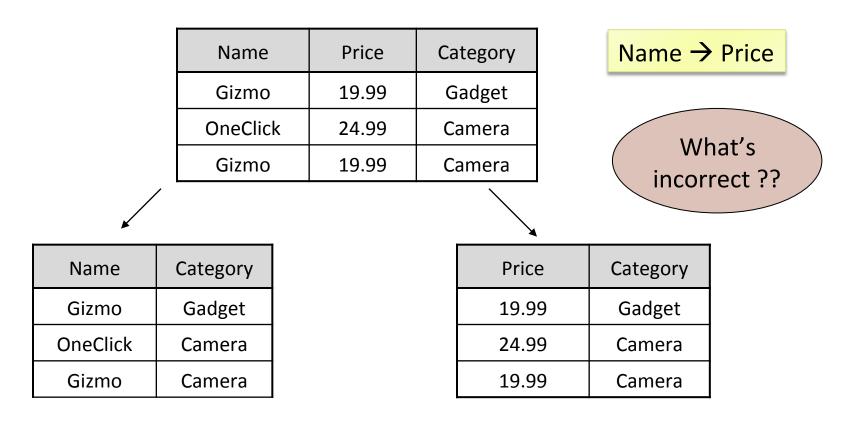
#### Sometimes it is correct:



#### Lossless decomposition

#### Incorrect Decomposition

#### Sometimes it is not:



Lossy decomposition

### Decompositions in General

$$R(A_{1}, ..., A_{n}, B_{1}, ..., B_{m}, C_{1}, ..., C_{p})$$

$$R_{1}(A_{1}, ..., A_{n}, B_{1}, ..., B_{m})$$

$$R_{2}(A_{1}, ..., A_{n}, C_{1}, ..., C_{p})$$

If 
$$A_1, ..., A_n \rightarrow B_1, ..., B_m$$
  
Then the decomposition is lossless

Note: don't need  $A_1, ..., A_n \rightarrow C_1, ..., C_p$ 

BCNF decomposition is always lossless. WHY?

### General Decomposition Goals

Elimination of anomalies

**BCNF** 

- 2. Recoverability of information
  - Can we get the original relation back?

3NF

- 3. Preservation of dependencies
  - Want to enforce FDs without performing joins

Sometimes cannot decompose into BCNF without losing ability to check some FDs in single relation

### BCNF and Dependencies

Unit	Company	Product

Unit → Company
Company, Product → Unit

So, there is a BCNF violation, and we decompose.

Unit	Company

Unit → Company

Unit	Product

No FDs

In BCNF we lose the FD

Company, Product → Unit

#### **3NF Motivation**

#### A relation R is in 3rd normal form if:

Whenever there is a nontrivial dep.  $A_1$ ,  $A_2$ , ...,  $A_n \rightarrow B$  for R, then  $\{A_1, A_2, ..., A_n\}$  is a super-key for R, or B is part of a key.

#### **Tradeoffs:**

BCNF: no anomalies, but may lose some FDs

3NF: keeps all FDs, but may have some anomalies

### Motivation of 4NF and higher

Assume for each course, we can independently choose a lecturer and a book. What is the problem?

#### **Classes**

Course	Lecturer	Book
cse444	Alexandra	Complete book
cse444	Wolfgang	Complete book
cse444	Alexandra	Cow book

Not part of exam!

cse444	Wolfgang	Cow book
	)	

Multi-valued dependency (MVD) Course →→ Lecturer: In every legal instance, each Course value is associated with a set of Lecturer values and this set is independent of the values in the other attributes (here Book).